Putting atomic diffusion theory of magnetic ApBp stars to the test: evaluation of the predictions of time-dependent diffusion models

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ABSTRACT

A series of recent theoretical atomic diffusion studies has addressed the challenging problem of predicting inhomogeneous vertical and horizontal chemical element distributions in the atmospheres of magnetic ApBp stars. Here we critically assess the most sophisticated of such diffusion models – based on a time-dependent treatment of the atomic diffusion in a magnetized stellar atmosphere – by direct comparison with observations as well by testing the widely used surface mapping tools with the spectral line profiles predicted by this theory. We show that the mean abundances of Fe and Cr are grossly underestimated by the time-dependent theoretical diffusion model, with discrepancies reaching a factor of 1000 for Cr. We also demonstrate that Doppler imaging inversion codes, based either on modelling of individual metal lines or line-averaged profiles simulated according to theoretical three-dimensional abundance distribution, are able to reconstruct correct horizontal chemical spot maps despite ignoring the vertical abundance variation. These numerical experiments justify a direct comparison of the empirical two-dimensional Doppler maps with theoretical diffusion calculations. This comparison is generally unfavourable for the current diffusion theory, as very few chemical elements are observed to form overabundance rings in the horizontal field regions as predicted by the theory and there are numerous examples of element accumulations in the vicinity of radial field zones, which cannot be explained by diffusion calculations.

Key words: diffusion – line: profiles – stars: abundances – stars: chemically peculiar.

1 INTRODUCTION

The upper main-sequence chemically peculiar stars are distinguished by a bewildering diversity of surface chemical anomalies. Several groups of these stars exhibit conspicuous overabundances of iron-peak and heavy elements in comparison to the abundance patterns of the Sun and cool main-sequence stars. Many of these chemically peculiar stars possess strong, stable, globally organized magnetic fields. These so-called magnetic ApBp stars exhibit the most extreme abundance anomalies, often accompanied by the horizontal (e.g. Kochukhov 2017, and references therein) and vertical (e.g. Ryabchikova 2014b, and references therein) chemical abundance inhomogeneities.

It is generally thought that non-solar surface abundances in the upper main-sequence stars arise due to selective levitation and sinking of chemical elements under the competing influence of radiation pressure and gravity. This atomic diffusion hypothesis (Michaud 1970; Michaud, Alecian & Richer 2015) has been reasonably successful in explaining the (horizontally homogeneous) build-up of metals in the radiative interiors of old Sun-like stars (Richard, Michaud & Richer 2005) and metallic-line A-type stars (Vick et al. 2010). In comparison, atmospheric diffusion calculations required to explain large element overabundances in magnetic ApBp stars and, especially, their highly non-uniform surface abundance topologies, are considerably more uncertain and computationally challenging. This is due to the necessity of detailed treatment of the radiative transport in a magnetized stellar atmosphere and uncertainties concerning the potential impact of several poorly constrained effects, such as weak stellar winds, on the diffusion calculations.

The first self-consistent equilibrium (based on the assumption of zero net particle flux) atmospheric diffusion models were presented by Hui-Bon-Hoa, LeBlanc & Hauschildt (2000) for blue horizontal-branch stars. Later, these models were improved and applied to chemically peculiar stars (LeBlanc & Monin 2004; LeBlanc et al. 2009). These calculations, predicting large mean element overabundances as well as substantial vertical chemical gradients in the line-forming atmospheric regions, compare favourably with observations (Ryabchikova 2008; Ryabchikova & LeBlanc 2011;
2 THEORETICAL DIFFUSION MODELS

Not every theoretical atomic diffusion calculation which has appeared in the recent literature lends itself to a straightforward quantitative analysis and comparison with observations. The comprehensive presentation of the bi-dimensional stratification profiles by Alecian & Stift (2010) provided data for 16 chemical elements and 4 values of effective temperature. However, these authors did not include information on the physical height in the stellar atmosphere in their plots, limiting their usefulness for an independent quantitative analysis. They also presented calculations only for a 20 kG dipolar magnetic field, which is well in excess of the 2.5 kG mean dipolar field strength of the nearby ApBp stars (Power et al. 2008) and the 2.2 kG mean field of the Ap stars typically targeted by DI studies (Kochukhov 2017). In addition, the bi-dimensional abundance maps presented by Alecian & Stift (2010) were based on only three individual stratification profiles at different field inclinations. Subsequent higher angular resolution calculations by Alecian (2012) revealed a significantly more structured surface abundance distribution, corresponding, in the case of Fe, to an equatorial over-abundance ring of only ±4° width.

