## V889 HER: ABRUPT CHANGES IN THE MAGNETIC FIELD OR DIFFERENTIAL ROTATION?

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## ABSTRACT

We have applied Zeeman-Doppler imaging (ZDI) to an extensive spectropolarimetric HARPSpol data set of the magnetically active young solar analogue V889 Her, covering 35 spectra obtained during six nights in May 2011. The data set allows us to study Stokes V profiles of the star at almost identical rotational phases, separated by one or more stellar rotations. We use these data to study if the line profiles evolve from one rotation to the next, and find that some evolution does indeed occur. We consider two possible explanations for this: abrupt changes in the large-scale magnetic field or differential rotation. We find it quite difficult to distinguish between the two alternatives using ZDI alone. A strong differential rotation could, however, explain the changes in the line profiles, so we conclude that it must be present, and the abrupt magnetic field evolution is left uncertain. Commonly, rapidly rotating stars are assumed to have only weak differential rotation. If the strong differential rotation of V889 Her is indeed present, as has been found in other studies as well, it could indicate that the theoretical and numerical results of differential rotation still need to be revised. The rapid changes that may have occurred in the magnetic field indicate that one should be quite cautious when interpreting ZDI maps constructed from data over long time intervals.

Subject headings: stars: activity — stars: individual (V889 Her) — stars: magnetic field — stars: solar-type

### 1. INTRODUCTION

Zeeman-Doppler imaging (ZDI) is a powerful tool used to indirectly map the magnetic field at the stellar surface (e.g. Brown et al. 1991; Kochukhov 2016). This is a further development of Doppler imaging (DI; Vogt et al. 1987; Piskunov et al. 1990), which is used to map the surface temperature distribution. The magnetic field is mapped by inverting a series of Stokes I and V profiles (and in some cases also Q and U profiles) of absorption lines, distributed over the stellar rotation phases, thus finding the magnetic field and brightness distribution which reproduces the observed rotational changes in the line profiles. To map the whole visible stellar surface, a good coverage over the rotational phases is required. Depending on the stellar rotation period, this requires observations over many nights, especally for more slowly rotating stars or stars with a rotation period close to a small multiple of one day. In order to produce a sensible ZDI map, one has to assume that the magnetic field does not evolve during these observations. Similarly, with DI, it is assumed that the spot configuration stays

constant through the observations. However, Strassmeier and Bartus (2000) showed that there has been some rapid spot evolution happening in the RS CVn type star V711 Tau. Strassmeier et al. (2003a) analyzed two DI maps from two consecutive rotations of the K giant V1192 Ori, and noted some differences, which they concluded to be due to anti-solar differential rotation. Donati et al. (2016, 2017) noted differences in the magnetic topology of two data sets of the T Tauri type star V830 Tau, which were separated by approximately one month, and were explained with differential rotation. Also Lehtinen et al. (2022) noted some evolution of the Stokes V profiles of the young solar analogue LQ Hya in two data sets with the duration of 9 and 11 consecutive nights.

The rate of changes happening in the magnetic field corresponds to the size of the magnetic structures. Large structures generally evolve slowly, while small structures can evolve more rapidly (Giles et al. 2017). Small-scale fields, however, are difficult to detect with ZDI, since opposite polarities of nearby regions cancel each other out. At worst, ZDI is able to recover less than 1 % of the total magnetic field energy (Kochukhov et al. 2020).

The object of this study, V889 Her, is a magnetically active (log  $R'_{\rm HK} = -4.175$ ; Lehtinen et al. 2016),

young solar analogue, of spectral class G2 V (Montes et al. 2001) and an estimated age of 30-50 million years (Strassmeier et al. 2003b). There are a multitude of published DI and ZDI maps of V889 Her, most recently by Willamo et al. (2019). They published 19 temperature maps of V889 Her, where the main feature was a dark polar spot present in all of them. Previous DI maps have been published by Strassmeier et al. (2003b), Järvinen et al. (2008), Huber et al. (2009) and Frasca et al. (2010), and ZDI maps by Marsden et al. (2006) and Jeffers and Donati (2008), who both found also a strong differential rotation to be present. Huber et al. (2009) found no evidence for differential rotation, and Kővári et al. (2011) found a differential rotation that was an order of magnitude weaker than that found by Marsden et al. (2006) and Jeffers and Donati (2008).

According to both theoretical (Kitchatinov and Rüdiger 1999) and numerical (e.g. Viviani et al. 2018) studies, rapidly rotating stars should not have very strong differential rotation relative to their rotation period. Many observational studies also agree with this (e.g. Reiners and Schmitt 2003; Lehtinen et al. 2016), although, as seen with the conflicting results of V889 Her, the observational results are not as clear. In the study of Reinhold and Gizon (2015) we can see that the differential rotation relative to the rotation rate decreases for rapid rotators, although the absolute rotational shear actually slightly increases. All in all, differential rotation has proven to be a difficult parameter to measure accurately from real stars (see also e.g. Hackman et al. 2019). Since differential rotation is a large unknown factor, it is unclear to what extent it can explain apparent evolution of spectral line profiles, and when these apparent changes correspond to true evolution of the magnetic field or spot structures.

