

Outline

- The cosmological principle:
 - Isotropy
 - Homogeneity
- Big Bang vs. Steady State cosmology
- Redshift and Hubble's law
- Scale factor, Hubble time, Horizon distance
- Olbers' paradox: Why is the sky dark at night?
- Particles and forces
- Theories of gravity: Einstein vs. Newton
- Cosmic curvature

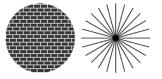
Covers chapter 2 + half of chapter 3 in Ryden

The Cosmological Principle I

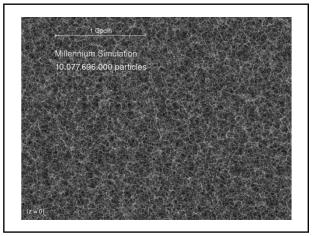
- •Modern cosmology is based on the assumption that the Universe is:

Isotropic

•Homogeneous \(\) The cosmological principle



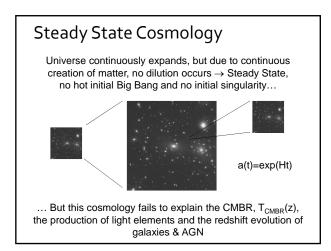
The Cosmological Principle II •These tenets seem to hold on large scales (>100 Mpc), but definitely not on small r<17.55, d>2", 6°slice Voids typically 70 Mpc across

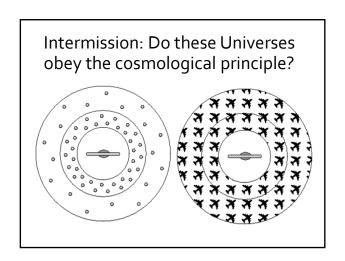


The Perfect Cosmological Principle

- In this case, one assumes that the Universe on large scales is:
 - Homogeneous
 - Isotropic
 - Non-evolving

This is incompatible with the Big Bang scenario, but the Steady State model (popular in the 1940-1960s) was based on this idea



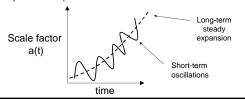


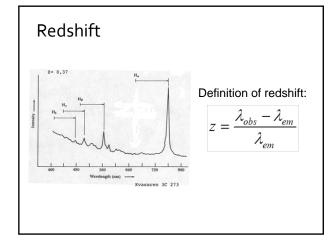
Suggestion for Literature Exercise: Quasi-Steady State Cosmology

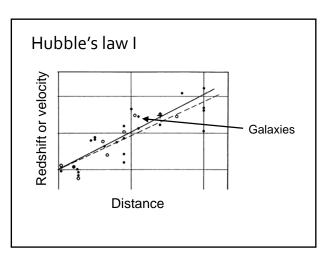
- Attempt in 1990s to resurrect Steady-State and explain the:
 - CMBR
 - production of light elements
 - dark matter
 - supernova type la data
 - Large-scale structure

Suggestion for Literature Exercise: Quasi-Steady State Cosmology

- Cyclic creation events → Long-term steady expansion, but with short-term oscillations
- To meet observational constraints, QSS requires:
 - Strange intergalactic dust
 - Cyclic creation events ("little bangs") which cause local expansion of space







Hubble's law II

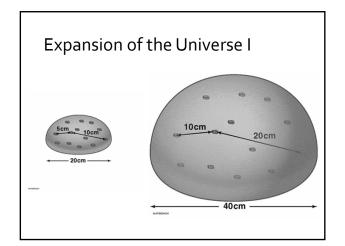
Hubble's law:

The Hubble "constant" Luminosity distance $z = \frac{H_0 d}{c}$

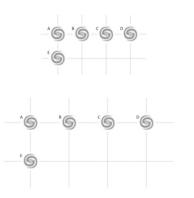
In observational astronomy, the term recession velocity, v, occurs frequently:

