

# ATOMIC DIFFUSION AND MIXING IN OLD STARS. I. VERY LARGE TELESCOPE FLAMES-UVES OBSERVATIONS OF STARS IN NGC 6397<sup>1</sup>

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## ABSTRACT

We present a homogeneous photometric and spectroscopic analysis of 18 stars along the evolutionary sequence of the metal-poor globular cluster NGC 6397 ( $[Fe/H] \approx -2$ ), from the main-sequence turnoff point to red giants below the bump. The spectroscopic stellar parameters, in particular stellar parameter differences between groups of stars, are in good agreement with broadband and Strömgen photometry calibrated on the infrared flux method. The spectroscopic abundance analysis reveals, for the first time, systematic trends of iron abundance with evolutionary stage. Iron is found to be 30% less abundant in the turnoff point stars than in the red giants. An abundance difference in lithium is seen between the turnoff point and warm subgiant stars. The impact of potential systematic errors on these abundance trends (stellar parameters, the hydrostatic and LTE approximations) is quantitatively evaluated and found not to alter our conclusions significantly. Trends for various elements (Li, Mg, Ca, Ti, and Fe) are compared with stellar structure models including the effects of atomic diffusion and radiative acceleration. Such models are found to describe the observed element-specific trends well, if extra (turbulent) mixing just below the convection zone is introduced. It is concluded that atomic diffusion and turbulent mixing are largely responsible for the subprimordial stellar lithium abundances of warm halo stars. Other consequences of atomic diffusion in old metal-poor stars are also discussed.

*Subject headings:* diffusion — globular clusters: individual (NGC 6397) — stars: abundances — stars: atmospheres — stars: evolution — stars: fundamental parameters — stars: interiors — stars: Population II

*Online material:* color figures

## 1. INTRODUCTION

Since the pioneering work of Chamberlain & Aller (1951), stars have been used to trace the chemical evolution of the Milky Way and other galaxies. Due to their long lifetimes, cool stars (of spectral types F to K) are particularly suited for studying the buildup of elements over the course of the past 12–14 Gyr. One of the basic assumptions made in this field of study is that the chemical composition in the atmospheric layers of such stars is representative of the gas out of which the stars once formed. In other words, it is assumed that there are no processes that substantially alter the chemical composition at the surface with time. However, stars are dynamical systems, and various processes (e.g., convection and diffusion) can lead to an exchange of material between the star's interior and its atmosphere.

From the 1970s, such processes have indeed been observed. For example, studies of carbon, nitrogen, and oxygen abundances

in giant stars (Lambert & Ries 1977; Kjaergaard et al. 1982) show clear signs of mixing with material processed in the stellar core, in qualitative agreement with expectations from stellar structure and evolution (Iben 1964). In globular clusters, anticorrelations between certain elements (e.g., O-Na) were also identified among giant stars (Kraft et al. 1997). It was, however, initially unclear whether these are caused by internal mixing processes or external pollution from an earlier generation of more massive stars. With the advent of 8 m-class telescopes during the 1990s, these anticorrelations could be traced in unevolved (turnoff point [TOP]) stars (Gratton et al. 2001, hereafter G01), clearly favoring the external pollution scenario.

Beyond such element-specific effects, models of stellar evolution predict general variations of the atmospheric abundances of elements in unevolved stars on long timescales. Atomic diffusion is expected to be at work in the Sun (Proffitt & Michaud 1991), but larger effects are expected in warm metal-poor stars, as they are generally older and their convective envelopes are thinner. In contrast, giant stars are predicted not to show this effect, as their deep outer convection zones restore the original composition in their atmospheres. From this point of view, giant stars are to be preferred

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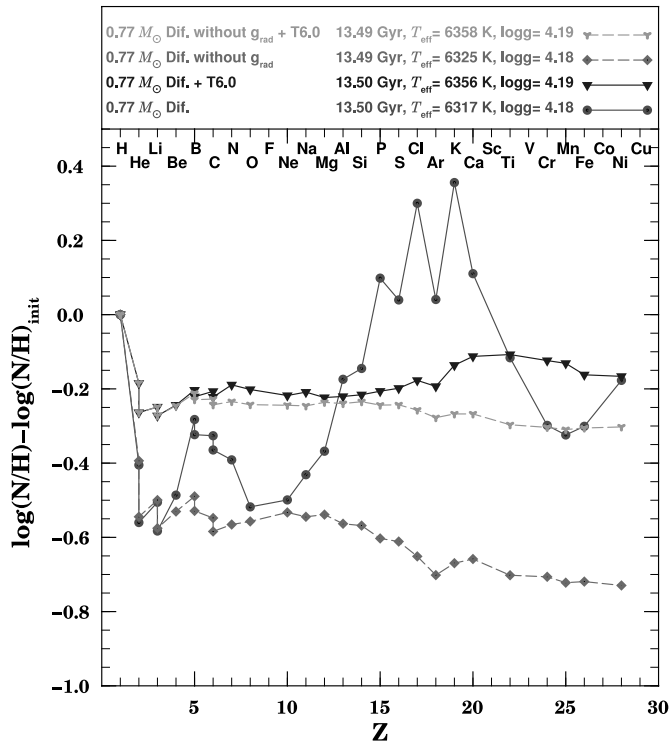


FIG. 1.—Predictions for the variations of atmospheric abundances relative to the initial composition for a  $0.77 M_{\odot}$  star with  $[\text{Fe}/\text{H}] = -2$  that reaches the TOP after 13.5 Gyr. Different symbols/line styles represent different model treating: atomic diffusion including radiative acceleration  $g_{\text{rad}}$  (*filled circles*); atomic diffusion without radiative acceleration (*rhombi*); atomic diffusion including radiative acceleration and turbulent mixing T6.0 (*triangles and solid line*); atomic diffusion without radiative acceleration, but with turbulent mixing T6.0 (*triangles and dashed line*). For details, see § 4 and Richard et al. (2002). [See the electronic edition of the Journal for a color version of this figure.]

as probes of chemical evolution. However, their atmospheric structures may be more poorly known and certain (fragile) elements (e.g., the light elements Li, Be, and B) can only be studied in near-main-sequence stars.

While early models predicted abundance reductions as large as a factor of 10 (Michaud et al. 1984), current models treating atomic diffusion (including radiative acceleration) and mixing below the convection zone suggest abundance effects smaller than a factor of 2 (see Fig. 1). Effects of this size are hard to trace observationally. One needs to compare abundances in unevolved and evolved stars all drawn from the same stellar population. Globular clusters of the Galactic halo offer adequate laboratories to put observational constraints on this theoretical expectation.

King et al. (1998) used the large light-collecting area of the Keck telescope to investigate the chemical composition of stars at the TOP of M92. They note “possible evidence for  $[\text{Fe}/\text{H}]$  differences within M92,” but the design of their study (only observing TOP stars) and the moderate data quality (signal-to-noise ratios  $[\text{S}/\text{Ns}]$  between 10 and 40) precluded firm conclusions. G01 were the first to perform a joint analysis of stars at the TOP and the base of the red giant branch (hereafter bRGB) in two nearby globular clusters, NGC 6397 and NGC 6752, using UVES on the VLT. While the main aim of their study was a detailed investigation of the anticorrelations discussed above, they found no indication of variations in iron abundances between the TOP and the bRGB stars.

Due to the fundamental importance of this result for cosmological studies (e.g., the interpretation of stellar lithium abundances in the framework of big bang nucleosynthesis), we started

TABLE 1  
MEDIAN AND MAXIMUM NUMBER OF OBSERVATIONS IN *uvby*

Filter	Median	Max
<i>u</i> .....	10	16
<i>v</i> .....	11	17
<i>b</i> .....	12	20
<i>y</i> .....	17	27

to reinvestigate the data of G01 in 2003. Data reduction problems in the effective temperature determination were uncovered that, once corrected for, leave room for a decrease of 20% in iron abundance [0.1 dex in  $\log(\text{Fe})$ ] due to atomic diffusion between these two groups of stars (Korn et al. 2006b). This finding prompted us to obtain new data on NGC 6397 in early 2005. Results concerning lithium were published in Korn et al. (2006a); here we give a full account of the analysis.

This article is organized in the following way: In § 2 the observations and data reduction techniques are discussed. The spectroscopic and photometric stellar parameter determinations and spectroscopic abundance analyses are presented in § 3. In § 4 the abundance trends are compared with predictions from stellar evolution models including diffusion. Finally, in §§ 5 and 6 the results are put into astrophysical context and are summarized.

## 2. OBSERVATIONS

### 2.1. Photometry and Target Selection

The photometric data on which our observations are based have been obtained with the Danish 1.54 m telescope on La Silla, Chile. Strömberg *uvby* data were obtained in 1997 May during a 2 week observing run, and additional *BVI* data were obtained in 2005. For all these imaging data the DFOSC instrument was used.

All photometric reductions were carried out using the suite of programs developed by Peter Stetson (Stetson 1987, 1990, 1994). The procedures for standard-star observations and photometric calibration of the *uvby* photometry employed here are identical to those described in Grundahl et al. (1998, 1999, 2000, 2002), and the reader is referred to these papers for further details. The uncertainties in the photometric zero points for *vby* are of the order 0.01 mag, as found in previous studies.

For the *BVI* data we did not observe standard stars since P. Stetson has provided a library of secondary standards through the CADC Web site<sup>3</sup> that are present in our field. We therefore adopted the stars from his list for calibrating the broadband photometry, and thus these stars act as local standards in each frame.

The total field covered by the *uvby* observations is roughly circular with a radius of  $9'$  and was made from several overlapping fields. It is located roughly  $5.5'$  to the west of the cluster center, at (R.A., decl.) = ( $17^{\text{h}}40^{\text{m}}04^{\text{s}}$ ,  $-53^{\circ}39'14''$ ) in the UCAC2 (Zacharias et al. 2004) system. The median and maximum numbers of observations are given for each filter in Table 1. For *BVI* we obtained three exposures in each filter.

Our *uvby* photometric data were also used to select the spectroscopic targets, and since observations are carried out with the fiber-fed multiobject spectrograph FLAMES, accurate astrometry was needed. For this we used the UCAC2 catalog at Vizier.<sup>4</sup> DFOSC is a focal reducer that may have distortion that could affect the astrometric precision. We therefore calibrated each image separately, removed the distortion, and subsequently combined

<sup>3</sup> See <http://cadwww.hia.nrc.ca/cadcbn/wdb/astrocat/stetson/query/>.

<sup>4</sup> See <http://vizier.u-strasbg.fr/viz-bin/VizieR>.

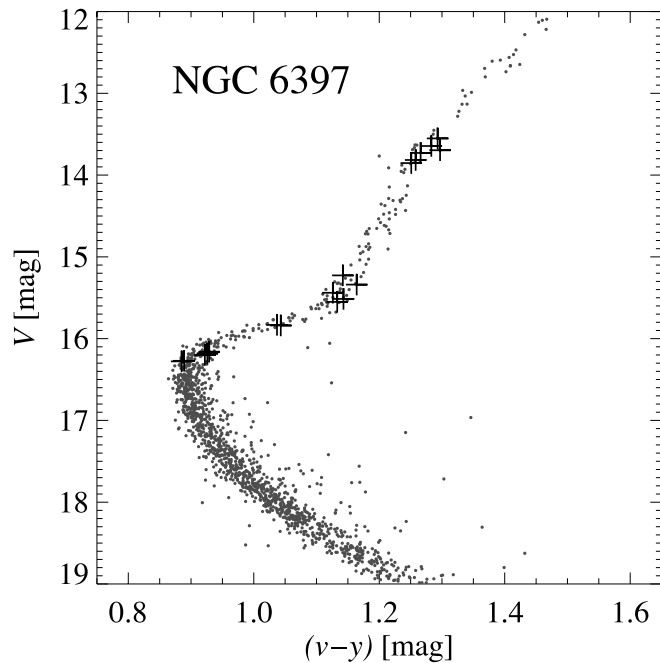


FIG. 2.—CMD of NGC 6397 with the four groups of stars (left to right: TOP, SGB, bRGB, and RGB) marked by crosses. [See the electronic edition of the *Journal* for a color version of this figure.]

all the images to obtain the astrometry for each target. The astrometric precision is of the order  $0.10''$  for individual stars. The stars, their designations, and J2000.0 positions are given in Table 9 of Appendix B.

## 2.2. FLAMES + UVES Observations

The FLAMES instrument (Pasquini et al. 2002) has a combined mode that allows the simultaneous observation of up to eight objects with UVES and 130 objects with GIRAFFE-MEDUSA. Here we only report on the observations with FLAMES-UVES; the

analysis of the GIRAFFE-MEDUSA data will be presented in a forthcoming paper (K. Lind et al. 2008, in preparation).

The total exposure time of  $\approx 20.5$  hr was split between three groups of stars, TOP, bRGB, and RGB stars (see Fig. 2 and Table 2). Two stars in the middle of the subgiant branch (hereafter SGB stars) were always observed in conjunction with the other groups of stars. With five to six stars in each group, this left one fiber to monitor the sky background. We reobserved some of the stars observed by G01, three in each of the two groups (TOP and bRGB).