## 2. DATA

We analyze data of V889 Her obtained with the HARPSpol high-resolution spectropolarimeter (Piskunov et al. 2011) at the ESO 3.6m telescope at La Silla, Chile, retrieved from the ESO archives. The observations are from May 15–20, 2011. They were reduced with the REDUCE package (Piskunov and Valenti 2002). Spread over a period of 6 nights and containing a total of 35 individual spectra, this is a data set of remarkably high quality, in terms of the signal-to-noise ratio and phase coverage. See Table 1 for more details. The phase coverage was enhanced by combining only two sub-exposures, instead of the standard four, for the production of LSD profiles (see next Section). Due to this, no null profiles are available for the spectra.

To calculate the rotation phase  $\phi$  of the star we have used the ephemeris:

$$\text{HJD}_{\phi=0} = 2449950.550 + P_{\text{rot}} \times E.$$
 (1)

The rotation period  $P_{\rm rot} = 1.3300 \pm 0.0031$  d was derived using photometry from Willamo et al. (2019), including only the 28 data points between Julian Dates 2455685 and 2455710, corresponding to May 2011. This way we get the best period for this particular data set, and are not affected by fluctuations in the period due to differential rotation or other factors. We determined the best period with the Three Stage Period Analysis method (Jetsu

TABLE 1 Observation log for V889 Her. #Night numbers the observing nights as they are referred to in the text. S/Nis the signal-to-noise ratio of the Stokes LSD V-profile.

#Night	Date (UT)	HJD-2455000	$\phi$	S/N
1	2011 05 15 5:49	696.743	0.446	41833
1	$2011 \ 05 \ 15 \ 6:17$	696.763	0.461	40821
1	2011 05 15 7:51	696.828	0.510	43419
1	2011 05 15 8:19	696.847	0.524	44942
1	$2011 \ 05 \ 15 \ 9:42$	696.905	0.568	37110
1	$2011 \ 05 \ 15 \ 10{:}04$	696.920	0.579	36540
1	$2011 \ 05 \ 15 \ 10{:}27$	696.936	0.591	36018
2	$2011 \ 05 \ 16 \ 5:50$	697.744	0.198	42084
2	$2011 \ 05 \ 16 \ 6:18$	697.763	0.213	42375
2	$2011 \ 05 \ 16 \ 7:50$	697.827	0.261	42257
2	$2011 \ 05 \ 16 \ 8:18$	697.847	0.276	44445
2	$2011 \ 05 \ 16 \ 9:47$	697.908	0.322	42123
2	$2011 \ 05 \ 16 \ 10{:}15$	697.928	0.337	42839
3	$2011 \ 05 \ 17 \ 5:19$	698.722	0.934	41581
3	$2011 \ 05 \ 17 \ 5:47$	698.742	0.949	44364
3	$2011 \ 05 \ 17 \ 8:18$	698.847	0.028	39113
3	$2011 \ 05 \ 17 \ 8:40$	698.862	0.039	37740
3	$2011 \ 05 \ 17 \ 10:05$	698.921	0.083	28415
3	$2011\ 05\ 17\ 10{:}26$	698.936	0.095	27794
4	$2011 \ 05 \ 18 \ 5:23$	699.725	0.688	33248
4	$2011 \ 05 \ 18 \ 5:51$	699.745	0.703	37410
4	$2011 \ 05 \ 18 \ 8:17$	699.846	0.779	37978
4	$2011 \ 05 \ 18 \ 8:38$	699.861	0.790	38071
4	$2011 \ 05 \ 18 \ 9:00$	699.876	0.802	36297
5	$2011 \ 05 \ 19 \ 4:54$	700.705	0.425	34808
5	2011 05 19 5:21	700.724	0.439	31547
5	$2011 \ 05 \ 19 \ 7:55$	700.831	0.520	35895
5	$2011 \ 05 \ 19 \ 8:23$	700.850	0.534	32362
5	$2011 \ 05 \ 19 \ 8:52$	700.870	0.549	34577
6	$2011 \ 05 \ 20 \ 5:19$	701.722	0.189	24631
6	$2011\ 05\ 20\ 5{:}47$	701.742	0.205	26713
6	$2011 \ 05 \ 20 \ 7{:}17$	701.804	0.251	23753
6	$2011 \ 05 \ 20 \ 7{:}45$	701.824	0.266	18648
6	2011 05 20 9:31	701.897	0.321	21406
6	2011 05 20 9:59	701.917	0.336	25625

and Pelt 1999).

