



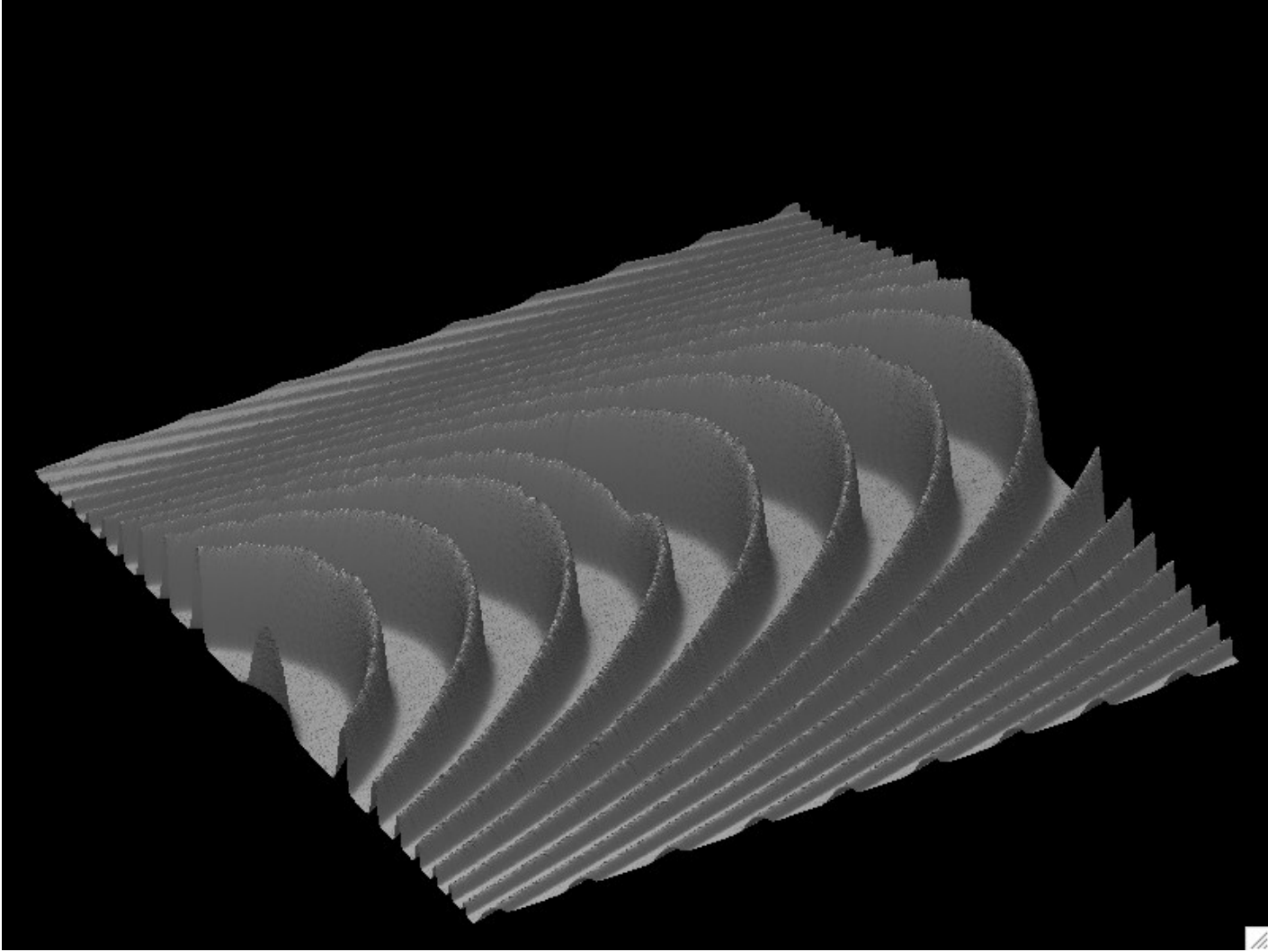
Observational Astronomy

SPECTROSCOPIC
data reduction

Piskunov & Valenti 2002, A&A 385, 1095



Worse-case scenario...





In addition we have calibration data:

- *Bias*
- *Flat field*
- *Dark current*
- *Order tracing*
- *Wavelength map (comparison spectrum)*
- *Blaze calibration*



Spectroscopic reduction in a nutshell

The intensity is given by:

$$I_x = \frac{s - b - d \cdot t}{f - b} \cdot g; \quad \lambda_x = F(x, x_{ThAr}, \lambda_{ThAr})$$

s – signal in science exposure

b – bias level

f – flat field signal

g – gain (e⁻/ADU)

d – dark current signal per unit time

t – exposure time



The problem is the errors:

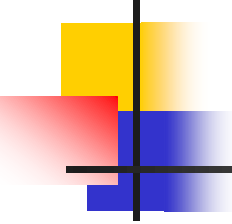
$$\frac{\delta I}{I} = \frac{\sqrt{\delta_s^2 + \delta_b^2 + \delta_{rd}^2 + \delta_d^2}}{s - b - d \cdot t} + \frac{\sqrt{\delta_f^2 + \delta_b^2 + \delta_{rd}^2}}{f - b} =$$