The wavelength coverage of the FLAMES-UVES spectra is 4800–6800 Å, with a small CCD gap around 5800 Å. The resolving power is  $R = 47,000$ . As seen in Table 2, the peak S/N per pixel varies between 56 (TOP star 507433) and 151 (RGB star 11093), while the average S/N in each group is more homogeneous and varies between 66 (TOP group) and 112 (SGB/RGB group). These values were computed from the rather line-free region around 5725 Å after rebinning by a factor of 2 (the rebinning does not degrade the resolution, as one resolution element consists of 5 pixels). The S/N remains roughly constant redward of 5725 Å, while it gradually degrades (by  $\leq 20\%$ ) toward the blue end of the spectrum at 4800 Å. In total, the S/N for the RGB stars is in line with the expectations from the FLAMES-UVES exposure time calculator, while it falls short for the TOP stars by about 50%. At least in part this can be attributed to the sky correction, which inevitably adds noise.

For comparison, the five TOP stars observed with UVES in slit mode by G01 had a total integration time of 20 hr, achieving S/Ns between 60 and 90 at a resolving power of  $R = 40,000$ . With FLAMES-UVES, we thus profit from a significant multiplexing advantage (at the dispense of wavelength coverage in the blue).

Barycentric radial velocities were computed from radial velocity measurements using several strong Mg I and Fe I lines. As shown in Table 2, barycentric radial velocities of individual stars scatter around a mean value of  $17.5 \text{ km s}^{-1}$ . This compares well with the mean radial velocity for NGC 6397 of  $18.9 \text{ km s}^{-1}$  given by Harris (1996). With typical velocity dispersions of  $5\text{--}10 \text{ km s}^{-1}$  for old globular clusters, all stars are found to be kinematic cluster

TABLE 2  
OBSERVATIONAL DATA OF THE NGC 6397 STARS OBSERVED WITH FLAMES-UVES

GROUP	STAR ID		$V$	$n_{\text{exp}}$	$t_{\text{exp}}$ (hr)	S/N <sub>tot</sub> <sup>a</sup> (pixel <sup>-1</sup> )	CORRECTED FOR SKY	$v_{\text{rad}}^{\text{bary}} \pm 1 \sigma$ (km s <sup>-1</sup> )
	This Work	G01						
TOP	9655	1622	16.20	12	12.75	75	Yes	$16.1 \pm 0.4$
	10197	...	16.16	12	12.75	69	Yes	$13.4 \pm 0.3$
	12318	...	16.18	12	12.75	68	Yes	$19.1 \pm 0.4$
	506120	202765	16.27	12	12.75	63	Yes	$24.4 \pm 0.3$
	507433	201432	16.28	12	12.75	56	Yes	$20.7 \pm 0.3$
SGB	5281	...	15.84	20	20.45	114	Yes	$18.8 \pm 0.2$
	8298	...	15.83	20	20.45	110	Yes	$17.9 \pm 0.2$
bRGB	3330	...	15.22	6	6.20	97	Yes	$17.9 \pm 0.1$
	6391	793	15.55	6	6.20	75	Yes	$16.6 \pm 0.1$
	15105	...	15.44	6	6.20	76	Yes	$19.6 \pm 0.1$
	23267	669	15.34	6	6.20	77	Yes	$17.1 \pm 0.1$
	500949	206810	15.51	6	6.20	76	Yes	$15.1 \pm 0.1$
RGB	4859	...	13.82	2	1.50	117	No	$17.9 \pm 0.1$
	7189	...	13.73	2	1.50	102	No	$15.7 \pm 0.1$
	11093	...	13.55	2	1.50	151	No	$19.1 \pm 0.1$
	13092	...	13.64	2	1.50	111	No	$15.6 \pm 0.1$
	14592	...	13.70	2	1.50	104	No	$15.6 \pm 0.1$
	502074	...	13.85	2	1.50	87	No	$13.5 \pm 0.1$

<sup>a</sup> Computed from the  $n_{\text{exp}}$  co-added spectra in the wavelength range around 5725 Å.

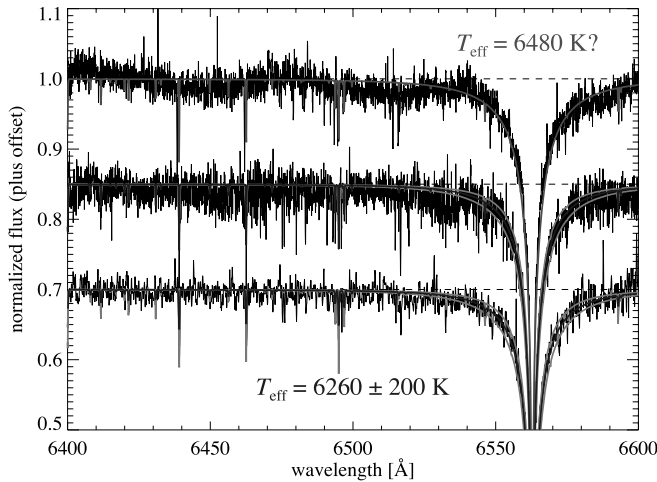


FIG. 3.—Three spectra of the TOP star 507433 taken with UVES in slit mode (*top*), FLAMES-UVES (*middle*), and GIRAFFE-MEDUSA (*bottom*). All spectra are normalized using linear rectification curves. The UVES spectrum suffers from data reduction problems as discussed in § 2.3. Both the FLAMES-UVES and the GIRAFFE-MEDUSA spectra indicate an effective temperature of  $T_{\text{eff}} = 6260 \text{ K}$ . [See the electronic edition of the *Journal* for a color version of this figure.]

members. Our abundance analysis confirms cluster membership for all stars analyzed.

### 2.3. Data Reduction

We make use of the FLAMES-UVES data reduction pipeline. After careful inspection of the behavior of the continuum, we found this pipeline to yield a sufficiently well behaved run of the continuum to recover the intrinsic profile of lines as wide as or wider than the free spectral range (FSR) of UVES (70 Å at H $\alpha$ ). The fiber feed to UVES improves the echelle blaze removal, as both the star and the flat-field lamp illuminate the spectrograph in the same way. As shown in Figure 3, this is not the case when UVES is used as a slit spectrograph: the blaze removal and subsequent order merging as implemented in the UVES pipeline leave significant residuals from which the analysis by G01 was shown to suffer (Korn et al. 2006b).

The individual exposures are corrected for fiber-to-fiber throughput, and the sky as monitored by one fiber is subtracted. They are co-added using MIDAS and C routines kindly made available by N. Christlieb.

## 3. ANALYSIS

We perform independent photometric and spectroscopic analyses to derive the fundamental stellar parameters  $T_{\text{eff}}$  and  $\log g$ . While it is desirable to achieve stellar parameters as free of systematic errors as possible, the detection of abundance differences between groups of stars basically requires stellar parameter *differences* that are free of systematic effects. Thus, for abundances derived from minority species like Li I, Mg I, and Fe I,  $\Delta T_{\text{eff}} = T_{\text{eff}}(\text{TOP}) - T_{\text{eff}}(\text{RGB})$  is the most pertinent quantity, while majority species like Ti II, Fe II, and Ba II react most sensitively to  $\Delta \log g = \log g(\text{TOP}) - \log g(\text{RGB})$ .

### 3.1. Photometry

Apart from providing the spectroscopic targets for our observations, the photometry can also be used to estimate the basic stellar parameters, such as effective temperature and surface gravity independently of the spectroscopic analysis. Here we describe the approach used to estimate these quantities.

It was found that our targets showed some scatter around the observed cluster sequences, most likely due to crowding effects and observational errors in the photometry. At the TOP, duplicity may play a role. In order to reduce this effect, we derived mean cluster fiducial sequences by first cleaning the photometry lists based on photometric quality (the DAOPHOT SHARP parameter) and location in the cluster (crowding). We then divided the  $V$  magnitudes into 0.22 mag bins, and for each of these bins the *same* stars were averaged (using robust estimation routines from the Astrolib library) for each filter (*uvbyBVI*) to produce mean fiducial points for each band.

When deriving effective temperatures based on photometry, we use color indices, and to ensure that these properly represent the cluster sequence, we overplotted the fiducial points on the cluster color-magnitude diagram (CMD) for each color-magnitude combination employed, for example, a ( $v - y$ ,  $V$ ) diagram. We estimate that the error in the color difference between the RGB and the cluster TOP is less than 0.01 mag, and we adopt this as our uncertainty estimate of this quantity.

Armed with the fiducial sequences, we proceed to derive fiducial colors for our target stars by interpolating their color in the fiducial sequence at their observed  $V$  magnitude. This approach effectively removes the star-to-star spread at any given magnitude and is the best we can do since our  $V$  magnitudes are the best calibrated and have the highest number of observations per star.

#### 3.1.1. Effective Temperatures

To estimate the effective temperatures, we use the empirical color calibrations by Alonso et al. (1996, 1999) and Ramírez & Meléndez (2005). When using the *uvby* system, it has been found that the  $v - y$  index gives a superior temperature discrimination for RGB and TOP stars compared to the ( $b - y$ ), which is normally used. Since such calibrations had not been derived by either Alonso et al. (1996, 1999) or Ramírez & Meléndez (2005), we asked them to derive new calibrations for different color combinations and then used these (A. Alonso and I. Ramírez 2006, private communication).

We present the new calibrations in Table 8 of Appendix B in the form of coefficients for the analytic formulae given in the respective original papers by Alonso et al. (1996, 1999) and Ramírez & Meléndez (2005).

Before applying the color-temperature calibrations, we discuss the cluster reddening since the calibrations employ the reddening-corrected colors. NGC 6397 has a nonnegligible reddening, and several estimates are available in the literature (Harris 1996). Following Anthony-Twarog & Twarog (2000), we adopt a value of  $E(B - V) = 0.179 \pm 0.003$ , a value very similar to the one derived by G01. To correct for reddening for the other photometric bands employed here, we use the coefficients given in Table 1 of Ramírez & Meléndez (2005).

For each target star we then derived effective temperatures based on the available colors. We calculated each star's effective temperature using both the dwarf and giant star calibrations. The resulting effective temperatures for each target are given in Table 9.

For the calibrations used we find that the ( $v - y$ ) calibration has a sensitivity of 22 and 38 K per 0.01 mag change in ( $v - y$ ) for giants and turnoff stars at  $[\text{Fe}/\text{H}] = -2.0$ , respectively. The ( $V - I$ ) color shows approximately the same sensitivity, i.e., with changes of around 20 and 40 K for the giant and dwarf calibrations, respectively. For a change of  $\pm 0.1$  dex in  $[\text{Fe}/\text{H}]$  the effective temperature changes by  $\pm 20$  K. We have used a metallicity of  $-2.0$  throughout for calculating effective temperatures, thus not making any implicit assumption about the existence of atomic diffusion.

As presented in Table 9, the  $\Delta T_{\text{eff}}$  values vary between 906 ( $B - V$ ) and 1108 K ( $b - y$ ). The other two calibrations both point to a  $\Delta T_{\text{eff}}$  close to 1100 K, indicating that  $B - V$  may underestimate the effective temperature differences between TOP and RGB stars.

Larger  $\Delta T_{\text{eff}}$  values seem possible based on Two Micron All Sky Survey (2MASS)  $V - J$ ,  $V - H$ , and  $V - K$  colors. However, at the magnitudes of TOP stars in NGC 6397, the 2MASS magnitudes have substantial uncertainties. More accurate infrared photometry would be desirable to reach the accuracy needed for studies like these.

### 3.1.2. Surface Gravities

Surface gravities were derived from the usual relation between  $\log g$  and the luminosity, temperature, and mass of the observed stars. We assumed a mass of  $0.779 M_{\odot}$  for the TOP stars and  $0.792 M_{\odot}$  for the RGB stars based on 13.5 Gyr isochrones of Richard et al. (2005). This is an upper limit for the age of NGC 6397, and the masses are therefore lower limits. The bias on the surface gravities introduced by these assumptions is, however, insignificant.

In order to determine the luminosity of the stars, we have to derive their bolometric corrections, and this was done using the calibrations of Alonso et al. (1999) assuming a metallicity of  $-2.0$  (as was done for the temperature derivation). For our estimated uncertainties in  $V$  (0.01 mag), metallicity (0.1 dex), and stellar mass ( $0.01 M_{\odot}$ ), the error in the determination of the effective temperature is the dominant error source in the determination of the  $\log g$  differences. An error of 50 K for the effective temperature difference translates into a change of 0.015 dex in  $\Delta \log g$ . For the calculation of the absolute surface gravities a value of  $(m - M)_V = 12.57$  was assumed. Given the reddening of the cluster, this value is well within the range determined by Reid & Gizis (1998). We note that the assumed values of  $(m - M)$  and reddening are secondary for the results of this work.

Here  $\Delta \log g_{\text{phot}}$  is determined to be  $1.38 \pm 0.05$ . The error is estimated from an uncertainty in effective temperature for each group of stars of 100 K. Given the multiple observations and targets, this is a rather conservative error estimate.

## 3.2. Spectroscopy

The spectroscopic analysis combines the constraints from fitting the wings of  $H\alpha$  and the iron ionization equilibrium ( $\text{Fe I/II}$ ) in non-LTE (NLTE) to iteratively derive reddening-free estimates of  $T_{\text{eff}}$ ,  $\log g$ , the metallicity  $[\text{Fe}/\text{H}]$ , and the microturbulence  $\xi$ . The analysis is line-by-line differential to the Sun and follows the techniques described in Korn et al. (2003). It employs profile fits rather than equivalent widths.