### 3. ZEEMAN-DOPPLER IMAGING

As the polarization signal in individual spectral lines, caused by the magnetic field, is too weak to be reliably detected, we use the Least-Square Deconvolution (LSD) method to enhance the signal. The method works by combining thousands of spectral lines into a mean LSD profile (Kochukhov et al. 2010). The line parameters are extracted from the VALD database<sup>1</sup> (Piskunov et al. 1995; Kupka et al. 1999). In the final profiles, 6545 lines between 3900-7100 Å were used, with a mean wavelength 5111.589 Å and a mean Landé *g*-factor 1.215.

We use the code inversLSD, developed by Kochukhov et al. (2014), to invert the ZDI maps. The stellar surface is divided into 1876 elements with approximately equal sizes, and the radial, meridional and azimuthal magnetic field components and the brightness is calculated for each. Instead of modeling directly the magnetic field components, the magnetic field is represented with spherical harmonic expansions , where higher order harmonics represent the magnetic field on smaller scales. For the number of spherical harmonic expansions, Hackman

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<sup>1</sup> http://vald.astro.uu.se/
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et al. (2016) found that increasing maximum angular degree  $\ell_{\max}$  to more than 5 did not significantly improve the fit to the Stokes V profiles. Also Lehtinen et al. (2022) noted, that although they used  $\ell_{\max} = 20$ , most of the magnetic energy was found in harmonics below  $\ell \leq 6$ . Both these studies analyzed stars with somewhat different values for  $v \sin i$  than V889 Her, but still of the same order of magnitude, so these results should be fairly comparable to V889 Her. Similarly to Willamo et al. (2022), we have limited the solution to  $\ell_{\max} = 10$  harmonics.

The magnetic field and brightness inversions are performed simultaneously, so that brightness inhomogeneities are taken into account in the magnetic field inversion. This is necessary, since a lower brightness will lead to a weaker polarization signal, which would be difficult to tell apart from a weaker magnetic field, if the inversions were done independently of each other. For the magnetic field, high-order modes are suppressed by a regularization function, while for the brightness inversion, Tikhonov regularization is used to constrain the solution to distributions with a minimal gradient. Smoother variations are thus preferred over sharper ones. The regularization and other parameters used in the inversion, as well as the stellar parameters, are shown in Table 2. A more thorough description of the regularization can be found in Rosén et al. (2016).

In our previous study of V889 Her (Willamo et al. 2019), the inclination i was set to 60°, following Marsden et al. (2006). However, from the light curve recently obtained by the TESS space telescope<sup>2</sup>, V889 Her seems to have at least one transiting exoplanet, which would indicate that the inclination is close to 90°, if the rotation of the star is aligned with the planetary disk. Thus we set the inclination to a higher value,  $i = 70^{\circ}$ , estimated with the equation:

$$\sin i = \frac{P_{\rm rot} v \sin i}{2\pi R},\tag{2}$$

where  $P_{\text{rot}}$  is the rotation period,  $v \sin i$  the projected rotation velocity, and R the stellar radius. References for these parameters are given in Table 2.

### 4. DIFFERENTIAL ROTATION

The latitudinal differential rotation parameter  $\alpha$  is defined as:

$$\alpha = \frac{\Omega_{\rm eq} - \Omega_{\rm pol}}{\Omega_{\rm eq}},\tag{3}$$

and the absolute latitudinal rotational shear is:

$$\Delta \Omega = \Omega_{\rm eq} - \Omega_{\rm pol},\tag{4}$$

where  $\Omega_{\rm eq}$  and  $\Omega_{\rm pol}$  are the angular velocities at the equator and at the poles, respectively. Published values for the differential rotation of V889 Her are  $\Delta\Omega = 0.402 \pm 0.044$  rad/d (Marsden et al. 2006),  $\Delta\Omega = 0.52 \pm 0.04$  rad/d for Stokes I data and  $\Delta\Omega = 0.47 \pm 0.04$  rad/d for Stokes V data (Jeffers and Donati 2008), and  $\Delta\Omega = 0.042$  rad/d (Kővári et al. 2011). Järvinen et al. (2008) found

<sup>2</sup> Available at

a weaker differential rotation than Marsden et al. (2006), although they did not derive a quantitative value for it, and Huber et al. (2009) found no evidence for differential rotation. In Willamo et al. (2019), V889 Her was assumed to have no differential rotation.

The differential rotation law is assumed to follow the solar differential rotation law, with the higher order terms neglected. The dependence of the surface rotation rate on the latitude  $\theta$  will thus be:

$$\Omega(\theta) = \Omega_{\rm eq}(1 - \alpha \sin^2(\theta)). \tag{5}$$

The differential rotation does not need to necessarily follow the solar differential rotation law, but it is assumed, since we have no information to make reliable guesses about alternative differential rotation laws.