Considering the newer time-dependent diffusion models, Alecian & Stift (2017) presented three-dimensional abundance distributions of Cr and Fe in a putative offset dipolar magnetic field geometry corresponding to that of the extraordinarily magnetic, cool Ap star HD 154708 (Hubrig et al. 2005). This object can hardly be considered representative of early-A magnetic chemically peculiar stars, which currently provide the bulk of observational constraints for the atomic diffusion theory. Furthermore, its low projected rotational velocity and an unfavourable inclination preclude deriving detailed magnetic and chemical spot maps which could be usefully compared to the model predictions.

This leaves us with the study by SA16, who presented the predicted vertical dependence of the Cr, Fe, and V abundance across the surface of a typical Ap star ($T_{\text{eff}} = 10000$ K, log $g = 4.0$) with a 1.95 kG centred dipolar magnetic field. The vertical abundance profiles were calculated for nine different magnetic co-latitudes, enabling fine sampling of the stellar surface. By virtue of choosing representative stellar parameters and tabulating the results at a sufficiently dense angular grid, these calculations are well suited for comparison with observations of typical Ap stars in this temperature range and for testing empirical abundance mapping tools. We exploit these theoretical (3D) distributions to compute synthetic spectral timeseries, which we in turn employ to reconstruct the implied surface distribution as viewed through the filter of (2D) DI.

However, no stellar rotation or other surface effects were considered in the calculations by SA16. Consequently, the orientation of the dipolar field axis and associated chemical abundance maps with respect to the stellar rotational axis is arbitrary. In this study we assumed a large obliquity angle ($\beta = 90^\circ$) and a moderately large inclination angle ($i = 60^\circ$), resulting in a reversing longitudinal magnetic field and significant line profile variation. The adopted magnetic field geometry is illustrated in Fig. 1. Figs 2 and 3 present the horizontal abundance maps of Fe and Cr at four representative optical depths. These maps were obtained with the help of linear interpolation within the grid of nine vertical abundance profiles provided for each element by SA16 in their fig. 5. It is evident that, despite being based on a significantly different physical foundation and different numerical treatment compared to the equilibrium approach to the atmospheric diffusion, the time-dependent diffusion model predicts a qualitatively similar accumulation of chemical elements, which coincides with...
Figure 1. Dipolar magnetic field topology adopted in our calculations. The upper row of spherical plots shows the field orientation (outward and inward pointing vectors) plotted over the field modulus distribution (colour map). The field strength scale, in kG, is indicated by the side bar. The lower set of spherical plots shows the corresponding field inclination with respect to the local surface normal. In this case, the side bar gives the absolute value of the field inclination angle in degrees. The solid contour lines correspond to the nine field inclinations considered by SA16. The star is shown at five rotational phases, as indicated above each panel. The thick double line and the short bar indicate the stellar rotational equator and the pole, respectively.

Figure 2. Surface distribution of Fe abundance at the optical depths $\log \tau_{5000} = 0.0, -1.0, -2.0, \text{and} -3.0$ (indicated with labels at left) for the time-dependent diffusion model of SA16. The abundance scale, in the log $N_{\text{el}}/N_{\text{tot}}$ units, is indicated by the colour bar at right.