The model atmosphere code used is MAFAGS (Grupp 2004) and employs the opacity distribution functions (ODFs) of Kurucz (1993). To fulfill the constraints of Balmer line profile fitting, a low value for the mixing-length parameter ( $\alpha_{\text{MLT}} = 0.5$ ) is used (Fuhrmann et al. 1993). This choice has a minor effect on metal lines, as they originate from shallower optical depth. Of all the Balmer lines,  $H\alpha$  is least affected by the choice of  $\alpha_{\text{MLT}} = 0.5$ . An enhancement of the  $\alpha$ -elements O, Mg, and Si by 0.5, 0.4, and 0.4 dex is used in the construction of the model atmosphere, as these elements can make significant contributions to the electron pressure and thus to the continuous opacity produced by  $\text{H}^-$ .

Test calculations with MARCS model atmospheres (Gustafsson et al. 1975; Asplund et al. 1997) show very similar results, for both the effective temperatures (see § 3.2.1) and the relative abundances. This is not surprising, as the input physics is very similar in both

program suites. Differences in the opacity treatment (ODF vs. opacity sampling) are not large at these low metallicities.

### 3.2.1. Effective Temperatures

For consistency with Korn et al. (2003) we use the resonance broadening theory of Ali & Griem (1966). While the self-broadening theory of Barklem et al. (2000) describes the neutral-particle interaction more realistically, the impact on the effective temperatures is small (20–40 K, as shown by test calculations with MARCS) when the analysis is done differentially to the Sun. This is because the improved self-broadening theory produces stronger theoretical profiles for both the Sun and metal-poor stars analyzed here. Parameter  $\Delta T_{\text{eff}}$  is affected by 20 K ( $<0.2\%$ ), which is not significant for our conclusions. This also means that broadening theory differences cannot explain the effective temperature differences between G01 and this study. A direct comparison of theoretical profiles (R. Gratton 2005, private communication) indicated that differences in the implementation (model atmosphere, broadening, etc.) are of the order of 50 K.

The effective temperature determination is done in two steps: First, the spectral region of  $H\alpha$  is normalized using continuum points at least  $\pm 50 \text{ \AA}$  away from the line center. These points are linearly interpolated across the  $H\alpha$  profile to obtain a normalized spectrum. Second, the normalized  $H\alpha$  profile is compared with theoretical profiles by eye to achieve a good overall agreement between theory and observation. The core of  $H\alpha$  (the innermost  $\pm 2 \text{ \AA}$ , residual flux below 0.75) is disregarded.

Figure 3 shows the spectrum of TOP 507433 (G01's target 201432) around  $H\alpha$ . The UVES spectrum (*top panel*; kindly made available by E. Carretta) shows echelle blaze and order-merging residuals with an amplitude of  $\pm 2\%$ , which limit the effective temperature determination to an accuracy of  $\pm 200 \text{ K}$ . However, the error associated with the residual order pattern is likely to have a systematic effect on the effective temperature determination, as the Balmer line wings are systematically suppressed ( $H\alpha$  falls into the convex part of this pattern). Thus, an overestimation of  $T_{\text{eff}}$  by as much as 200 K appears possible (Korn et al. 2006b). This conclusion is supported by the FLAMES-UVES spectrum (*middle panel*) of the same star, which does not seem to suffer from these instrumental artifacts. An effective temperature of 6260 K is derived, a value that also finds support from the analysis of the GIRAFFE-MEDUSA spectrum (*bottom panel*;  $R = 29,000$ ,  $\text{FSR} \geq 200 \text{ \AA}$ ) of this star (K. Lind et al. 2008, in preparation). A careful reanalysis of the archival data of G01 for this star using the REDUCE software package (Piskunov & Valenti 2002) pointed toward an effective temperature of  $T_{\text{eff}} = 6230 \text{ K}$ , again in line with the new spectra obtained.

We note that the problems encountered with the UVES spectra have a far smaller influence on the effective temperature determination of the bRGB (and RGB) stars, as their Balmer line profiles are significantly narrower (see Fig. 4).

If we assume an uncertainty for deriving  $T_{\text{eff}}$  for an individual star to be 200 K, then  $\Delta T_{\text{eff}}(\text{TOP} - \text{RGB})$  turns out to be  $1124 \pm 120 \text{ K}$  (see Table 3). This value is in excellent agreement with the majority of the photometric indices presented in Table 9 and discussed above.

### 3.2.2. Surface Gravities

The iron ionization equilibrium is used to constrain  $\log g$  via the requirement that Fe I and Fe II lines show the same mean abundance. Fe I is modeled in NLTE, using the photoionization cross sections computed by Bautista (1997), modeling in detail the UV fluxes and treating inelastic collisions with hydrogen according to Drawin (1969) and Steenbock & Holweger (1984)

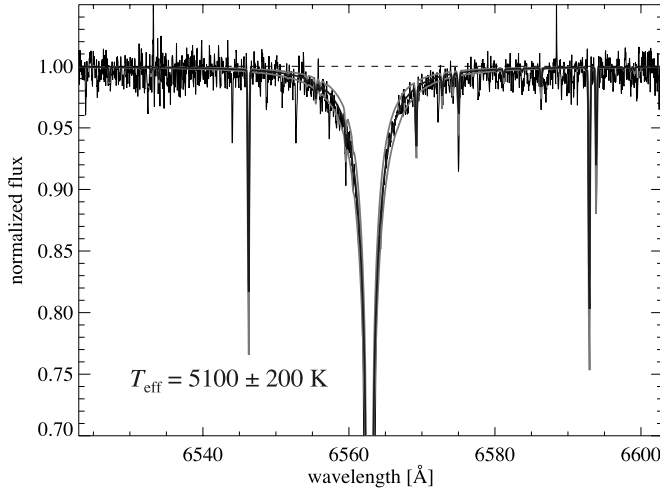


FIG. 4.—FLAMES-UVES spectrum of the RGB star 11093. The Balmer line is significantly weaker than in the TOP stars, but the effective temperature sensitivity coupled with the higher S/N allows constraining  $T_{\text{eff}}$  to  $\pm 200$  K. [See the electronic edition of the *Journal* for a color version of this figure.]

with a scaling factor of 3 (for details see Korn et al. 2003 and references therein). At the same time, the microturbulence is derived by requiring that Fe I and Fe II line abundances show no trend with line strength.

The iron ionization equilibrium is considered as established if the difference in the mean abundances derived from Fe I and Fe II is 0.01 dex or less. This means that we determine  $\log g$  values with an accuracy of 0.03 dex.

It is worth noting that overionization in Fe I is found to be only 0.03–0.05 dex for all stars (this is because the calibrated NLTE model employs rather efficient hydrogen collisions). This means

that the absolute  $\log g$  values are raised by about 0.1 dex for all stars compared to the LTE case. There are practically no differential NLTE effects. In this sense, our conclusions are not affected by particular choices as regards the underlying line formation theory.

Here  $\Delta \log g$  is determined to be  $1.33 \pm 0.12$  (assuming an uncertainty of 0.2 dex in  $\log g$  for the individual star; see Table 3). This compares very favorably with the photometric estimates based on  $\Delta V$  of  $\Delta \log g_{\text{phot}} = 1.38 \pm 0.05$ .

We note that some authors find smaller microturbulence values for TOP stars. For example, G01 assign a common microturbulence of  $\xi = 1.32 \text{ km s}^{-1}$  to their TOP stars. With a mean  $\xi$  of  $2 \text{ km s}^{-1}$ , our TOP star analyses give systematically higher values. However, these values are only marginally ( $0.2 \text{ km s}^{-1}$ ) higher than the value derived for local TOP star HD 84937 ( $T_{\text{eff}} = 6350 \text{ K}$ ,  $\log g = 4.0$ ,  $[\text{Fe}/\text{H}] = -2.16$ ,  $\xi = 1.8 \text{ km s}^{-1}$ ) using the same methodology (for details see Korn et al. 2003). The higher microturbulence values could be caused by the line selection, which in turn is constrained by the wavelength coverage and the S/N. To minimize the impact of this parameter on the overall analysis, we made an effort to base the analysis on lines as weak as possible (see Appendix A). Simultaneously, such weak lines have the highest possible abundance sensitivity. Figure 5 give examples of the line abundances as a function of line strength and excitation energy for a TOP and an RGB star.

### 3.3. Comparison between Photometry and Spectroscopy

The best agreement between photometry and spectroscopy is obtained for the Strömgren indices  $(b - y)$  and  $(v - y)$ .  $(V - I)$  performs as well as  $(v - y)$  as regards  $\Delta T_{\text{eff}}$ , but the absolute effective temperatures are offset toward cooler temperatures by roughly 100 K.  $B - V$  indicates a smaller  $\Delta T_{\text{eff}}$  of 906 K. The agreement with the spectroscopic  $\Delta T_{\text{eff}}$  is thus excellent for three out of four color indices.

TABLE 3  
SPECTROSCOPIC STELLAR PARAMETERS OF THE 18 STARS OBSERVED WITH FLAMES-UVES

GROUP	STAR ID		$T_{\text{eff}}$ (K)	$\log g$ (cgs)	$[\text{Fe}/\text{H}] \pm 1 \sigma$ (dex)	$\xi$ ( $\text{km s}^{-1}$ )
	This Work	G01				
TOP .....	9655	1622	6260	3.85	$-2.29 \pm 0.06$ (22)	2.1
	10197	...	6250	3.95	$-2.29 \pm 0.10$ (21)	2.0
	12318	...	6240	3.90	$-2.28 \pm 0.08$ (21)	2.0
	506120	202765	6260	3.85	$-2.26 \pm 0.09$ (23)	1.9
	507433	201432	6260	3.90	$-2.26 \pm 0.06$ (20)	2.0
SGB .....	5281	...	5800	3.55	$-2.25 \pm 0.08$ (26)	1.75
	8298	...	5810	3.60	$-2.23 \pm 0.07$ (24)	1.75
bRGB .....	3330	...	5430	3.35	$-2.16 \pm 0.08$ (24)	1.7
	6391	793	5510	3.40	$-2.14 \pm 0.09$ (29)	1.6
	15105	...	5470	3.40	$-2.18 \pm 0.07$ (25)	1.75
	23267	669	5370	3.30	$-2.23 \pm 0.09$ (27)	1.8
	500949	206810	5500	3.40	$-2.19 \pm 0.09$ (25)	1.8
RGB .....	4859	...	5150	2.65	$-2.12 \pm 0.08$ (38)	1.6
	7189	...	5130	2.55	$-2.14 \pm 0.08$ (36)	1.6
	11093	...	5100	2.50	$-2.14 \pm 0.08$ (42)	1.7
	13092	...	5120	2.55	$-2.12 \pm 0.08$ (38)	1.6
	14592	...	5130	2.55	$-2.12 \pm 0.08$ (37)	1.6
	502074	...	5150	2.60	$-2.10 \pm 0.09$ (35)	1.5
TOP <sub>ave</sub> .....	...	...	$6254 \pm 90$	$3.89 \pm 0.09$	$-2.28 \pm 0.04$	$2.0 \pm 0.1$
SGB <sub>ave</sub> .....	...	...	$5805 \pm 140$	$3.58 \pm 0.14$	$-2.24 \pm 0.05$	$1.75 \pm 0.15$
bRGB <sub>ave</sub> .....	...	...	$5456 \pm 90$	$3.37 \pm 0.09$	$-2.18 \pm 0.04$	$1.73 \pm 0.1$
RGB <sub>ave</sub> .....	...	...	$5130 \pm 80$	$2.56 \pm 0.08$	$-2.12 \pm 0.03$	$1.6 \pm 0.1$

NOTES.—The standard deviation for all Fe I and Fe II lines measured (total number of lines in parentheses) is given. For  $T_{\text{eff}}$ ,  $\log g$ , and  $\xi$ , measurement uncertainties of 200 K, 0.2 dex, and  $0.2 \text{ km s}^{-1}$  are assumed, respectively. These errors are propagated into the error for the group-averaged properties given at the bottom of the table.

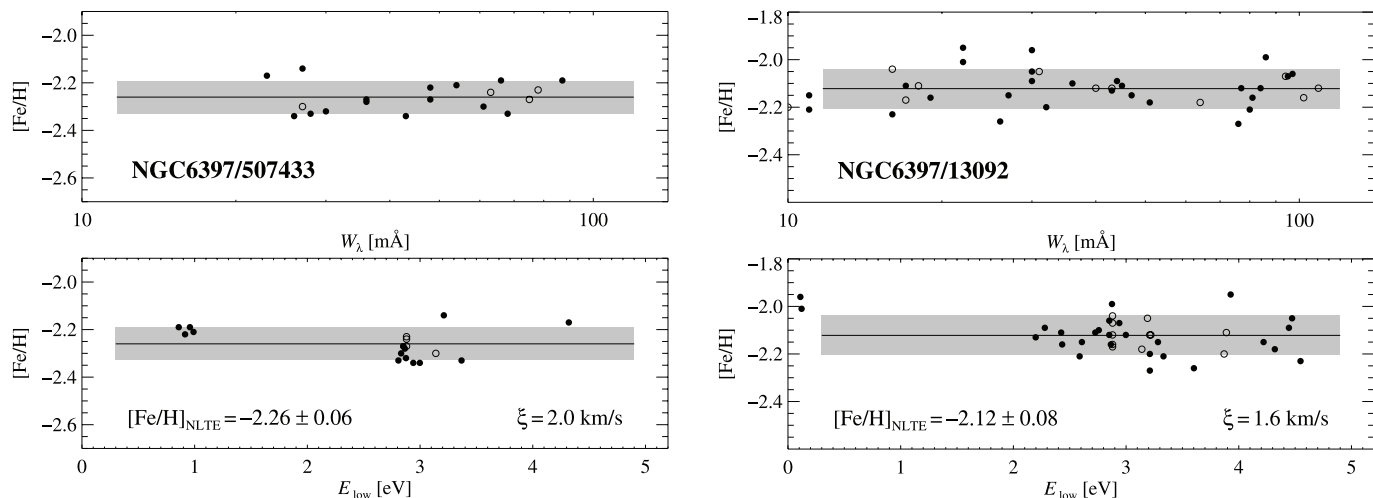


FIG. 5.— Individual line abundances of Fe I (*filled circles*) and Fe II (*open circles*) lines as a function of line strength (*top*) and excitation energy of the lower level  $E_{low}$  (*bottom*) for a TOP star and an RGB star, respectively. While there is no obvious trend of  $[Fe/H]$  with  $E_{low}$ , this is not true for all targets and we do not use the excitation equilibrium as an additional effective temperature indicator.