With different values of  $\alpha$ , the rotation period  $P_{\rm rot}$ must also be changed. Since  $P_{\rm rot}$  in the model is measured at the equator, but the observational value comes from the latitude of the dominating spot structure, the optimal value of  $P_{\rm rot}$  is expected to decrease with increasing  $\alpha$ . In practice, the best values for  $\alpha$  and  $P_{\rm rot}$ are found by trying a grid of different values, and finding the minimum for the deviation between model and observations.

### 5. STOKES V PROFILES

The data set analyzed here contains 35 spectra. A typical (Z)DI data set contains perhaps a little more than 10 spectra (e.g. Willamo et al. 2019; Hackman et al. 2019; Lehtinen et al. 2022; Willamo et al. 2022), which, if spread evenly over the rotational phases, already provide a sufficient phase coverage. There are also studies with similar amounts of phases as here, though, for example of V830 Tau (Donati et al. 2017). Our data set of V889 Her also contains some spectra at almost identical phases, which are separated by one or a few rotations. These are essential for the aim of this study, since, if no magnetic field evolution or differential rotation is present, the surface structure seen to the observer, and thus also the line profiles, from these phases should be identical. These multiple observations of the same phase can thus be used as a rough check of the assumption of the stability of the magnetic field over the time span of the observations. They are, however, not very useful for improving the phase coverage, and are thus commonly avoided in the observations due to time limitations, especially when one tries to get sufficient observations of as many stars as possible.

Fig. 1 shows the Stokes LSD I and V profiles of the spectra, and the model fitted to the data, both separately for the first three nights and last three nights. There is especially one pair of profiles at  $\phi = 0.337$  and  $\phi = 0.336$ , where the Stokes V profiles are clearly not identical, although separated only by  $\Delta \phi = 0.001$  (shown together in the lower panel of Fig. 1). The difference between these is evidence that the star cannot have rotated as a solid body with a constant magnetic field structure during these observations, assuming that the rotation period we use is correct. Also phases around  $\phi = 0.2$  (0.198 and 0.213 in the first three nights, 0.189 and 0.205 in the last three nights) and  $\phi = 0.5$  (0.510 and 0.524 in the first three nights, 0.520 in the last three nights) are notably different in the figures.

https://mast.stsci.edu/portal/Mashup/Clients/Mast/Portal. html

 TABLE 2

 Stellar parameters of V889 Her and parameters used in the ZDI inversions.

Parameter	Value	Reference
$P_{\rm rot}$	1.3300 d	This study
$v \sin i$	$38.5 \mathrm{~km/s}$	Willamo et al. $(2019)$
i	$70^{\circ}$	This study
R	$1.09 \ R_{\odot}$	Strassmeier et al. $(2003b)$
Microturbulence	$1.6 \ \mathrm{km/s}$	Järvinen et al. $(2008)$
Macroturbulence	3.0  km/s	Strassmeier et al. (2003b)
Regularization (brightness)	$5 \times 10^{-9}$	
Regularization (magnetic field)	$8 \times 10^{-13}$	
Effective Landé $g$ factor	1.215	
Mean $\lambda$	5630.0  Å	

Active stars, especially M dwarfs, are often showing flaring activity. Whereas flares can affect Stokes I profiles, they should not significantly affect the polarized Stokes V profiles (e.g. Donati et al. 2017). As a G-type star, V889 Her is not expected to show very high levels of flaring activity. A flare would also raise the continuum level of the I profile, which would be seen as a significant weakening of the line. This is not seen in any of the spectra. Thus, flares cannot explain the discrepancies seen at simultaneous rotational phases, as there are multiple examples of differences in the Stokes V profiles of closeby phases.

### 6. ZEEMAN-DOPPLER MAPS

In this section we present the ZDI maps constructed from our data. We first study the case where the star is assumed to rotate as a solid body with no differential rotation and the magnetic field is allowed to evolve between two subsets of the observations. After this we require the magnetic field to stay constant through the observations, and allow for differential rotation. These alternatives are then compared to each other, using the deviation between the model and observations:

$$\sigma = \frac{\sum_{\phi,\lambda} \omega_{\phi,\lambda} (I_{\text{obs},\phi,\lambda} - I_{\text{mod},\phi,\lambda})^2}{n_{\phi} n_{\lambda}}, \qquad (6)$$

where  $I_{\text{obs},\phi,\lambda}$  and  $I_{\text{mod},\phi,\lambda}$  are the observed and modeled intensities at each phase  $\phi$  and wavelength  $\lambda$ ,  $\omega_{\phi,\lambda}$  is the weight of each data point, which is proportional to the square of the S/N of the spectrum, and  $n_{\phi}$  and  $n_{\lambda}$  are the number of phases and wavelength points.  $\sigma$  is shown for each model in Table 3, where we see that the static model with no magnetic field evolution or differential rotation clearly has the highest deviation.

## 6.1. Case 1: Abruptly evolving magnetic field

First we perform the analysis without differential rotation, but allowing the magnetic field to evolve during the observations.