3 MODEL ATMOSPHERE AND LINE PROFILE CALCULATIONS

Using the set of Fe and Cr stratification profiles reported by SA16, we calculated a grid of nine LLMODELS (Shulyak et al. 2004) atmospheres for $T_{\text{eff}} = 10\,000$ K and log $g = 4.0$. These calculations were iterated several times to achieve full consistency between the stratification specified on the $\log \tau_{5000}$ scale and the model $T(\tau)$ relation. Abundances of other chemical elements were assumed to be solar and their vertical distributions were taken to be homogeneous. As shown by Khan & Shulyak (2007), Fe and Cr are by far the most important sources of line opacity in ApBp-star atmospheres. SA16 also showed that there is little back-reaction of the stratification of other elements on that of Fe, implying that individual abundances and stratifications of other elements are relatively unimportant for...
the model atmosphere structure. In addition to chemically stratified models, we also calculated a reference solar abundance model for $T_{\text{eff}} = 10000$ K and $\log g = 4.0$.

In the next step, we employed the INVERS13 code (Kochukhov et al. 2013) to simulate a set of Fe II spectral line profiles for the theoretical 3D abundance distribution of Fe. Originally developed for a self-consistent magnetic field and temperature mapping, INVERS13 can be used in the forward mode to synthesize the Stokes parameter spectra for an arbitrary surface map relating a certain scalar parameter to a grid of local model atmospheres. In this case, the model grid incorporates different Cr and Fe abundance stratifications as a function of the magnetic co-latitude. Using INVERS13, we calculated profiles of the intermediate strength Fe II lines 4273.32, 4520.22, 4555.89, 4666.75 Å, used by Silvester et al. (2014) in their magnetic DI study of $\alpha^2$ CVn. The Zeeman effect due to the (vertically uniform) 1.95 kG dipolar magnetic field was included in detail, with the individual Zeeman splitting patterns and other parameters of the studied transitions extracted from the VALD3 data base (Ryabchikova et al. 2015). The Fe line profiles were calculated for 20 equidistant rotational phases, assuming the projected rotational velocity of $v\sin i = 25$ km s$^{-1}$ and the resolving power of $\lambda/\Delta\lambda = 120000$, corresponding to the HARPS polarimeter (Piskunov et al. 2011). Random noise with $\sigma = 2 \times 10^{-3}$ (signal-to-noise ratio 500) was added to the data. These spectra will be used in Section 4.1 to test the individual line abundance mapping procedure.

Another set of non-magnetic local Stokes I spectra was calculated for each of the nine chemically stratified model atmospheres with the SYNMAST (Kochukhov, Makaganiuk & Piskunov 2010) code, this time considering all metal lines deeper than 1 per cent of the continuum in the 4000–7000 Å wavelength interval. The local intensity profiles were tabulated for a grid of 20 limb angles. The instrumental broadening corresponding to the resolving power of 120 000 was applied to both sets of calculations. The resulting zero $v\sin i$ spectra will be used in Section 4.1 for the determination of mean Fe and Cr abundances. The $v\sin i = 25$ km s$^{-1}$ spectra were further modified by adding random noise with $\sigma = 1 \times 10^{-3}$ (signal-to-noise ratio 10). These spectra will be used for the least-squares deconvolution (LSD) analysis and inversion in Section 4.3.

4 ANALYSIS OF THEORETICAL 3D ABUNDANCE MAPS

4.1 Mean abundances

We used the zero $v\sin i$ flux profiles for rotational phases 0.0 (minimum strength of Fe and Cr lines) and 0.25 (maximum Fe and Cr line strength), as well as the phase-averaged spectrum for the classical abundance determination with the equivalent width method. Initially, we aimed to perform this analysis based on the same set of neutral and singly ionized lines as was employed by Ryabchikova (2014a) for the analysis of the non-magnetic equilibrium diffusion calculations by LeBlanc et al. (2009). However, it turned out that, with the iron distribution from the study by SA16, only nine
lines from that list (Fe I 5383.37 Å and Fe II 5410.91, 4923.92, 5132.66, 5169.03, 5197.58, 5291.66, 5325.55, 6432.68 Å) were strong enough for a meaningful abundance estimate. The mean Fe abundance inferred from these spectral features using the reference solar-abundance model atmosphere is \( \log N_\text{Fe}/N_\text{tot} = -4.77 \pm 0.12 \) for phase 0.0, \(-4.61 \pm 0.17\) for phase 0.25, and \(-4.68 \pm 0.15\) for the phase-averaged spectrum. The studied lines cover a wide range of excitation potentials, from 2.8 to 10.5 eV, and therefore yield slightly different abundances depending on their formation depth. This is reflected in the quoted standard deviations. On the other hand, the range of mean abundance variation with rotational phase is only 0.09 dex.