Due to the low sensitivity of the photometric  $\Delta \log g$  values to  $\Delta T_{eff}$ , all indices indicate a  $\Delta \log g$  of around 1.38 [only  $(B - V)$  points toward a value of 1.31]. All these values are fully compatible with the spectroscopic value of  $1.33 \pm 0.12$ .

#### 3.4. Comparison with Other Studies on NGC 6397

It now becomes clear why we find abundance trends where G01 reported iron abundances of TOP and bRGB stars to “agree perfectly”: the difference lies in the effective temperatures assigned to the TOP stars, which results in a lower effective temperature difference relative to other groups of stars (bRGB or RGB stars; see above). For bRGB star 6391 (G01’s target 793), we derived  $T_{eff} = 5480$  K, confirming the effective temperature estimate of G01 (Korn et al. 2006b).

The new spectroscopic effective temperatures are judged to be more trustworthy (see § 2.3). Furthermore, the new effective temperatures find independent support from photometry and from the fact that the iron ionization equilibrium could be established for all stars. Neither of these requirements was included in the G01 analysis.<sup>5</sup>

The effective temperature difference between TOP and bRGB stars is spectroscopically determined to be 798 K, and three of the four photometric indices point toward values between 806 and 833 K.  $(B - V)$  predicts a markedly lower effective temperature difference of 615 K. All these values are significantly lower than the 1000 K derived by G01.

As a result of the lower effective temperature difference between TOP and bRGB stars, the gravity difference also turns out to be lower than that derived by G01. At 0.1 dex, the difference is, however, not significant.

In addition to the reanalyses of G01 stars, we also analyze one of the TOP stars observed by Thévenin et al. (2001). This star (A2084) has the same  $V$  magnitude as NGC 6397–12318. Based on the UVES pipeline output (kindly made available by F. Thévenin), we confirm the stellar parameters and iron abundance derived by Thévenin et al. (2001) to within  $1 \sigma$  measurement uncertainties:

<sup>5</sup> Local subdwarfs were observed in the same observing program and used as a point of reference for  $T_{eff}$ . However, none of these have an effective temperature above 6100 K. As the problems with blaze residuals and order merging worsen toward hotter effective temperatures (broader Balmer line profiles), this poor coverage in  $T_{eff}$  may have caused the systematic effects on the TOP star effective temperatures to go undetected.

$T_{eff} = 6250 \pm 200$  K,  $\log g = 4.0 \pm 0.2$ ,  $[Fe/H] = -2.27 \pm 0.1$ ,  $\xi = 1.7 \pm 0.2$  km s<sup>-1</sup>. This indicates once more that our TOP star effective temperatures are essentially correct.

#### 3.5. Chemical Abundances

It may seem that one has a great variety of elements to choose from when investigating atomic diffusion predictions like those shown in Figure 1. However, various groups of elements are not suited for testing such predictions by comparing their abundances in unevolved and evolved globular cluster stars. Helium is unobservable in these cool stars. Lithium can be observed in TOP stars but is significantly processed in RGB stars. Beryllium and boron require near-UV spectroscopy and suffer from the same type of processing as lithium. Carbon and nitrogen in RGB stars may rather reflect the contamination of the atmosphere with material processed in the stellar core. Oxygen, sodium, magnesium, and aluminum suffer from the anticorrelations discussed in § 1. We are then left with elements like silicon, sulfur, calcium, titanium, and iron group elements (no predictions currently exist for elements heavier than nickel).

According to Figure 1, a clear signature of atomic diffusion and mixing would be steep trends [ $\Delta \log \varepsilon(X) = \log \varepsilon(X)_{RGB} - \log \varepsilon(X)_{TOP} = 0.2$ ] in silicon, rather flat trends [ $\Delta \log \varepsilon(X) = 0.1$ ] in calcium and titanium and intermediate trends [ $\Delta \log \varepsilon(X) = 0.15$ ] in iron group elements.

Once the stellar parameters, and in particular stellar parameter differences, are determined, it is a straightforward task to derive abundances, and potential abundance differences, for various elements. As abundance differences are a differential indicator, the exact choice of atomic data for a given line is not critical. This is why we do not tabulate the line data in detail (the lines used are specified in Appendix A). However, even differential indicators may be affected by departures from LTE, as excitation, ionization, and collisions are inherently different in dwarf and giant stars. We therefore made an effort to model as many elements as possible using NLTE line formation: Mg I is modeled following Gehren et al. (2004), Ca I following Mashonkina et al. (2007), Fe I following Korn et al. (2003), and Ba II following Mashonkina et al. (1999). Lines arising from transition in Ti II and Fe II are believed to be formed under near-LTE conditions; these species constitute the dominant ionization stages of the respective element. The case of Li I is discussed in § 5.2.

TABLE 4  
MEAN STELLAR PARAMETERS AND ELEMENTAL ABUNDANCES OF THE 18 STARS OBSERVED WITH FLAMES-UVES

Group	$T_{\text{eff}}$ (K)	$\log g$	[Fe/H]		$\log \varepsilon(\text{Li})^{\text{a}}$		$\log \varepsilon(\text{Mg})^{\text{b}}$		$\log \varepsilon(\text{Ca})^{\text{c}}$		$\log \varepsilon(\text{Ti})^{\text{d}}$		$\log \varepsilon(\text{Ba})^{\text{e}}$	
			NLTE	LTE	LTE	NLTE	NLTE	LTE	LTE	NLTE	LTE	NLTE		
TOP <sub>ave</sub> .....	6254	3.89 <sup>f</sup>	-2.28	2.24	5.64	4.52	2.99	-0.12						
SGB <sub>ave</sub> .....	5805	3.58 <sup>f</sup>	-2.24	2.36	5.71	4.52	2.91	-0.10						
bRGB <sub>ave</sub> .....	5456	3.37	-2.18	1.38	5.72	4.54	3.01	-0.08						
RGB <sub>ave</sub> .....	5130	2.56	-2.12	0.98	5.85	4.59	3.05	-0.12						

<sup>a</sup> Based on Li I  $\lambda 6707$  (see Appendix A).

<sup>b</sup> Based on Mg I  $\lambda 5528$  (see Appendix A).

<sup>c</sup> Based on Ca I  $\lambda \lambda 6122, 6162, \text{ and } 6439$  (see Appendix A).

<sup>d</sup> Based on Ti II  $\lambda \lambda 5188 \text{ and } 5226$  (see Appendix A).

<sup>e</sup> Based on Ba II  $\lambda 6496$  (see Appendix A).

<sup>f</sup> Not corrected for helium diffusion (see § 5.1).

After co-adding the spectra within each group of stars, lines as weak as 20 mÅ could easily be measured in the TOP stars. Such lines (depending on the line-specific atomic data) have line strengths of 60–70 mÅ in the RGB stars. The analysis is then insensitive to  $\xi_{\text{TOP}}$  but has some sensitivity to  $\xi_{\text{RGB}}$ . In Table 5, the sensitivity of a few representative lines to variations in stellar parameters (including microturbulence) is given.

We find systematic trends of abundance with evolutionary phase for iron and magnesium. Propagating the standard deviation of all iron lines into the mean iron abundance of each group of stars, the abundance difference  $\Delta \log \varepsilon(\text{Fe}) = 0.16 \pm 0.05$  is significant at the 3  $\sigma$  level. Likewise, assuming an uncertainty of 0.05 dex on the magnesium abundance determined from the weak Mg I  $\lambda 5528$  line, the *relative* abundance trend  $\Delta \log \varepsilon(\text{Mg}) = 0.21 \pm 0.07$  is also significant at the 3  $\sigma$  level. As shown in Table 4, calcium, titanium, and barium show shallower trends of weak statistical significance.

#### 4. COMPARISON WITH DIFFUSION MODELS

The atomic diffusion models were computed as described in Richard et al. (2005) and references therein for the metallicity of NGC 6397. The abundances of  $\alpha$ -elements were increased by 0.3 dex compared to the solar mixture. These models take into account atomic diffusion (gravitational settling, radiative acceleration, thermal diffusion, diffusion due to concentration gradients) in a self-consistent way. The detailed treatment of atomic diffusion is described in Turcotte et al. (1998), and the radiative accelerations are from Turcotte et al. (1998), with corrections for redistribution from Gonzalez et al. (1995) and LeBlanc et al. (2000). The Rosseland opacity and radiative accelerations are computed at each time step in each layer for the exact local chemical composition using OPAL monochromatic opacities for 24 elements. Convection and semiconvection are modeled as diffusive processes as described in Richer et al. (2000) and Richard et al. (2001).

The main free parameter in these calculations is the efficiency of (turbulent) mixing below the outer convection zone. As discussed in Richard et al. (2005), this extra ingredient is needed to meet the constraints imposed by the observations of  ${}^7\text{Li}$  in warm halo stars: a thin and flat plateau can only be retained in the presence of diffusion, if extra mixing is introduced into the models.

As no parameter-free physical description of turbulent mixing is available, it is introduced into the stellar evolution models in an ad hoc manner. The turbulent diffusion coefficient,  $D_T$ , is linked to the atomic diffusion coefficient of He at a reference

temperature  $T_0$  and is chosen to vary with density  $\rho$  to the inverse third power:

$$D_T = 400 D_{\text{He}}(T_0) \left[ \frac{\rho}{\rho(T_0)} \right]^{-3}.$$

There are two tunable parameters in this formula, the proportionality constant and the exponent. A steep  $\rho$  dependence, i.e., localizing this mixing to a narrow region below the outer convection zone, is suggested by the solar beryllium abundance, which is believed to be essentially unaltered since the formation of the solar system (Proffitt & Michaud 1991). We thus keep this parameter fixed to  $-3$ . The assumed overall strength of turbulent mixing can be changed by modifying the proportionality constant or the reference temperature  $T_0$ . Following Richard et al. (2005), the proportionality constant is kept fixed, and we vary the reference temperature between  $\log T = 5.8$  and 6.09. This is the range of least efficient turbulent mixing that is compatible with the constraints of observed lithium abundances in warm halo stars.

In Figure 6 the observed abundance trends are compared with predictions from stellar evolution models. We find the T6.0 model to match our observations best. Higher efficiency mixing produces shallower trends for most elements. However, calcium and titanium can be levitated by radiative forces, and additional mixing suppresses this tendency, making trends mildly steeper. The element-specific trends observed and their agreement with the atomic diffusion model suggest a causal connection between the abundance trends and effects due to atomic diffusion moderated by mixing below the convective envelope. We have empirically determined the amount of mixing that is required to reproduce the observed trends.

#### 4.1. Error Analyses

Here we address the question of whether the observed abundance trends are caused by contrived sets of stellar parameters or fundamental assumptions made in the modeling of stellar atmospheres, i.e., the hydrostatic approximation with convection according to mixing-length theory.