As it was clear from Fig. 1 that without differential rotation the magnetic field had to evolve during the observations, we divided our observation set in two, to get two subsets containing three consecutive nights each, labeled as '1-3' and '4-6'. We also divided a third subset from the data, from which we removed the spectra of the first and last night, thus containing four nights from the middle of the observation set, labeled as '2-5'. It might be questionable whether the magnetic field stays constant even for the period of three or four nights, but by producing separate maps for these subsets, we show that the resulting fields are indeed different.

If we assume one spectrum to cover 10 % of the rotation period, then all six nights combined have a phase coverage  $f_{\phi} = 0.967$ . With the division of the observations to three subsets, we have phase coverages  $f_{\phi,1-3} = 0.744$ for the first set,  $f_{\phi,2-5} = 0.925$  for the middle set and  $f_{\phi,4-6} = 0.674$  for the last set, all being acceptable phase coverages on their own. We used the same inversion parameters for each subset.

The three resulting ZDI maps are shown in Fig. 2, separately for the radial, meridional and azimuthal field components, and the brightness. We see that the subsets 1-3 and 2-5 are very similar, but differ from the subset 4-6, where the magnetic field strength is reduced significantly. If this is the case, then the magnetic field evolution would have happened quite abruptly during the last nights.

The deviation  $\sigma$  for each of these maps is shown in Table 3. To study whether an abruptly changing magnetic field or differential rotation is a better explanation to the data, these values should be compared to the one resulting from the analysis involving differential rotation, which is studied in the next section.

### 6.2. Case 2: Differential rotation

Now we test how well the data can be reconstructed when differential rotation is allowed. This will stretch the magnetic field, which is assumed to be frozen into the stellar surface, but it is otherwise kept constant. A map of the deviation  $\sigma$  for different values of  $\alpha$  and  $P_{\rm rot}$  is shown in Fig. 3. The minimum for  $\sigma$  is found with parameters  $\alpha = 0.075^3$  and  $P_{\rm rot} = 1.31$  d, with  $\sigma = 2.5298 \times 10^{-5}$ . The ZDI map corresponding to these best fit parameters is shown in Fig. 4. The corresponding LSD profiles are shown in Fig. 5. When looking at the profiles, the fits seem fairly good, which could mean that a strong differential rotation can explain the observed apparent line profile evolution even without significant abrupt changes in the magnetic field.

The uncertainty of the differential rotation is difficult to estimate quantitatively. In Fig. 6 we show how  $\sigma$ changes as a function of  $\alpha$ , where the best  $P_{\rm rot}$  value is always chosen for each  $\alpha$ . The minimum of  $\sigma$  is at  $\alpha = 0.075$ , but with a larger  $\alpha$ , the value of  $\sigma$  increases only a little. We did thus not estimate any formal error bars for  $\alpha$ . This demonstrates further the difficulties in

 $<sup>^3</sup>$  This corresponds to  $\Delta\Omega=0.36$  rad/d, slightly less than the values derived by Marsden et al. (2006) and Jeffers and Donati (2008).



FIG. 1.— Upper panel: the Stokes LSD profiles for the three first nights (left) and the three last nights (right). The black lines are the observed LSD profiles, and the red lines are fits made to these. The rotational phase is indicated for each profile. Lower panel: V profiles for the two phases closest to each other, where the difference is most notable. The phase  $\phi = 0.337$  is part of the map for nights 1-3, while the phase  $\phi = 0.336$  is part of the map for nights 4-6, in Fig. 2. This indicates that either a strong differential rotation must be present, or there has been some rapid evolution of the magnetic field.

accurately estimating the amount of differential rotation, even for very high-quality data.

From Table 3 we see that the case with differential rotation is a better fit to the data than the subset 4-6 without differential rotation (note, however, that night 6 has slightly lower S/N than the other nights, which could somewhat increase the value of  $\sigma$  for data sets where this night is included), but subsets 1-3 and 2-5 fit the data better than the model with differential rotation. A clear distinction between the cases is thus quite difficult.

The results above were derived from only Stokes V data. We performed a similar study on I data as well.

The results from the I data, however, indicate a very strong anti-solar-like differential rotation (negative  $\alpha$ ). This is probably artificially caused by the cool polar spot, which has a similar influence on the mean line profile as anti-solar differential rotation would have (Hackman et al. 2019). Tikhonov regularization prefers the solution with the anti-solar differential rotation, since it tries to minimize the temperature gradient. From Fig. 1 one can see that the model for the I profiles is categorically deeper than the observations, which also indicates that the I data is not modeled as well as the V data. Thus, we do not conclude anything based on the differential rotation

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FIG. 2.— Magnetic field and brightness maps for nights 1-3 (up), 2-5 (centre) and 4-6 (down), without differential rotation. The vertical lines correspond to phases used for each map. The horizontal line indicates the limit of the visible surface due to the inclination.