At low z:

$$z \approx \frac{v}{c} \rightarrow v = H_0 d$$

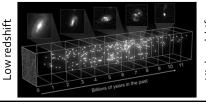


Expansion of the Universe II



Redshift and distance I

- Low redshift (z≈o) corresponds to:
 - Small distance (local Universe)
 - Present epoch in the history of the Universe
- High redshift corresponds to:
 - Large distance
 - Earlier epoch in the history of the Universe



High redshift

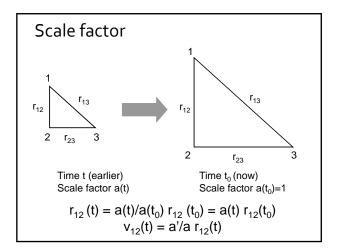
Redshift and distance II

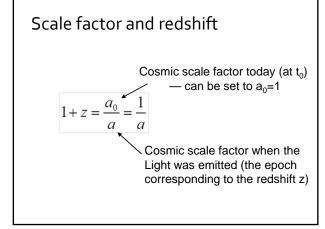
- •But beware:
 - At low redshift, Doppler components coming from peculiar motions may be substantial – must be corrected for before d is derived from z
 - The redshift coming from cosmic expansion is <u>not</u> a Doppler shift don't treat it like one!
 - The linear version of Hubble's law is only appropriate at z<0.15 (at 10% accuracy)

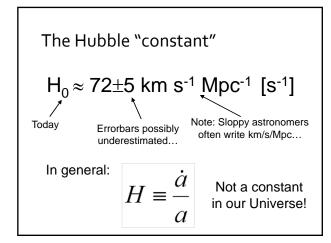
Intermission

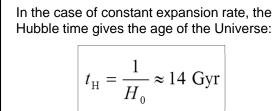


 $z \approx -0.001$ What does it mean?



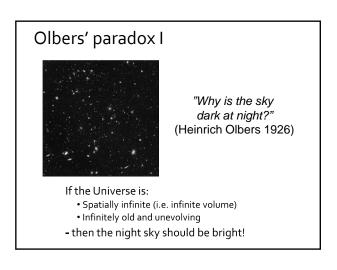


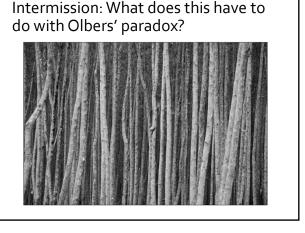


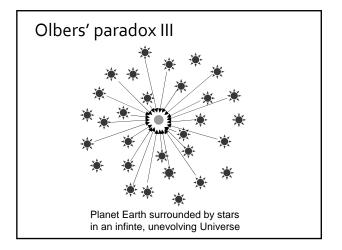


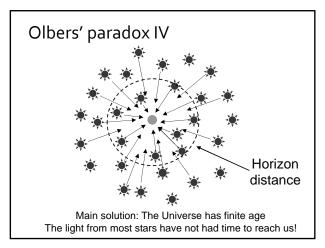
Hubble time

In more realistic scenarios, the expansion rate changes over time, but the currently favoured age of the Universe is still pretty close – around 13—14 Gyr.









Horizon distance

- Horizon distance = Current distance to the most faraway region from which light has had time to reach us
- This delimits the causally connected part of the Universe an observer can see at any given time
- Horizon distance at time t₁:

$$d_{\text{hor}}(t_1) = c \int_{t=0}^{t_1} \frac{\mathrm{d}t}{a(t)}$$

• Most realistic scenarios give:

 $d_{hor}(t_o)$ ~c/ H_o (the so-called Hubble radius)

Particles and forces I

- •The particles that make up the matter we encounter in everyday life:
 - Protons, p
 938.3 MeV
 Neutrons, n
 939.5 MeV
 Electrons, e

 Baryons (made of 3 quarks)

Since most of the mass of 'ordinary matter' is contributed by protons and neutrons, such matter is often referred to as *baryonic*. Examples of mostly baryonic objects: Planets, stars, gas clouds (but not galaxies or galaxy clusters)