##### 4.1.1. Stellar Parameters

Given that G01 found no abundance differences in iron between their TOP and bRGB stars, we can ask ourselves whether all abundance trends vanish if we assume TOP effective temperatures  $\approx 250$  K hotter. As can be seen from Table 5, this is not the case. An extreme example is the trend derived from Mg I  $\lambda 5528$ , which would require well above 400 K hotter TOP stars (or 300 K

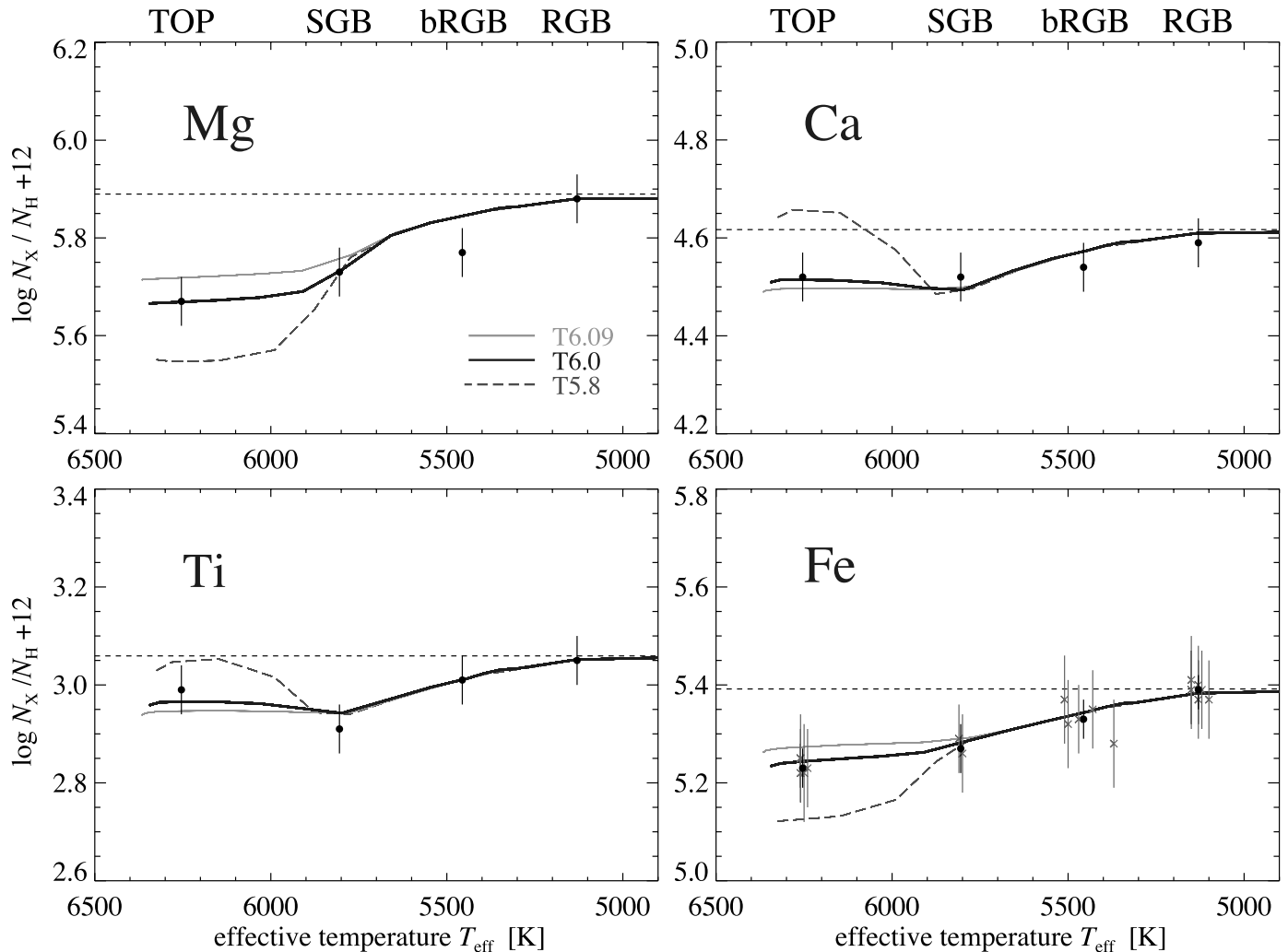


FIG. 6.—Observed trends of elemental abundances with evolutionary stage (*filled circles with error bars*) compared to predictions from stellar evolution models including atomic diffusion and turbulent mixing with three different efficiencies. Note how the T5.8 model falls below or above the best-fitting T6.0 model depending on the element (likewise the T6.09 model). For details, see text. [See the electronic edition of the *Journal* for a color version of this figure.]

cooler RGB stars) to completely remove the abundance trend. Even larger  $T_{\text{eff}}$  corrections would be required, if one were to consider the feedback from  $\log g$ . Given that  $\Delta T_{\text{eff}}$  is around 1100 K, such corrections are of the order of 30%. We regard it as unlikely that we underestimate  $\Delta T_{\text{eff}}$  by as much as one-third.

Along the same lines, the diffusion signature in lithium between the TOP and SGB stars of 0.12 dex would require 170 K hotter TOP stars or 150 K cooler SGB stars. The effective temperature difference between these two groups of stars is no larger than 450 K; thus, a correction of more than 30% would also be required here.

When it comes to  $\log g$ -sensitive species like Fe II, surface gravity corrections of  $\geq 0.4$  dex are required to harmonize TOP and RGB iron abundances ( $\Delta \log g$  would then be larger than 1.7). Given that  $\Delta \log g_{\text{phot}}$  is robustly determined from  $\Delta V$ , a  $\Delta \log g$  larger than 1.5 can practically be ruled out.

In the absence of spectroscopic or photometric evidence for either hotter TOP star or cooler RGB star effective temperatures, it seems rather unlikely that these trends are produced by biased stellar parameters. Increasing TOP star effective temperatures by 100 K to remove the abundance trends, as claimed by Bonifacio et al. (2007), is not possible. It is one of the strengths of this analysis that it combines independent techniques to derive stellar parameters that turn out to agree rather well.

#### 4.1.2. Model Atmospheres

##### 4.1.2.1. Effects of the First Dredge-up

The giant stars of NGC 6397 are expected to be affected by the first dredge-up of CN processed material, and more so the higher up the stars are along the giant branch. Along the lower giant branch the Population II stars are predicted to be only marginally affected, corresponding to a decrease of  $[C/Fe]$  by about 0.15 dex or less (Charbonnel 1994; Vandenberg & Smith 1988), which has also been verified by Gratton et al. (2000) for Population II field stars, and a corresponding increase of  $[N/Fe]$ , keeping the absolute number of C+N nuclei constant. A much more severe decrease of  $[C/Fe]$  matched by an  $[N/Fe]$  increase is found by Gratton et al. (2000) for field stars that have evolved off the bump in the RGB luminosity function around  $\log L = 1.8 L_{\odot}$ , where a reduction by a factor of 2.5 in the carbon abundance is common. For cluster giants, even deeper mixing may occur, which may contribute to the O depletion/Na enhancement observed (Kraft 1994). A question is now whether such phenomena that vary systematically from the TOP up along the RGB may cause differential effects on the stellar atmospheres that could affect the measures of abundance differences between our different stellar groups.

Experiments with varying the CNO abundances in a set of MARCS models show that the differential effects in the model

TABLE 5  
INFLUENCE OF STELLAR PARAMETERS ON ABUNDANCES FOR A FEW REPRESENTATIVE LINES

Variation	Li I $\lambda 6707$	Mg I $\lambda 5528$	Ca I $\lambda 6122$	Ti II $\lambda 5226$	Fe II $\lambda 5018$	Fe II $\lambda 5234$	Fe I $\lambda 6494$
TOP							
$T_{\text{eff}} + 100 \text{ K}$ .....	0.070	0.047	0.064	0.035	0.022	0.011	0.078
$\log g + 0.3 \text{ dex}$ .....	-0.002	-0.011	-0.006	0.100	0.091	0.105	-0.003
$\xi + 0.3 \text{ km s}^{-1}$ .....	-0.003	-0.010	-0.009	-0.005	-0.089	-0.005	-0.010
$T_{\text{eff}} + 200 \text{ K}$ .....	0.139	0.089	0.122	0.069	0.042	0.023	0.154
$\log g + 0.6 \text{ dex}$ .....	-0.003	-0.024	-0.017	0.200	0.174	0.210	-0.004
$\xi + 0.6 \text{ km s}^{-1}$ .....	-0.004	-0.021	-0.020	-0.022	-0.158	-0.002	-0.019
$T_{\text{eff}} - 100 \text{ K}$ .....	-0.072	-0.041	-0.055	-0.036	-0.023	-0.011	-0.080
$\log g - 0.3 \text{ km s}^{-1}$ .....	0.003	0.016	0.014	-0.100	-0.096	-0.104	0.003
$\xi - 0.3 \text{ km s}^{-1}$ .....	-0.003	0.017	0.020	0.010	0.113	0.010	0.019
$T_{\text{eff}} - 200 \text{ K}$ .....	-0.151	-0.087	-0.117	-0.073	-0.047	-0.023	-0.162
$\log g - 0.6 \text{ dex}$ .....	0.008	0.025	0.022	-0.200	-0.197	-0.207	0.007
$\xi - 0.6 \text{ km s}^{-1}$ .....	-0.003	0.030	0.036	0.027	0.249	0.020	0.024
SGB							
$T_{\text{eff}} + 100 \text{ K}$ .....	0.079	0.055	0.075	0.040	0.030	0.013	0.091
$\log g + 0.3 \text{ dex}$ .....	-0.000	-0.027	-0.019	0.099	0.069	0.104	-0.008
$\xi + 0.3 \text{ km s}^{-1}$ .....	-0.010	-0.017	-0.019	-0.017	-0.128	-0.010	-0.028
$T_{\text{eff}} + 200 \text{ K}$ .....	0.155	0.107	0.142	0.078	0.059	0.025	0.178
$\log g + 0.6 \text{ dex}$ .....	-0.000	-0.056	-0.045	0.197	0.128	0.206	-0.018
$\xi + 0.6 \text{ km s}^{-1}$ .....	-0.020	-0.033	-0.040	-0.032	-0.231	-0.013	-0.051
$T_{\text{eff}} - 100 \text{ K}$ .....	-0.081	-0.052	-0.067	-0.041	-0.033	-0.013	-0.094
$\log g - 0.3 \text{ km s}^{-1}$ .....	0.001	0.029	0.025	-0.099	-0.079	-0.103	0.006
$\xi - 0.3 \text{ km s}^{-1}$ .....	0.009	0.021	0.032	0.021	0.148	0.016	0.034
$T_{\text{eff}} - 200 \text{ K}$ .....	-0.165	-0.110	-0.141	-0.083	-0.067	-0.026	-0.191
$\log g - 0.6 \text{ dex}$ .....	0.003	0.050	0.040	-0.198	-0.166	-0.206	0.011
$\xi - 0.6 \text{ km s}^{-1}$ .....	0.017	0.040	0.060	0.047	0.301	0.034	0.078
bRGB							
$T_{\text{eff}} + 100 \text{ K}$ .....	0.088	0.064	0.092	0.046	0.036	0.016	0.111
$\log g + 0.3 \text{ dex}$ .....	-0.002	-0.053	-0.042	0.094	0.051	0.105	-0.029
$\xi + 0.3 \text{ km s}^{-1}$ .....	-0.003	-0.027	-0.031	-0.035	-0.137	-0.013	-0.063
$T_{\text{eff}} + 200 \text{ K}$ .....	0.172	0.129	0.176	0.105	0.075	0.030	0.218
$\log g + 0.6 \text{ dex}$ .....	-0.003	-0.099	-0.092	0.187	0.092	0.198	-0.065
$\xi + 0.6 \text{ km s}^{-1}$ .....	-0.005	-0.051	-0.064	-0.063	-0.251	-0.029	-0.114
$T_{\text{eff}} - 100 \text{ K}$ .....	-0.091	-0.073	-0.083	-0.048	-0.040	-0.012	-0.116
$\log g - 0.3 \text{ km s}^{-1}$ .....	0.003	0.046	0.050	-0.096	-0.067	-0.099	0.023
$\xi - 0.3 \text{ km s}^{-1}$ .....	0.002	0.021	0.048	0.043	0.150	0.027	0.079
$T_{\text{eff}} - 200 \text{ K}$ .....	-0.187	-0.144	-0.176	-0.096	-0.081	-0.023	-0.236
$\log g - 0.6 \text{ dex}$ .....	0.006	0.087	0.089	-0.193	-0.134	-0.200	0.039
$\xi - 0.6 \text{ km s}^{-1}$ .....	0.004	0.044	0.091	0.097	0.292	0.056	0.174
RGB							
$T_{\text{eff}} + 100 \text{ K}$ .....	0.099	0.070	0.104	0.051	0.040	0.018	0.127
$\log g + 0.3 \text{ dex}$ .....	-0.007	-0.074	-0.066	0.087	0.041	0.098	-0.044
$\xi + 0.3 \text{ km s}^{-1}$ .....	-0.002	-0.054	-0.073	-0.095	-0.178	-0.039	-0.123
$T_{\text{eff}} + 200 \text{ K}$ .....	0.193	0.144	0.202	0.101	0.079	0.033	0.248
$\log g + 0.6 \text{ dex}$ .....	-0.014	-0.143	-0.142	0.170	0.074	0.185	-0.099
$\xi + 0.6 \text{ km s}^{-1}$ .....	-0.003	-0.098	-0.140	-0.166	-0.342	-0.073	-0.221
$T_{\text{eff}} - 100 \text{ K}$ .....	-0.103	-0.087	-0.102	-0.051	-0.041	-0.008	-0.134
$\log g - 0.3 \text{ km s}^{-1}$ .....	0.008	0.054	0.065	-0.091	-0.051	-0.092	0.036
$\xi - 0.3 \text{ km s}^{-1}$ .....	0.002	0.039	0.085	0.126	0.172	0.060	0.149
$T_{\text{eff}} - 200 \text{ K}$ .....	-0.212	-0.167	-0.212	-0.099	-0.079	-0.016	-0.275
$\log g - 0.6 \text{ dex}$ .....	0.018	0.105	0.117	-0.179	-0.111	-0.190	0.064
$\xi - 0.6 \text{ km s}^{-1}$ .....	0.004	0.082	0.164	0.277	0.313	0.129	0.311

NOTE.—These are computed using MARCS by matching group-averaged equivalent widths.