FIG. 3.— Map of the deviation  $\sigma$  for differential rotation parameters of V889 Her. The colour scaling corresponds to the deviation between the model and observations in the respective ZDI map, with the unit being  $10^{-5}$ . The best fit is indicated with a cross.

analysis of the I data, except that the apparent results from I and V data can be radically different. A  $\sigma$  map for the I data is shown in Appendix A.

# 6.3. Case 3: Abruptly evolving magnetic field and differential rotation

The two scenarios, abrupt evolution of the magnetic field and differential rotation, do not exclude each other. We thus still explore the possibility of implementing them both.

With the best fit value for the differential rotation, we tried to repeat the analysis keeping the parameters

TABLE 3 Deviation between the model and observations  $\sigma$  for different data sets and different differential rotation parameters for Stokes V data.

Nights included	$\alpha$	$P_{\rm rot}$	$\sigma  imes 10^{-5}$
1-6	0	1.3300	3.3560
1-3	0	1.3300	1.9456
2-5	0	1.3300	2.1631
4-6	0	1.3300	2.8015
1-6	0.075	1.31	2.5298
1-3	0.075	1.31	1.9440
2-5	0.075	1.31	2.0933
4-6	0.075	1.31	2.6936

 $\alpha = 0.075$  and  $P_{\rm rot} = 1.31$  d, but now inserting them separately to the subsets 1-3, 2-5 and 4-6 of the data. As is seen from Table 3, the inclusion of differential rotation does not much affect  $\sigma$  for subset 1-3, while subsets 2-5 and 4-6 now have a clearly better fit. The ZDI maps of the three subsets, including differential rotation, are shown in Fig. 7. The main features of the maps appear fairly similar as in the maps without differential rotation. Now, though, the magnetic field strength increases from the subset 1-3 to subsets 2-5 and 4-6, while in the maps without differential rotation it decreased from subsets 1-3 and 2-5 to subset 4-6. The corresponding Stokes LSD profiles are shown in Appendix B.

## 7. DISCUSSION

It is evident that a constant magnetic field without differential rotation cannot explain our data. A comparison of the two different alternatives, a rapidly changing magnetic field or solar-like differential rotation, presented in Table 3, reveals that the values for the deviation between model and observations,  $\sigma$ , do not clearly prefer one alternative over the other. For the subset with nights 1-3,



FIG. 4.— Magnetic field and brightness maps for all six nights with differential rotation parameters  $\alpha = 0.075$  and  $P_{\rm rot} = 1.31$  d. The observed phases are not indicated, since with differential rotation there is no unique rotation period. The horizontal line indicates the limit of the visible surface due to the inclination. The maps are shown for the epoch HJD=2455699.0



FIG. 5.— The Stokes profiles for the best value for differential rotation,  $\alpha = 0.075$  and  $P_{\rm rot} = 1.31$  d. The black lines are the observed LSD profiles, and the red lines are fits made to these. The rotational phase is indicated as HJD relative to 2455699.0

 $\sigma$  is very similar with or without differential rotation, whereas for subset 4-6 the solution with differential rotation is preferred. It seems difficult to clearly distinguish between the two cases. The fit to the LSD profiles without magnetic field evolution (Fig. 5) is fairly good, and the inclusion of differential rotation does also decrease  $\sigma$ for the models with magnetic field evolution (although only marginally for nights 1-3). Thus it seems that differential rotation is required to explain the observations. We would argue that the most likely explanation is a situation were differential rotation is present, and some abrupt evolution does indeed also happen in the magnetic field configuration. Indeed, if nights 1-3 and 4-6 are modeled independently, including differential rotation, the resulting magnetic field strengths are different, which is the biggest evidence for the abrupt magnetic

field evolution to be present besides the differential rotation. At longitude 120, there is a radial magnetic field feature in the 4-6 map and possibly 2-5 map, which is missing in the 1-3 map. If this feature is real, its appearance could also explain the observed difference.

The deviation  $\sigma$  increases gradually in all models from nights 1-3 to 2-5 and 4-6. The appearing magnetic region could be an explanation for this, but it could also be explained with the S/N, which is lower for the last nights, especially night 6, and will thus introduce larger residuals between the model and observations. Thus we cannot say with certainty, how significant the possible magnetic field evolution would be.

### 8. IMPLICATIONS FOR ZDI

In this section we assume that the hypothesis of the abruptly evolving magnetic field is true, and discuss its



FIG. 6.— The deviation  $\sigma$  as a function of  $\alpha$ , where for each  $\alpha$  the value for  $P_{\rm rot}$  which minimizes  $\sigma$  is used.

possible implications.

Since this data set is of unusually good quality, when compared to other sets collected for V889 Her, it is impossible to say if it is common for the magnetic field of V889 Her to evolve this rapidly. At least this result demonstrates that (Z)DI maps should be regarded with some caution, and the underlying assumption that the magnetic field stays constant through the time span of the observations should be kept in mind. For example, the observations in Willamo et al. (2019) were generally done over a period of 11 nights, an almost two times longer time span than the six nights analyzed here. Differential rotation was not taken into account in that study either. Its main result, a persistent polar spot, should not be too much affected by abrupt magnetic field evolution or differential rotation, though.