Determination of the mean Cr abundance was based on equivalent widths of eight Cr II lines (4261.91, 4558.65, 4554.99, 4588.20, 4592.05, 4618.80, 4634.07, 4824.13 Å). These are some of the strongest Cr features in the spectra of ApBp stars and are often unsuitable for an abundance analysis due to their saturation. However, for the 3D Cr abundance distribution published by SA16 the equivalent widths of these lines do not exceed 25 mÅ. Using these Cr II transitions, we derived \( \log N_{\text{Cr}}/N_\text{tot} \) for phase 0.0, \(-7.39 \pm 0.02\) for phase 0.0, \(-7.30 \pm 0.01\) for phase 0.25, and \(-7.34 \pm 0.01\) for the phase-averaged spectrum. All considered Cr II lines have excitation potentials in a narrow range from 3.9 to 4.1 eV and therefore similar line formation depth, which explains the small line-to-line scatter.

In Fig. 4 we compare the phase-averaged Fe and Cr abundances inferred by our analysis of the SA16 model with observed Fe and Cr abundances for the sample of normal and chemically peculiar ApBp stars compiled by Ryabchikova (2005), and with the mean abundances corresponding to the non-magnetic diffusion models by LeBlanc & Monin (2004) and LeBlanc et al. (2009) (see Ryabchikova 2008, 2014a for details). It is evident that while the latter theoretical models achieve a reasonable agreement with observations in a wide \( T_\text{eff} \) range, the time-dependent diffusion calculations by SA16 underestimate the apparent mean Fe abundance at \( T_\text{eff} = 10000 \) K by about 1.5 dex and underpredict the mean Cr abundance by as much as 3 dex.

4.2 Doppler imaging with individual lines

In this test we used the Stokes \( I \) profiles of the four Fe II lines computed as described in Section 3 for mapping the horizontal Fe abundance distribution with the INVERS10 code (Kochukhov & Piskunov 2002; Piskunov & Kochukhov 2002). The fixed dipolar magnetic field was taken into account. This inversion was carried out under the usual assumption of a vertically homogeneous Fe abundance distribution and relied upon a single, solar-abundance model atmosphere. Following the practice of many recent multilines abundance DI studies, we allowed the code to adjust oscillator strengths of three out of four lines. In this case, such an adjustment partly compensates for the chemical stratification effects (which are not included in our model). In applications to real stars, this oscillator strength correction also alleviates inevitable errors in atomic data and in treatment of unresolved blends.

The DI inversion was constrained with the Tikhonov regularization function. The corresponding regularization parameter was chosen according to the procedure described by Kochukhov (2017). The resulting abundance map is compared to theoretical distribution in Fig. 5 and the fit to 20 phases of simulated observations is presented in Fig. 6. INVERS10 succeeds in reproducing the spectral line profiles corresponding to the theoretical 3D Fe abundance distribution with a 2D map. The final standard deviation of the fit (0.22 per cent) is only marginally larger than the nominal random noise (0.2 per cent) injected in the data. The log \( g_f \) corrections do not exceed 0.06 dex. The 2D Fe map obtained by INVERS10 is shown in Fig. 5b. This distribution turns out to be very similar to the cross-section of the input 3D element distribution at \( \tau_{5000} = -2 \) (Fig. 5a), which corresponds to the typical formation depths of intermediate strength Fe lines. The morphology of the principal surface features and the range of Fe abundance variation across the stellar surface agree very well in these two maps.