TABLE 6  
3D – 1D LTE CORRECTIONS TO Mg, Ti, AND Fe ABUNDANCES  
FOR THE METAL-POOR RGB AND TOP STAR

LINE	log $gf$	$E_{\text{low}}$ (eV)	log $\varepsilon_{3D} - \log \varepsilon_{1D}$	
			RGB	TOP
Mg I $\lambda 5528$ .....	-0.620	4.346	-0.09	+0.03
Ti II $\lambda 5226$ .....	-1.230	1.566	+0.06	+0.01
Fe I $\lambda 4920$ .....	0.068	2.832	-0.08	-0.01
Fe I $\lambda 5328$ .....	-1.466	0.915	-0.29	-0.45
Fe I $\lambda 5424$ .....	0.580	4.320	-0.02	+0.04
Fe II $\lambda 4923$ .....	-1.260	2.891	+0.23	+0.34
Fe II $\lambda 5234$ .....	-2.230	3.221	+0.16	+0.08
Fe II $\lambda 5316$ .....	-1.850	3.153	+0.26	+0.13

NOTE.—Stellar parameters for the models are  $T_{\text{eff}} = 5035$  K,  $\log g = 2.20$ ,  $[\text{Fe}/\text{H}] = -2.0$ ,  $\xi = 1.6$  km s $^{-1}$  (RGB) and  $T_{\text{eff}} = 6180$  K,  $\log g = 4.04$ ,  $[\text{Fe}/\text{H}] = -2.0$ ,  $\xi = 2.0$  (TOP).

structures by such changes are only marginal, leading to maximum changes in the temperature gradient of  $\delta T/\delta \tau(\text{Ross})$  of less than 10 K. Moreover, the gradient is diminished, causing weaker, sooner than stronger, metal lines for the giants than in the case of unmodified abundances. Thus, we conclude that the observed trends of Figure 6 cannot be explained by such dredge-up effects.

#### 4.1.2.2. Three-dimensional Corrections

Recent stellar surface convection simulations indicate that the structural differences between three-dimensional (3D) hydrodynamic and one-dimensional (1D) hydrostatic model atmospheres may have a significant effect on the predicted strength of spectral lines and hence on the derived spectroscopic abundances in metal-poor stars (Asplund et al. 1999; Asplund & García Pérez 2001; Collet et al. 2006). We use here the surface convection simulations of a red giant (Collet et al. 2007) and of a turnoff star (Asplund & García Pérez 2001) at a metallicity of  $[\text{Fe}/\text{H}] = -2$  as time-dependent 3D hydrodynamic model atmospheres to calculate Mg, Ti, and Fe spectral lines and estimate the impact of 3D models on the determination of abundance trends for these elements with respect to stellar evolutionary stage. Corresponding calculations were not made for Ca, since LTE was found to be inappropriate (see Appendix A). The relevant stellar parameters of the 3D model atmospheres considered here are given in the caption of Table 6.

From the full RGB and TOP star simulations, we select two representative sequences, 10,000 and 60 minutes long, respectively, of about 40 snapshots taken at regular intervals in time. We then compute spectral line profiles for a number of Mg, Ti, and Fe lines (see Table 6) under the assumption of LTE. For each line, we solve the radiative transfer equation along 17 directions (four  $\mu$ -angles, four  $\phi$ -angles, plus the vertical), after which we perform a disk integration and a time average over all snapshots.

Using the 3D models, we derive the abundances of Mg, Ti, and Fe from the measured equivalent widths of individual lines of these elements. We then carry out a differential comparison with the results of the abundance analysis based on classical 1D LTE plane-parallel hydrostatic MARCS model atmospheres constructed with the same stellar parameters and chemical compositions as the hydrodynamic simulations. We caution that this 3D – 1D analysis is restricted in two ways. First, the analysis is based on equivalent widths, and an analysis based on line profiles may return somewhat different results. Second, microturbulence enters on the 1D side of the analysis, making the results dependent on microturbulence

when strong lines (Fe I  $\lambda 4920$ , Fe I  $\lambda 5328$ , and Fe II  $\lambda 4923$ ) are investigated.

The results of the 3D – 1D differential Mg, Ti, and Fe abundance analysis for the RGB and TOP cases are shown in Table 6. No clear picture emerges:  $\Delta \log \varepsilon(\text{Mg})$  becomes smaller,  $\Delta \log \varepsilon(\text{Ti})$  becomes steeper, while weak and strong Fe I and Fe II lines show corrections modifying  $\Delta \log \varepsilon(\text{Fe})$  between +0.11 and -0.16. The average  $\Delta \log \varepsilon(\text{Fe})_{3D}$  is 0.02 dex steeper than its 1D counterpart. Judging from the most reliable weak Fe II lines, a steeper abundance trend in iron seems possible (by about 0.1 dex). However, this does not fit to the 3D trends in Mg and Ti, which become flatter and steeper, respectively (see the T6.09 model in Fig. 6). The most important conclusion is that the abundance trends as such are probably not an artifact of the modeling in 1D.

That 1D flux-constant models are not fully adequate for the detailed analysis of metal-poor stars has been realized for some time. One could ask whether inaccuracies in the models could mimic the observed abundance trends. By experimenting with ad hoc steepenings of the temperature gradients in MARCS models, we have found that a lowering of the temperature by typically 400 K in the outer atmosphere for the giants, keeping the temperature in the continuum-forming layers fixed and applying no corresponding steepening for the TOP stars, would remove abundance trends similar to those shown in Figure 6 (see also Gustafsson 1983). (We note in passing that the Fe I/II balance would be affected by such a steepening since the effects are smaller for Fe II lines. The consistency of our ionization balance with the log  $g$  values derived from the luminosities thus suggests that the trends in Figure 6 are not due to such a steepening. This is, however, an uncertain argument, as it is dependent on the correctness of the NLTE calculations for iron.) The steepening of the temperature gradient needed is considerable, more than twice the total line-blanketing effect on the temperature gradient of the MARCS models. It may, however, not be totally excluded. The upper temperature in real stars is set by the balance between the adiabatic cooling of the up-streaming gas and the heating by radiation from below, and the purely adiabatic temperature gradient is below the steepened MARCS model. The radiative heating may be overestimated in 1D models, and also in present-day 3D ones, if the thermal coupling to the gas is lower than our LTE models predict. This could be the case if scattering processes dominate.

Future analysis in 3D, with a more detailed treatment of the radiative field, based on line profiles and preferably with stellar parameters derived in a self-consistent way, may change details. However, the general results of the present study will likely remain.

#### 4.1.3. NLTE Effects

While we made an effort to treat the line formation of the investigated elements as detailed as possible, there are uncertainties in present-day statistical equilibrium calculations. These mainly arise from poorly known cross sections for inelastic collisions with neutral hydrogen. All NLTE studies listed in § 3.5 take an empirical approach in calibrating the efficiency of such collisions on stars with known stellar parameters, i.e., local subdwarfs with accurate *Hipparcos* parallaxes. In all cases, it is found that the neglect of hydrogen collisions leads to NLTE effects that are too large (judged on line-to-line scatter or equilibria of two ionization stages, where available). Larger NLTE effects are possible to obtain (and could alter the observed abundance trends, if they introduce differential effects), but this would be in conflict with the empirical findings. It should be noted that the NLTE approach flattens abundance trends for two elements, calcium and barium (see Appendix A). We thus regard it as unlikely that modeling

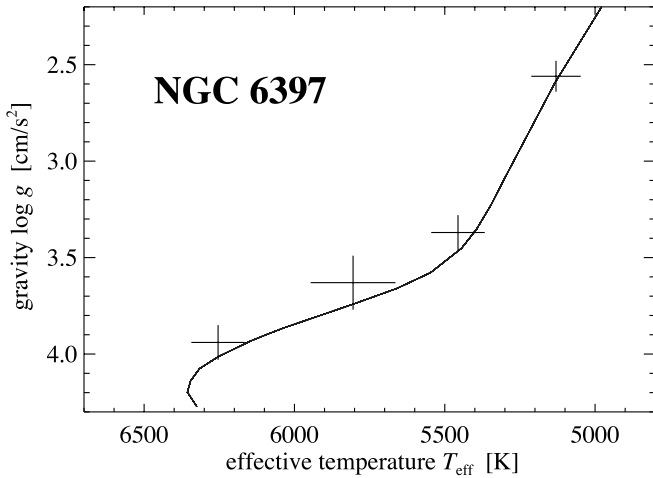


FIG. 7.—Stellar parameters compared to a 13.5 Gyr isochrone constructed from the T6.0 diffusion model. Helium diffusion corrections to  $\log g$  have been applied to the TOP and SGB stars (+0.05 dex in both cases). The TOP stars have effective temperatures about 100 K lower than the turnoff point, in line with expectations from photometry. The cluster may be somewhat younger than 13.5 Gyr, which, however, has only a small effect on our comparison between observed abundance trends and atomic diffusion predictions. [See the electronic edition of the *Journal for a color version of this figure.*]

deficits in the current NLTE treatment conspire to produce the element-specific trends seen in Figure 6.

## 5. DISCUSSION

In the following, consequences of the atomic diffusion interpretation of the observed abundance trends are discussed.

### 5.1. Helium

The uncovered abundance trends also have structural effects on the atmosphere that one needs to consider. Due to its high abundance, the downward diffusion of helium (by about 0.25 dex in the T6.0 model) is accompanied by a corresponding change in mean molecular weight. According to Strömberg et al. (1982), this effect can be mapped as a shift in surface gravity. That is, the line spectrum of a helium-normal atmosphere corresponds to the line spectrum of a helium-poor atmosphere at somewhat higher  $\log g$ . This increases the  $\log g$  values for the TOP and SGB stars by +0.05 dex, while the original helium abundance is practically recovered for the bRGB stars and, even more so, RGB stars. This improves the agreement between the spectroscopic and photometric  $\Delta \log g$  values even further.

The empirical turbulent mixing calibration constrains the amount of atmospheric helium diffusion. This has, however, little effect on globular cluster ages, as the central helium diffusion is unaffected by the amount of turbulent mixing acting just below the convective envelope. We emphasize, however, that the new TOP stellar parameters do not contradict the cosmological age constraint. In other words, in spite of effective temperatures 230 K cooler than what was derived by G01, NGC 6397 is younger than 13.5 Gyr (see Fig. 7).

### 5.2. Lithium

Lithium shows abundance trends quite different from any of the other elements discussed above. This is because one sees its surface abundance become diluted as the stars evolve to become red giants. The dilution seems to set in just below the SGB star group, that is, below 5800 K (see Fig. 8). The dilution that the

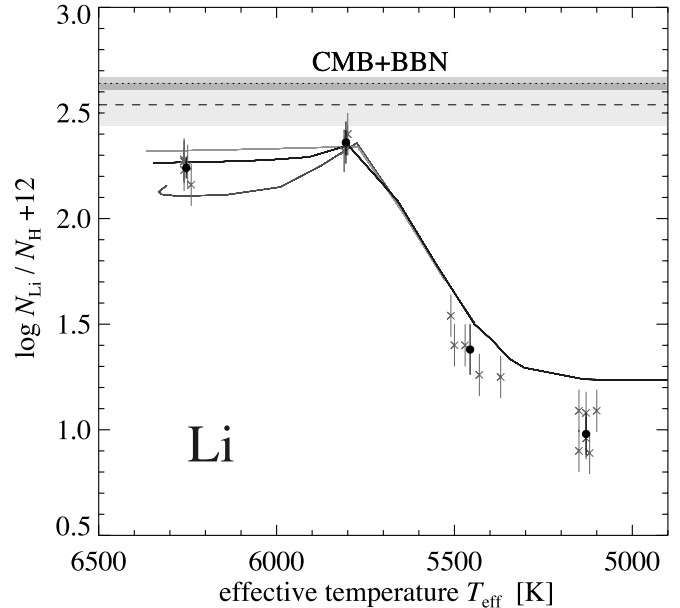


FIG. 8.—Observed trends of lithium. Crosses indicate individual stellar abundances, while filled circles show group averages. Solid lines represent the atomic diffusion model predictions (see Fig. 6), which have an original abundance as given by the dashed line [ $\log \epsilon(\text{Li}) = 2.54 \pm 0.1$ ]. The dark shaded area shows the predicted primordial lithium abundance [“CMB+BBN:”  $\log \epsilon(\text{Li}) = 2.64 \pm 0.03$ ; Spergel et al. 2007]. [See the electronic edition of the *Journal for a color version of this figure.*]

models predict falls successively short of the observed abundances for the bRGB and RGB stars. For the latter group, the discrepancy exceeds 0.2 dex and is usually ascribed to a source of extra mixing not considered in these calculations (Charbonnel 1995).

We find lithium abundances in the TOP stars of  $\log \epsilon(\text{Li}) = 2.24 \pm 0.05$ . Bonifacio et al. (2002) derive lithium abundances for 12 TOP stars in NGC 6397 drawn from the studies of G01 and Thévenin et al. (2001). They derive a mean abundance of  $\log \epsilon(\text{Li}) = 2.34 \pm 0.056$ , 0.1 dex above our TOP star lithium abundances. For the three stars in common with this study (see Table 2), they assign effective temperatures 145 K hotter on average. This  $T_{\text{eff}}$  difference fully explains the offset in lithium abundances.

Comparing the average lithium abundances in the TOP and SGB groups, we detect an abundance difference of 0.12 dex. The stellar structure models with atomic diffusion also predict higher abundances in the SGB stars. We have thus identified a diffusion signature on the Spite plateau of lithium (Spite & Spite 1982) that has so far only been identified in a statistical sense (Charbonnel & Primas 2005) in comparing lithium abundances in field dwarf and subgiant stars. With hindsight, this signature may possibly be traced in the lithium abundances of three TOP stars in NGC 6397 (with  $T_{\text{eff}}$  values between 6000 and 6180 K) analyzed by Pasquini & Molaro (1996).

We note that the T5.8 model has turbulent mixing that is too weak to keep the Spite plateau flat in the turnoff region around  $T_{\text{eff}} = 6300$  K. This is indicated in Figure 8 by the hook at the hot end of the T5.8 model. It thus seems that our observations constrain turbulent mixing to a strength that is just sufficient to keep the Spite plateau flat on the main sequence and around the turnoff region.