According to the photometry analyzed in Willamo et al. (2019), V889 Her was in a phase of increasing activity in 2011. Around this time, the fairly regular cycle was replaced with a monotonous increase of activity, lasting at least until 2019. It would be reasonable to expect that this kind of abrupt changes in the magnetic field are more common in times of higher activity, such as for the Doppler images published by Willamo et al. (2019) during 2012-2017.

The possibility of rapid magnetic field evolution should be kept in mind for other stars as well. Still, it would be reasonable to assume that the magnetic field of V889 Her might change considerably rapidly, since V889 Her is a very active (log  $R'_{\rm HK} = -4.175$ ; Lehtinen et al. (2016)), rapidly rotating star, with a rotation period of approximately 1.3 days. Also in the study by Lehtinen et al. (2022) of LQ Hya, a similar, almost as rapidly rotating star ( $P_{\rm rot} \approx 1.6$  d), there are a few spectra at close by rotational phases (separated by some stellar rotations), which display some variation in the Stokes V profiles, although much less than in the data analyzed here. In Donati et al. (2016, 2017), ZDI was applied to the T Tauri star V830 Tau ( $P_{\rm rot} \approx 2.7$  d) using two approximately one month long data sets, separated by one month. In this case, there were slight variations in the magnetic topology, which were assigned to differential rotation, but essentially a stable magnetic surface structure and

no apparent problems with ZDI, even for such a long observation span. With less active, more slowly rotating stars, these kind of rapid variations might be less common. Nevertheless, this suggests that rapid variations in the magnetic fields of active stars can happen, and more caution should be applied in the interpretation of results from ZDI. Especially if differential rotation is not taken into account, both of these possible effects can affect the results.

### 9. FIELD DYNAMICS

Regardless of the model for differential rotation or magnetic field evolution, the magnetic field is very much dominated by its poloidal and axisymmetric components. These are listed in Table 4, along with the average and maximum field strength. The magnetic field is notably stronger (average field strength between 1-2 kG in most scenarios<sup>4</sup>) than in the data from 2004 and 2005 from Marsden et al. (2006) and Jeffers and Donati (2008), where the field strength was much below 1 kG. Those magnetic field maps also have a much stronger azimuthal component than our maps. Some changes in the magnetic field topology may thus have occurred. During 2004-2005 V889 Her was close to a spot activity maximum, according to the photometric cycle seen in Willamo et al. (2019), but in 2011 the star had entered a state of higher activity than the previous maximum, as its cyclicity had temporarily been replaced with a monotonous decrease in brightness. The state of higher spot activity may thus explain the stronger magnetic field and different magnetic topology.

It should be noted, that the very axisymmetric magnetic field topology makes the estimation of differential rotation more difficult, and could lead to uncertainties regarding it. Differential rotation is also otherwise known to be a difficult parameter to estimate reliably.

The brightness map, again in all the models for differential rotation or magnetic field evolution, is dominated by a high-latitude spot, which is centered a bit off the pole. The low-latitude features are different in the different models, as is the contrast of the high-latitude spot, but the main result from the brightness map, the persistent polar or high-latitude spot, is the same as in earlier Doppler imaging studies of V889 Her (e.g. Willamo et al. 2019).

Assuming some correlation between spots and magnetic fields, the possible rapid field evolution would indicate that there are spots appearing and disappearing rapidly on V889 Her. Giles et al. (2017) found on their sample of Kepler stars, that hotter stars have shorter spot life times than cooler stars; in their Figure 8, there appear to be spots with short life times, with decay times around 10 days (which they also used as a lower limit for the decay time) only in G and F-type stars, while not in the cooler K and M-stars. As a G-type star, the possible rapid field evolution of V889 Her would fit in this picture.

The most dramatic topological changes, seen in the radial and meridional magnetic field, happen at low lati-

 $<sup>^4</sup>$  The magnetic field strength might exceed the limit for the weak field approximation ( $\approx 1$  kG) that is assumed for the LSD profiles (see Kochukhov et al. 2010), which means that the field strength in regions with the strongest field is not reliable. The order of magnitude should, nevertheless, be correct.

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FIG. 7.— Magnetic field and brightness maps with differential rotation parameters  $\alpha = 0.075$  and  $P_{rot} = 1.31$  d, for subsets with nights 1-3 (up), nights 2-5 (centre) and nights 4-6 (down). The observed phases are not indicated, since with differential rotation the corresponding longitude is not trivial. The horizontal line indicates the limit of the visible surface due to the inclination. All maps are shown for the epoch HJD=2455699.0

TABLE 4

The amounts of poloidal and axisymmetric magnetic field, and the average and maximum magnetic field strength for each model. Multiple definitions for the axisymmetry are shown (with modes  $m < \ell/2$  and m = 0 being counted as axisymmetric). The amounts of toroidal and non-axisymmetric magnetic field can be calculated from these as 100% - the poloidal or axisymmetric component.