4.3 Doppler imaging with least-squares deconvolved profiles

In the final test we assessed the reconstruction of the Fe horizontal abundance map from the Stokes \( I \) LSD profiles. This experiment
is motivated by the common application of such mean profiles for simultaneous mapping of the magnetic and abundance structures of ApBp stars (Folsom et al. 2008; Kochukhov et al. 2014, 2017; Oksala et al. 2018).

The input data for the inversion was calculated by applying the LSD code (Kochukhov et al. 2010) to 20 rotational phases of \( \sin i = 25 \) km s\(^{-1} \) spectra calculated for the wide wavelength interval as described in Section 3. The LSD line mask was comprised of 566 Fe I and II lines deeper than 5 per cent of the continuum, as well as 249 blending features of other chemical elements treated with a separate mean profile. The LSD procedure increased the signal-to-noise ratio from 100 per 0.8 km s\(^{-1} \) velocity bin in the input spectra to about 2300 per 1.0 km s\(^{-1} \) bin in the mean profiles. The resulting LSD profiles were interpreted with the INVERSLSD surface mapping code, based on the methodology described by Kochukhov et al. (2014). This inversion code models the intensity or/and polarization LSD spectra using a pre-computed grid of local mean profiles. This grid was calculated by applying LSD to the local spectra synthesized for a range of vertically homogeneous Fe abundances, using a single, reference solar abundance model atmosphere.

The final model fit to the simulated LSD profiles is shown in Fig. 7. The corresponding 2D Fe distribution inferred by INVERSLSD is illustrated in Fig. 7c. Once again, we find a very good concordance between this LSD-based Fe map, the results of individual line mapping discussed in Section 4.2, and a horizontal cross-section of the theoretical 3D iron abundance distribution.

5 CONCLUSIONS AND DISCUSSION

In this paper we have carried out a detailed assessment of the predictions of recent theoretical time-dependent atomic diffusion calculations by Stift & Alecian (2016). Their model aims to realistically describe the overall accumulation of metals, as well as the vertical and horizontal chemical inhomogeneities, in the atmospheres of magnetic ApBp stars. Deriving mean Fe and Cr abundances from the spectra generated according to the three-dimensional theoretical distributions of these elements, we revealed a major discrepancy between theoretically predicted and observationally inferred mean element concentrations. Contrary to the well-established \( \sim 1 \) dex Fe and \( \sim 2 \) dex Cr average overabundances typical of Ap stars with \( T_{\text{eff}} \) close to 10 000 K, the model by SA16 predicts a near-solar mean abundance of Fe and \( \sim 1 \) dex underabundance of Cr.

To the best of our knowledge, the inability of time-dependent diffusion calculations to predict correct mean Fe-peak abundances has not been previously discussed in the literature. Considering the presentation by Alecian & Stift (2010) of the bi-dimensional element distributions, one can conclude that the problem of underpredicting abundances of certain element (e.g. Si) was also present to some extent in their earlier equilibrium models. On the other hand, Cr and Fe were estimated to be overabundant at \( T_{\text{eff}} = 10 000 \) K (see figs 14 and 15 of Alecian & Stift 2010), in agreement with independent non-magnetic atomic diffusion modelling by LeBlanc et al. (2009). The latter calculations have been extensively verified by comparison with observations and were shown to yield correct mean Fe-peak element abundances, to reproduce their trends with \( T_{\text{eff}} \), and to provide a reasonable match to the observed vertical element distributions (Ryabchikova 2014a,b). In this context, the prediction of completely unrealistic mean abundances by the newest time-dependent version of the atomic diffusion theory is a step backwards. This problem needs to be addressed before these theoretical models can be considered to be a competitive contribution to our understanding of these phenomena.