The atomic diffusion model predicts the abundance of lithium these NGC 6397 stars had when they formed. This value,  $\log \epsilon(\text{Li}) = 2.54 \pm 0.1$ , compares well with the *WMAP*-based

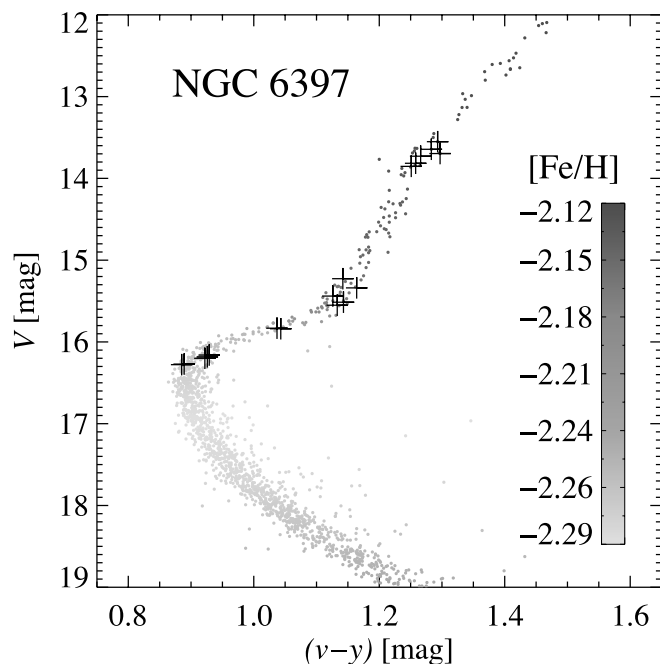


FIG. 9.—CMD of NGC 6397 with gray scale according to the atomic diffusion model with turbulent mixing as calibrated on the observed stars (*plus signs*). [See the electronic edition of the *Journal* for a color version of this figure.]

predictions of standard big bang nucleosynthesis,  $\log \varepsilon(\text{Li}) = 2.64 \pm 0.03$  (Spergel et al. 2007). It thus seems that atomic diffusion is predominantly responsible for photospheric lithium abundances of stars on the Spite plateau being systematically below the primordial value.

In comparing with the primordial lithium abundance, no correction for galacticochemical production of lithium (by cosmic-ray spallation) is considered. Empirical trends of lithium abundance with metallicity vary from author to author: some find trends as steep as  $\approx 0.1$  dex per 1 dex in  $[\text{Fe}/\text{H}]$  (Ryan et al. 1999; Asplund et al. 2006), while others find no trend at all (Meléndez & Ramírez 2004; Shi et al. 2007). The different behavior is primarily caused by differences in the adopted effective temperature scale. Accounting for an extra 0.1 dex lessens the agreement between diffusion-corrected stellar abundances and the primordial value. A gap of 0.1–0.2 dex can, however, be explained, e.g., by mixing through Population III stars (see Piau et al. 2006; but for some criticism of this scenario see also Prantzos 2006).

### 5.3. Abundance Ratios

Atmospheric abundances of unevolved, metal-poor stars seem systematically affected by atomic diffusion. This is particularly true for ratios with respect to hydrogen where diffusion corrections can reach 0.2–0.3 dex for widely used elements like Mg or Fe (see Fig. 9). Abundance ratios of metals (e.g., Mg/Fe) may only be affected by 0.05 dex. Nonetheless, for the highest accuracy the predictions from atomic diffusion models have to be included.

For the time being, we have no understanding of the metallicity dependence of turbulent mixing. It could be that extremely metal-poor stars (like HE 1327–2326; Frebel et al. 2005) are therefore more (or less) affected by atomic diffusion. We are in the process of investigating this issue. It is highly desirable to understand the physical processes that give rise to mixing below the convection zone. Encouraging results based on hydrodynamic models have already been presented by Charbonnel & Talon (2005).

### 5.4. Stellar Isochrone Ages

In deriving stellar ages with the help of isochrones, two fundamentally different situations need to be discussed. On the one hand, there are populations of stars (like globular clusters); on the other hand, there are individual field stars. The impact of atomic diffusion on age determinations differs in these two cases, as detailed below.

Globular cluster ages are unlikely to be affected by our findings, for two reasons: First, their metallicities are usually derived from red giant stars that show in their atmospheres the composition of the gas they formed from (with some notable exceptions). Second, helium diffusion has been considered in deriving globular cluster isochrone ages for quite some time (Chaboyer et al. 1998).

Ages for unevolved halo field stars will be modified by atomic diffusion. One needs to consider the interplay of metal diffusion (i.e., comparing to the correct isochrone) and helium diffusion (i.e., shifting the surface gravity upward). Main-sequence and TOP stars will likely get lower ages, while subgiants may become somewhat older. We postpone a quantitative discussion of these effects to a forthcoming paper.

### 5.5. Abundance Gradients in the Halo

Large, magnitude-limited surveys like the Sloan Digital Sky Survey (SDSS) provide us with a wealth of information on the chemical composition of the Galactic halo. If one performs analyses of dwarfs and giants in a certain apparent magnitude range, one inevitably samples different space volumes, more nearby ones with the dwarfs, more distant ones with the giants. Large samples of stars can then define metallicity distribution functions (MDFs), and one may want to look for gradients with galactocentric distance or height above the Galactic plane. Assume that one finds that the MDFs of distant giants and more nearby dwarfs peak at the same metallicity. Does this mean that there are no abundance gradients in that direction? In the light of atomic diffusion affecting dwarf star abundances only, this apparent null result actually means that the more distant population of stars is 0.1–0.2 dex more metal-poor.

### 5.6. Other Metallicities

We recently computed models similar to those used here for  $[\text{Fe}/\text{H}] = -1.5$ , the metallicity of NGC 6752. The predictions indicate abundance trends practically as large as in NGC 6397 (if turbulent mixing is assumed to be equally efficient). We will study NGC 6752 with FLAMES-UVES and GIRAFFE-MEDUSA to quantify potential effects of atomic diffusion and mixing at this metallicity.

Cohen & Meléndez (2005) studied M13 at  $[\text{Fe}/\text{H}] \approx -1.5$  but found no abundance trends. However, their work only included three unevolved (subgiant) stars. This study may thus not sample the region where atomic diffusion acts in sufficient detail. Nonetheless, the three least evolved stars show a mean iron abundance 0.15 dex below the average of the other 22 (giant) stars.

Better sampling of the turnoff region was achieved by Ramírez & Cohen (2003) for M5 at  $[\text{Fe}/\text{H}] \approx -1.3$  (six TOP stars). To within the abundance uncertainties (claimed to be 0.1 dex), they find no trends for a variety of elements. Concerns about the data quality could be raised, as the TOP stars have S/Ns of 40–50 *per 4 pixel resolution element*. However, there is currently no satisfactory explanation for the absence of abundance trends in M5, unless one proposes that turbulent mixing is markedly more efficient than the strength found in NGC 6397.

At even higher metallicities, effects are expected to diminish, as the convection zones of more metal-rich stars are more massive than those of metal-poor ones.

## 6. CONCLUSIONS

We have identified significant abundance trends for the elements lithium, magnesium, and iron between groups of stars from the turnoff point to the bump on the RGB. Other elements studied (calcium, titanium, and barium) show shallower trends of weak statistical significance in NGC 6397. For lithium, the global trend can be explained by dilution of the atmospheric layers with lithium-free material as the convective envelope expands inward. For the other elements, we show that atomic diffusion (the net effect from gravitational settling and radiative levitation) and turbulent mixing below the convective envelope can describe the trends in an element-specific way. A diffusion signature is also identified for lithium in stars on the Spite plateau, and their original lithium abundance is inferred to be  $\log \epsilon(\text{Li}) = 2.54 \pm 0.1$ , in good agreement with *WMAP*-based predictions of big bang nucleosynthesis (Spergel et al. 2007).

Our study has consequences for the use of unevolved metal-poor stars as tracers of the chemical evolution of the Galaxy. Their isochrone ages are also systematically affected by atomic diffusion.

For the time being, the turbulent mixing needed to bring theoretical predictions in agreement with observations is prescribed in an ad hoc way. It would be desirable to isolate the physical process that gives rise to the turbulent mixing below the convective envelope. The predictions of hydrodynamic models will have to be put to the test by means of observations like the ones we presented here.

Recently,  ${}^6\text{Li}$  was traced in several metal-poor field stars at levels well above those that can be explained by Galactic production

(Asplund et al. 2006). The atomic diffusion corrections derived here ( $\approx +0.25$  dex; see Fig. 1) elevate the abundances even further. Together with pre-main-sequence burning, they thus aggravate the  ${}^6\text{Li}$  problem. If the detections are confirmed by more sophisticated modeling (cf. Cayrel et al. 2007), it is unclear where all this  ${}^6\text{Li}$  was synthesized; various processes are investigated (Jedamzik et al. 2006; Tatischeff & Thibaud 2007). Lithium thus remains an enigmatic element.

We are only beginning to investigate the effects of atomic diffusion and mixing in old stars observationally. More work is needed to establish their impact on stellar atmospheric abundances and ages. Globular clusters like NGC 6397 (see Fig. 9) will play a key role in this endeavor.

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*Facilities:* VLT:Kueyen (FLAMES+UVES)

## APPENDIX A

### NOTES ON INDIVIDUAL ELEMENTS

#### A1. LITHIUM

We adopt 0.1 dex as a representative error for the *absolute* lithium abundance. However, the star-to-star scatter among the TOP stars is smaller: at 0.05 dex ( $1\sigma$ ) it can likely be fully ascribed to observational uncertainties. Line strengths vary between 21.3 (star 12318) and 26.5 mÅ (star 506120). There are some indications for real differences in lithium abundance between the two SGB stars (see Fig. 10).

We use abundances in LTE, as the combined correction from 3D and NLTE was found to be very small (Barklem et al. 2003). NLTE corrections in 1D are typically  $-0.1$  dex for both TOP and SGB stars when charge exchange reactions are considered. They decrease

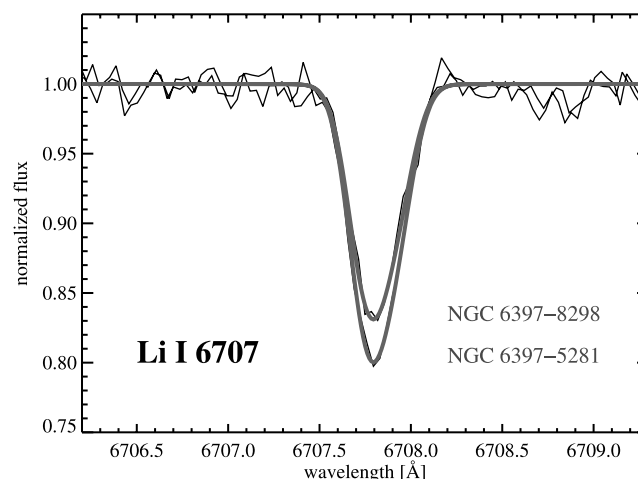


FIG. 10.—Observed Li I  $\lambda 6707$  line profiles for the two SGB stars. These two stars seem to have slightly (0.08 dex) different lithium abundances. With only two stars in this evolutionary stage it is, however, impossible to tell whether this indicates nonnegligible dispersion. [See the electronic edition of the *Journal* for a color version of this figure.]

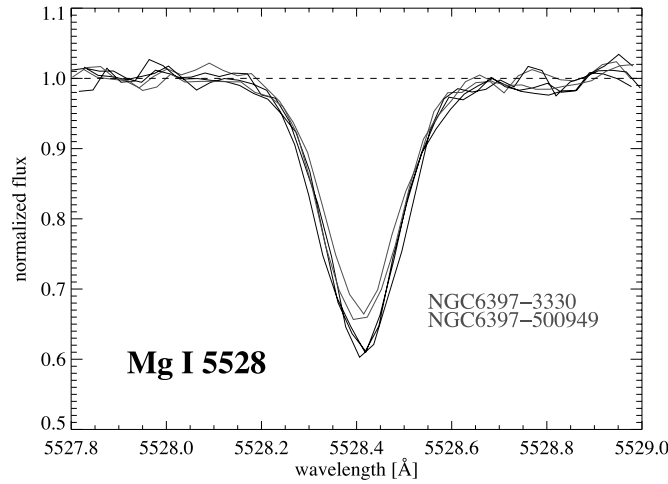


FIG. 11.—Observed Mg I  $\lambda 5528$  line profiles for the five bRGB stars. Both star 3330 and star 500949 have significantly weaker profiles than the other three bRGB stars. We attribute this to the conversion of Mg to Al commonly observed in globular clusters (see, e.g., G01). [See the electronic edition of the Journal for a color version of this figure.]