Nights included	$\alpha$	$P_{\rm rot}$	$E_{\rm pol}$ [%]	$E_{m < \ell/2}  [\%]$	$E_{m=0}$ [%]	$\langle  B  \rangle$ [G]	$B_{\rm max}$ [G]
1-6	0	1.3300	94	93	90	1050	2720
1-3	0	1.3300	92	89	86	1160	3310
2-5	0	1.3300	96	98	96	1450	3430
4-6	0	1.3300	80	75	59	540	2570
1-6	0.075	1.31	98	98	97	2030	4730
1-3	0.075	1.31	92	90	86	1030	3350
2-5	0.075	1.31	98	98	97	1910	4450
4-6	0.075	1.31	93	86	83	1780	4950

tudes. Note that these changes still take place above the equator – with the spherical harmonic decomposition of the magnetic field, where the sum of the magnetic field penetrating the stellar surface is forced to be zero, the magnetic features below the equator are quite uncertain. This is because we do not have any information of the magnetic field around the invisible pole, and the inversion forces a strong lower latitude magnetic field with opposite polarity to compensate for the observed magnetic field around the visible pole, even though a large part of the magnetic field is probably unobservable to us.

If the possible magnetic field evolution truly happens close to equatorial regions, as the radial feature around longitude 120 could indicate, then one phenomenon, seen in numerical magnetohydrodynamic simulations, which could possibly give an explanation for this, are 'magnetic wreaths'. They are banded, large-scale magnetic structures, which arise at low latitudes on both hemispheres

in simulations of rapidly rotating stars (Brown et al. 2010). More recently, higher-resolution simulations (see, e.g., Viviani et al. 2018) have revealed that these structures can exhibit small-scale structures, as the toroidal band of magnetic field is twisted and obtains a complicated helical structure. This means that it is not only manifested in the azimuthal magnetic field component, but also in the radial and meridional ones. The wreaths show faster and more dynamical behavior than the nonaxisymmetric large-scale structures appearing at higher latitudes in these simulations. Since it is known that there is a large contribution of small-scale fields, which is not captured by ZDI (Kochukhov et al. 2020), the rapid time scale of the magnetic field evolution supports the conclusion that the actual changes in the magnetic field happen on small scales. Since these wreaths have strong structures of small-scale fields, they could be expected to evolve on short time scales, due to rapid processes such

![](_page_9_Figure_1.jpeg)

FIG. 8.— Map of the deviation  $\sigma$  for differential rotation parameters of V889 Her, using Stokes I data. The colour scaling corresponds to the deviation between the model and observations in the respective ZDI map, with the unit being  $10^{-4}$ . The best fit is indicated with a cross.

as reconnection and diffusion. Thus, they provide a possible explanation for the fast low latitude changes seen in V889 Her.

### 10. CONCLUSIONS

We have applied ZDI for an extensive set of spectropolarimetry from six consecutive nights in May 2011 for V889 Her. We showed that a constant magnetic field on a solidly rotating star cannot explain the data. Thus we studied two alternative scenarios; rapid evolution of the magnetic field and differential rotation. From our analysis we conclude that it is not easy to distinguish between these two alternatives from ZDI alone. It is evident that strong differential rotation is present in V889 Her. The abrupt evolution of the magnetic field is not as certain, but it seems likely that at least some evolution has also occurred. Our result disagrees with the theory and models where rapidly rotating stars do not show strong differential rotation (compare our  $\alpha = 0.075$  to e.g.  $\alpha < 0.01$ for simulations with comparable rotation (Viviani et al. 2018), or  $\alpha \lesssim 0.05$  for Kepler stars with  $T_{\rm eff} < 6000$  K in Reinhold and Gizon (2015)). We would also urge to caution, when interpreting results of ZDI from long data

sets, since it seems possible that some evolution of the large-scale magnetic fields of rapid rotators is possible in short time-scales of only a few days.

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# APPENDIX

# DIFFERENTIAL ROTATION FOR STOKES I DATA

## STOKES PROFILES FOR THE MODEL WITH BOTH DIFFERENTIAL ROTATION AND MAGNETIC FIELD EVOLUTION

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![](_page_10_Figure_1.jpeg)

FIG. 9.— The Stokes profiles for the best value for differential rotation,  $\alpha = 0.075$  and  $P_{\text{rot}} = 1.31$  d, when the magnetic field is also allowed to evolve. These are independently modeled for nights 1-3 (left), nights 2-5 (centre) and nights 4-6 (right). The black lines are the observed Stokes LSD profiles, and the red lines are fits made to these.

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