In addition to examining mean Fe and Cr abundances, we performed a series of numerical simulations to study the robustness of the standard 2D DI analysis applied to the line profiles computed according to 3D theoretical element distributions. These tests demonstrated that DI mapping, whether based on modelling of individual spectral lines or on interpretation of LSD profiles, yields sensible two-dimensional element distributions with the surface structure details and abundance ranges closely matching the input 3D model at the typical line-forming atmospheric depth. These results provide a clear demonstration that vertical
Testing time-dependent atomic diffusion theory

Figure 6. Comparison of the Stokes $I$ profiles of individual Fe II lines simulated according to the 3D atomic diffusion model (symbols) and the fit achieved by the INVERS10 code (solid line) with the 2D Fe abundance map illustrated in Fig. 5b. Rotational phases are indicated on the right-hand side of the plot. The spectra are offset vertically. The error bars in the lower right corner indicate the horizontal (0.5 Å) and vertical (3 per cent) scales.

abundance gradients do not confuse DI codes and that the resulting empirical 2D surface maps can be directly compared to the atomic diffusion theory.

However, for a number of years, attempts to compare theoretically computed ApBp-star abundance maps with real observations appear to have been largely futile due to a fundamental failure of modern diffusion calculations to generate the observed diversity of the surface locations of chemical spots. As summarized by Alecian (2015) for the equilibrium diffusion model, all elements that are expected to exhibit a strongly non-uniform distribution across the stellar surface (Alecian specifically mentions Mg, Al, Ti, V, Cr, Mn, Fe, Co, Ni) are expected to accumulate at different depths only in the region of nearly horizontal magnetic field lines, i.e. at the magnetic equator for stars with dipole-like global field geometries. As of yet, no equivalent summary of the time-dependent diffusion predictions has been published. However, according to Alecian & Stift (2017) as well as Figs 2 and 3 of our paper, at least Cr and Fe are, again, predicted to accumulate exclusively at the magnetic equator.

As noted by many observational studies (e.g. Kochukhov et al. 2004, 2017; Nesvacil et al. 2012; Silvester et al. 2014, 2015), such equatorial overabundance rings are exceedingly rare in real ApBp stars. The only well-established examples of such surface structures are the O map of ε UMa (Rice, Wehlau & Holmgren 1997) as well as the C and O distributions of HR 3831 (Kochukhov et al. 2004). All other cases of various chemical elements mapped in about 40 ApBp stars show different distributions, often with spots located exactly at, or close to, the magnetic poles, where no element expected to exhibit a strongly non-uniform distribution across the stellar surface (Alecian specifically mentions Mg, Al, Ti, V, Cr, Mn, Fe, Co, Ni) are expected to accumulate at different depths only in the region of nearly horizontal magnetic field lines, i.e. at the magnetic equator for stars with dipole-like global field geometries. As of yet, no equivalent summary of the time-dependent diffusion predictions has been published. However, according to Alecian & Stift (2017) as well as Figs 2 and 3 of our paper, at least Cr and Fe are, again, predicted to accumulate exclusively at the magnetic equator.

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chemical elements cannot be the same. In this case, it is evident
make it abundantly clear that the surface distributions of these two
DI mapping of this star by Silvester et al. (2014). These curves
the equivalent width variation of Cl and Cr lines employed for the
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Figure 8. Variation of the mean longitudinal magnetic field (upper panel) and relative equivalent widths (lower panel) of Cl (circles) and Cr (squares) lines in the spectrum of the prototypical Ap star α² CVn.

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To conclude, our evaluation of the time-dependent atomic diffusion calculations by SA16 demonstrates two major weaknesses of their model. First, their calculations fail to produce mean abundance accumulation compatible with large Fe-peak element overabundances observed in late-B and early-A magnetic ApBp stars. Second, the prediction of similar horizontal abundance distributions, with accumulation at the magnetic equator for all elements, stands in fundamental conflict with the well-established diversity of the surface abundance structures in ApBp stars. It appears that, despite notable advances in the numerical treatment of polarized radiative transfer and its coupling with the atomic diffusion processes in a magnetized stellar atmosphere, the time-dependent diffusion model by SA16 does not reach the level of realism necessary for interpretation of observations of real stars.
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