TABLE 7  
IRON LINES USED IN THE STELLAR PARAMETER AND IRON ABUNDANCE DETERMINATION

Line	TOP	SGB	bRGB	RGB
Fe I $\lambda 5225.5$ .....			X	X
Fe I $\lambda 5247.0$ .....				X
Fe I $\lambda 5250.2$ .....				X
Fe I $\lambda 5269.5$ .....	X			
Fe I $\lambda 5328.0$ .....	X			
Fe I $\lambda 5371.4$ .....	X			
Fe I $\lambda 5397.1$ .....	X		X	
Fe I $\lambda 5405.7$ .....	X	X	X	
Fe I $\lambda 5250.6$ .....				X
Fe I $\lambda 6421.3$ .....		X	X	X
Fe I $\lambda 6663.4$ .....				X
Fe I $\lambda 6494.9$ .....	X			
Fe I $\lambda 6593.8$ .....				X
Fe I $\lambda 6065.4$ .....		X	X	X
Fe I $\lambda 6200.3$ .....				X
Fe I $\lambda 6322.6$ .....				X
Fe I $\lambda 6546.2$ .....			X	X
Fe I $\lambda 6592.9$ .....		X	X	X
Fe I $\lambda 4890.7$ .....	X	X	X	X
Fe I $\lambda 4891.4$ .....	X	X	X	X
Fe I $\lambda 4918.9$ .....	X	X	X	X
Fe I $\lambda 4920.5$ .....	X	X	X	
Fe I $\lambda 4957.2$ .....	X	X	X	X
Fe I $\lambda 4957.5$ .....	X	X	X	
Fe I $\lambda 5139.2$ .....			X	
Fe I $\lambda 5139.4$ .....			X	
Fe I $\lambda 5232.9$ .....	X	X	X	X
Fe I $\lambda 5266.5$ .....	X	X	X	X
Fe I $\lambda 5217.3$ .....		X	X	X
Fe I $\lambda 5253.4$ .....				X
Fe I $\lambda 5324.1$ .....	X		X	X
Fe I $\lambda 5586.7$ .....	X	X	X	
Fe I $\lambda 5615.6$ .....		X	X	X
Fe I $\lambda 6232.6$ .....				X
Fe I $\lambda 6246.3$ .....		X	X	X
Fe I $\lambda 4985.2$ .....				X
Fe I $\lambda 5074.7$ .....			X	X
Fe I $\lambda 5364.8$ .....		X	X	X
Fe I $\lambda 5424.0$ .....	X	X	X	X
Fe I $\lambda 5410.9$ .....		X	X	X
Fe I $\lambda 6024.0$ .....				X

TABLE 7—Continued

Line	TOP	SGB	bRGB	RGB
Fe II $\lambda$ 6516.0.....				X
Fe II $\lambda$ 5284.1.....				X
Fe II $\lambda$ 5169.0.....	X	X	X	X
Fe II $\lambda$ 5018.4.....	X	X	X	X
Fe II $\lambda$ 4923.9.....	X	X	X	X
Fe II $\lambda$ 5362.8.....				X
Fe II $\lambda$ 5316.6.....	X	X	X	X
Fe II $\lambda$ 5234.6.....	X	X	X	X
Fe II $\lambda$ 5197.5.....		X	X	X
Fe II $\lambda$ 5284.1.....				X
Fe II $\lambda$ 6456.3.....				X
Fe II $\lambda$ 6247.5.....				X

to  $-0.07$  dex for the bRGB stars and further to  $-0.04$  dex for the RGB stars. The need for extra mixing discussed in § 5 is thus somewhat alleviated when 1D NLTE abundances are considered. Studies in 3D NLTE will shed further light on this question.

## A2. MAGNESIUM

As lines of silicon are not detected in our spectra, we use magnesium as an element for which the stellar structure models of Richard et al. (2005) predict trends very similar to silicon [ $\Delta \log \varepsilon(\text{Mg}) = 0.2$ ; see § 3.5]. However, magnesium is known to anticorrelate with aluminum in globular clusters. The atomic diffusion signature could thus be masked by such anticorrelations.

Line strength for Mg I  $\lambda$ 5528 varies between 42 (TOP stars) and 87 mÅ (RGB stars). NLTE effects on Mg I  $\lambda$ 5528 vary between  $+0.11$  and  $+0.14$  dex. Thus, the LTE abundance trend is very similar, albeit at lower overall magnesium abundances.

While we find no obvious line strength differences for the TOP and SGB stars, both the bRGB and RGB stars show some line strength variation for Mg I  $\lambda$ 5528. Figure 11 clearly shows that two of the five bRGB stars have weaker Mg I  $\lambda$ 5528 lines. This is confirmed by NLTE analyses of the Mg I  $b$  lines at 5172 and 5183 Å. The overall range of magnesium abundances is found to be 0.2 dex in both groups of evolved stars. Among the RGB stars, 11093 seems to be the least mixed, displaying the strongest magnesium lines and the weakest line of Na I  $\lambda$ 5688.

## A3. CALCIUM

Together with barium, calcium shows NLTE abundance trends that are significantly different from their LTE counterparts. While overionization dominates in the TOP stars (weakening the lines and increasing the abundances by between  $+0.05$  and  $+0.12$  dex), there are competing NLTE effects between the line core and the line wings as the lines become stronger toward the RGB stars. For example, Ca I  $\lambda$ 6162 has an average line strength of 43 mÅ in the TOP stars, and the NLTE correction is  $+0.1$  dex. In the RGB stars, this line is 92 mÅ strong and the NLTE effect is  $-0.05$  dex. Average NLTE effects for all three lines (Ca I  $\lambda$ 6122, 6162, and 6439) range from  $+0.11$  (TOP stars) to  $-0.03$  dex (RGB stars). In total,  $\Delta \log \varepsilon(\text{Ca})_{\text{LTE}} = 0.21$ , while  $\Delta \log \varepsilon(\text{Ca})_{\text{NLTE}} = 0.07$ .

## A4. TITANIUM

The titanium abundance is derived from two weak Ti II lines at 5188 and 5226 Å. The prior line is blended with a V I line at 5188.85 Å, but the resolving power of FLAMES-UVES is high enough to safely separate the contribution of this element. Line strengths vary between 30 and 80 mÅ (Ti I  $\lambda$ 5188) and between 22 and 67 mÅ (Ti I  $\lambda$ 5226). LTE is assumed to be a good approximation for these lines arising from transitions in the dominant ionization stage.

TABLE 8  
PHOTOMETRIC CALIBRATIONS FOR  $v - y$  BASED ON TWO DIFFERENT CALIBRATIONS OF THE INFRARED FLUX METHOD,  
ALONSO ET AL. (1996, 1999) AND RAMÍREZ & MELÉNDEZ (2005)

Index/Calibration	a0	a1	a2	a3	a4	a5	P0	P1	P2	P3	P4
Ramírez											
$(v - y)$ /giant.....	0.5067	0.4163	-0.0522	0.0132	-0.0984	-0.0141	3230.60	-7214.50	5698.73	-1894.18	226.107
$(v - y)$ /dwarf.....	0.4739	0.4552	-0.0556	-0.0379	-0.0378	-0.0186	269.223	-514.148	234.499	0.000	0.000
Alonso											
$(v - y)$ /giant.....	0.5408	0.3074	0.03415	-0.00796	-0.05368	-0.009701	...	...	...	...	...
$(v - y)$ /dwarf.....	0.3726	0.6648	-0.1597	-0.03442	-0.02909	-0.01220	...	...	...	...	...

NOTE.—The coefficients refer to the analytic formulae given in the respective paper.

TABLE 9  
PHOTOMETRIC STELLAR PARAMETERS OF THE 18 STARS OBSERVED WITH FLAMES-UVES

Star ID	R.A. (J2000.0)	Decl. (J2000.0)	$V$	$b - y$	$T_{\text{eff}}$ Dwarf/Giant	$\log g$ Dwarf/Giant	$v - y$	$T_{\text{eff}}$ Dwarf/Giant	$\log g$ Dwarf/Giant	$B - V$	$T_{\text{eff}}$ Dwarf/Giant	$\log g$ Dwarf/Giant	$V - I$	$T_{\text{eff}}$ Dwarf/Giant	$\log g$ Dwarf/Giant
NGC 6397-11093	17 40 13.950	-53 42 25.40	13.551	0.478	.../5102	.../2.51	1.052	.../5104	.../2.51	0.651	.../5224	.../2.56	0.875	.../5034	.../2.48
NGC 6397-13092	17 40 19.980	-53 39 17.70	13.644	0.478	.../5103	.../2.54	1.047	.../5115	.../2.55	0.646	.../5242	.../2.60	0.868	.../5051	.../2.52
NGC 6397-14592	17 40 23.840	-53 36 40.40	13.696	0.476	.../5113	.../2.57	1.041	.../5126	.../2.58	0.642	.../5251	.../2.63	0.865	.../5060	.../2.55
NGC 6397-7189	17 39 59.760	-53 45 03.90	13.729	0.474	.../5120	.../2.59	1.038	.../5134	.../2.59	0.641	.../5257	.../2.64	0.862	.../5066	.../2.56
NGC 6397-4859	17 39 48.710	-53 40 16.90	13.815	0.470	.../5139	.../2.63	1.028	.../5153	.../2.63	0.636	.../5272	.../2.68	0.857	.../5081	.../2.60
NGC 6397-502074	17 40 50.850	-53 36 08.80	13.853	0.468	.../5148	.../2.65	1.024	.../5162	.../2.65	0.634	.../5279	.../2.70	0.854	.../5088	.../2.62
NGC 6397-3330	17 39 40.250	-53 41 49.60	15.227	0.428	5405/5351	3.30/3.28	0.932	5436/5359	3.31/3.28	0.568	5492/5491	3.33/3.33	0.784	5368/5298	3.28/3.25
NGC 6397-23267	17 40 43.750	-53 37 17.40	15.339	0.424	5429/5373	3.35/3.33	0.920	5466/5385	3.37/3.34	0.560	5520/5519	3.39/3.39	0.778	5386/5298	3.34/3.30
NGC 6397-15105	17 40 25.540	-53 43 31.10	15.439	0.419	5458/5399	3.40/3.38	0.909	5497/5411	3.42/3.39	0.551	5552/5551	3.44/3.44	0.770	5410/5321	3.39/3.35
NGC 6397-500949	17 40 34.580	-53 33 20.70	15.514	0.416	5480/5418	3.44/3.42	0.900	5520/5431	3.46/3.42	0.544	5576/5574	3.48/3.48	0.764	5428/5338	3.42/3.39
NGC 6397-6391	17 39 55.900	-53 35 11.90	15.551	0.412	5503/5437	3.47/3.44	0.890	5547/5452	3.48/3.45	0.539	5593/5591	3.50/3.50	0.760	5442/5351	3.44/3.41
NGC 6397-8298	17 40 04.130	-53 40 53.10	15.832	0.369	5791/5677	3.68/3.64	0.799	5819/5666	3.69/3.63	0.478	5822/5819	3.69/3.69	0.689	5682/5571	3.64/3.60
NGC 6397-5281	17 39 50.570	-53 35 21.70	15.839	0.368	5802/5687	3.68/3.64	0.796	5828/5673	3.69/3.64	0.476	5832/5828	3.69/3.69	0.686	5693/5580	3.65/3.61
NGC 6397-10197	17 40 10.770	-53 38 26.40	16.160	0.314	6204/...	3.93/...	0.695	6187/...	3.93/...	0.402	6135/...	3.91/...	0.585	6096/...	3.90/...
NGC 6397-12318	17 40 17.640	-53 39 34.20	16.182	0.312	6217/...	3.95/...	0.691	6201/...	3.94/...	0.399	6148/...	3.93/...	0.581	6113/...	3.92/...
NGC 6397-9655	17 40 09.090	-53 43 26.40	16.200	0.311	6227/...	3.96/...	0.688	6212/...	3.95/...	0.396	6159/...	3.94/...	0.578	6128/...	3.93/...
NGC 6397-506120	17 40 41.590	-53 45 49.30	16.271	0.308	6248/...	3.99/...	0.683	6233/...	3.99/...	0.391	6179/...	3.97/...	0.570	6163/...	3.97/...
NGC 6397-507433	17 40 16.070	-53 47 18.60	16.278	0.308	6249/...	3.99/...	0.682	6235/...	3.99/...	0.391	6180/...	3.97/...	0.570	6166/...	3.97/...
$\Delta T_{\text{eff}}(\text{TOP} - \text{RGB})$					1108	1.38		1082	1.37		906	1.31		1070	1.38
$\Delta \log g(\text{TOP} - \text{RGB})$															

NOTES.—The indices are calibrated on the IRFM by Alonso et al. (1996, 1999). At the metallicity of NGC 6397, the calibrations of Ramirez & Meléndez (2005) produce very similar results. For the SGB and bRCGB stars, the results of both the dwarf and giant calibration are given.

## A5. BARIUM

The analysis of this element is solely based on Ba II  $\lambda 6496$ . Line strengths vary between 8 (TOP stars) and 66 mÅ (RGB stars). While the LTE trend is steep [ $\Delta \log \varepsilon(\text{Ba})_{\text{LTE}} = 0.21$ ], no significant trend is found in NLTE [ $\Delta \log \varepsilon(\text{Ba})_{\text{NLTE}} = 0.00$ ]. Like in the case of calcium, NLTE effects change sign in going from the TOP group (+0.11 dex) to the RGB group (−0.10 dex). The SGB and rRGB groups fall in between in terms of NLTE corrections.

We caution that the TOP star line is rather weak and may well be affected by telluric absorption.

No atomic diffusion predictions exist for barium. In the future, efforts should be made to compare our observations with detailed calculations for the expected behavior of barium between these groups of stars.

## A6. IRON

In Table 7 the lines used for the surface gravity, iron abundance, and microturbulence determination for the four groups of stars are given. Lines are listed according to their lower excitation energy; the corresponding line data can be found in Korn et al. (2003).

## APPENDIX B

## PHOTOMETRIC CALIBRATIONS AND STELLAR PARAMETERS

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