Lepton

Particles and forces II

- •Other important particles (for this course):
 - ullet Photon, γ Massless, velocity: c
 - $\begin{array}{l} \bullet \mbox{ Neutrinos, } \nu_e \ \nu_\mu \ \nu_\tau \\ \sim \mbox{eV (?), velocity close to c} \\ \mbox{Interacts via weak nuclear force only} \end{array}$

Particles and forces III

- The four forces of Nature:
 - Strong force

0.511 MeV

- Very strong, but has short range (~10⁻¹⁵ m)
- Holds atomic nuclei together
- Weak force
 - Weak and has short range
- Responsible for radioactice decay and neutrino interactions
- Electromagnetic force
 - Weak but long-range
- Acts on matter carrying electric charge
- Gravity
- Weak, very long-range and always attractive

On the large scales involved in cosmology, gravity is by far the dominant one

Newtonian gravity

- Space is Euclidian (i.e. flat)
- Planet are kept in their orbits because of the gravitational force:

$$F = -\frac{GM_g m_g}{r^2}$$
 Gravitational mass

• The acceleration resulting from the gravitational force:

 $F = m_i a$ Inertial mass

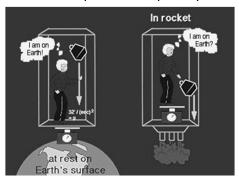
Equivalence Principle

• Gravitational acceleration towards an object with mass M_a is:

$$a = -\frac{GM_g}{r^2} \left(\frac{m_g}{m_i}\right)$$

- Empirically $M_q = M_i$ (to very high precision)
- The equality of gravitational mass and inertial mass is called the equivalence principle
- In Newtonian gravity, $M_{\rm g}$ = $M_{\rm i}$ is just a strange coincidence, but in General Relativity, this stems from the idea that masses cause curvature of space

Intermission: What does this have to do with the equivalence principle?



General Relativity

- 4D space-time
- Mass/energy curves space-time
- Gravity = curvature
- Pocket summary:
 - Mass/energy tells space-time how to curve
 - Curved space-time tells mass/energy how to move



Small-scale curvature

Small-scale distortions caused by astronomical objects

What about the large-scale curvature?

Global Curvature I

In the world models of general relativity, our Universe may have spatial curvature (on global scales)

Positive curvature

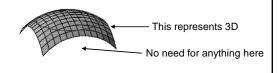
Negative curvature

Zero curvature (flat/Euclidian space)

Global Curvature II

Very tricky stuff...

- This an intrinsic curvature in 3D space
- Note: No need for encapsulating our 3D space in 4D space to make this work



Global Curvature III

Angles in curved spaces







Flat: $\alpha + \beta + \gamma = 180^{\circ}$

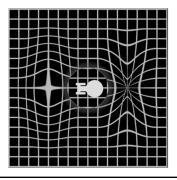
Negative: $\alpha + \beta + \gamma < 180^{\circ}$

Positive: $\alpha + \beta + \gamma > 180^{\circ}$

Intermission: What is this figure meant to illustrate?



Intermission: What is this figure meant to illustrate?



Metrics I

- Metric: A description of the distance between two points
- •Metric in 2 dimensional, flat space:

$$ds^2 = dx^2 + dy^2 \qquad (F$$

(Pythagoras)

• Metric in 3 dimensional, flat space:

$$ds^2 = dx^2 + dy^2 + dz^2$$

Metrics II

• Metric in 3 dimesions, flat space, polar coordinates:

$$ds^2 = dr^2 + r^2 d\Omega^2$$

$$d\Omega^2 = d\theta^2 + \sin^2\theta \, d\phi^2$$

• Metric in 3 dimensions, arbitrary curvature:

$$ds^2 = \frac{dx^2}{1 - \kappa x^2 / R^2} + x^2 d\Omega^2$$

Curvature radius

Flat: $\kappa = 0, x = r$

Negative: $\kappa = -1$, $x = R \sinh(r/R)$

Positive: $\kappa = 1$, $x = R \sin(r/R)$