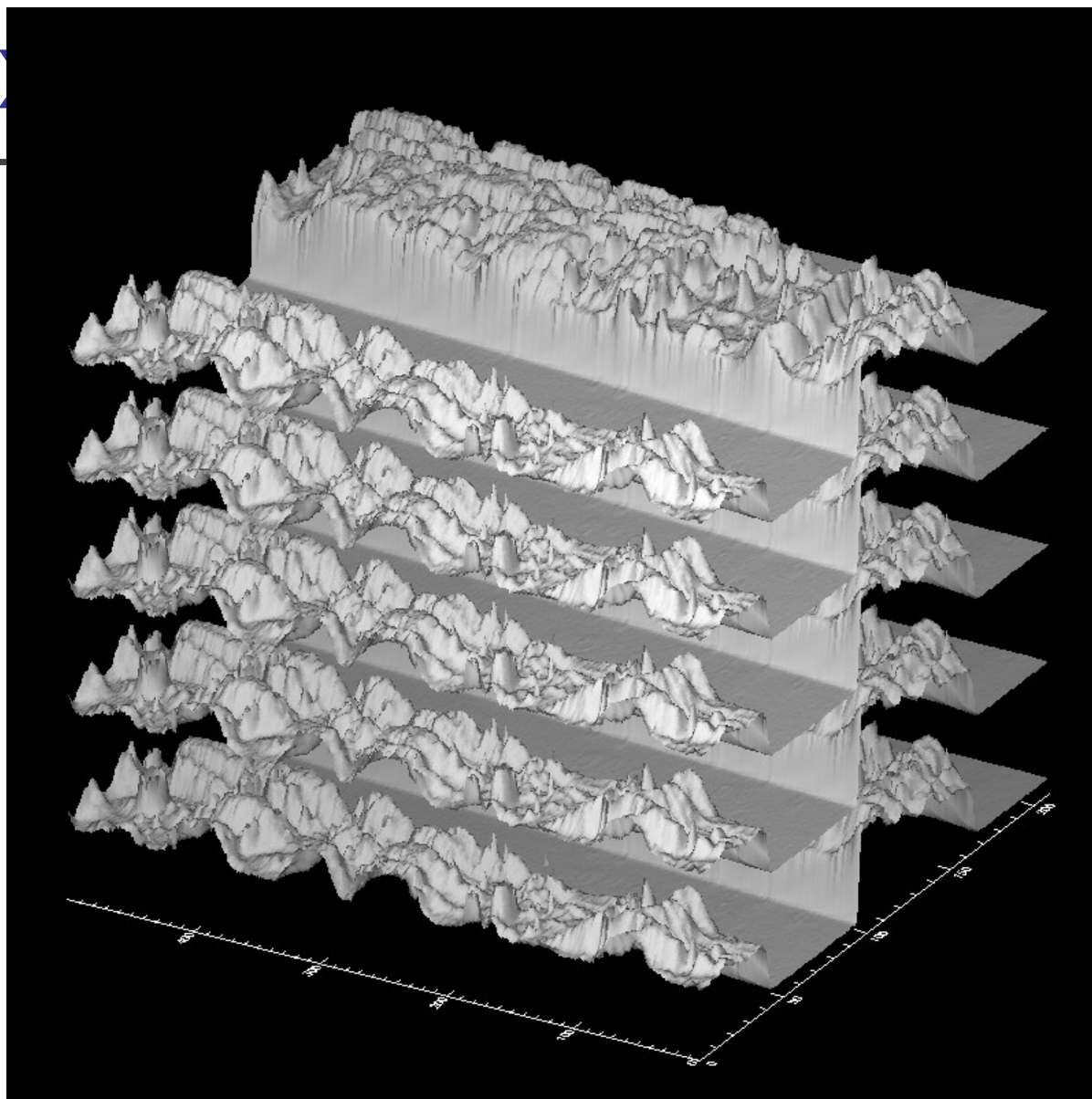
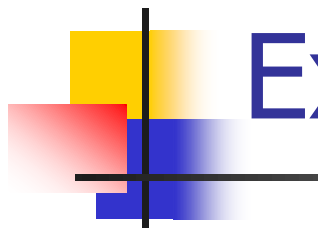
$$= \frac{\sqrt{s + b + \delta_{rd}^2 + d \cdot t}}{s - b - d \cdot t} + \frac{\sqrt{f + b + \delta_{rd}^2}}{f - b};$$

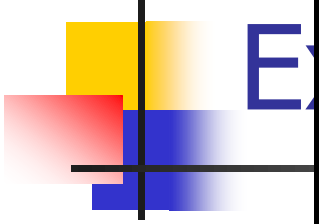
$$\frac{S}{N} = \frac{(s - b - d \cdot t) \cdot (f - b)}{(f - b) \cdot \sqrt{s + b + \delta_{rd}^2 + d \cdot t} + (s - b - d \cdot t) \cdot \sqrt{f + b + \delta_{rd}^2}}.$$

If f is close to b , the S/N is determined by the S/N of the flat field!!!

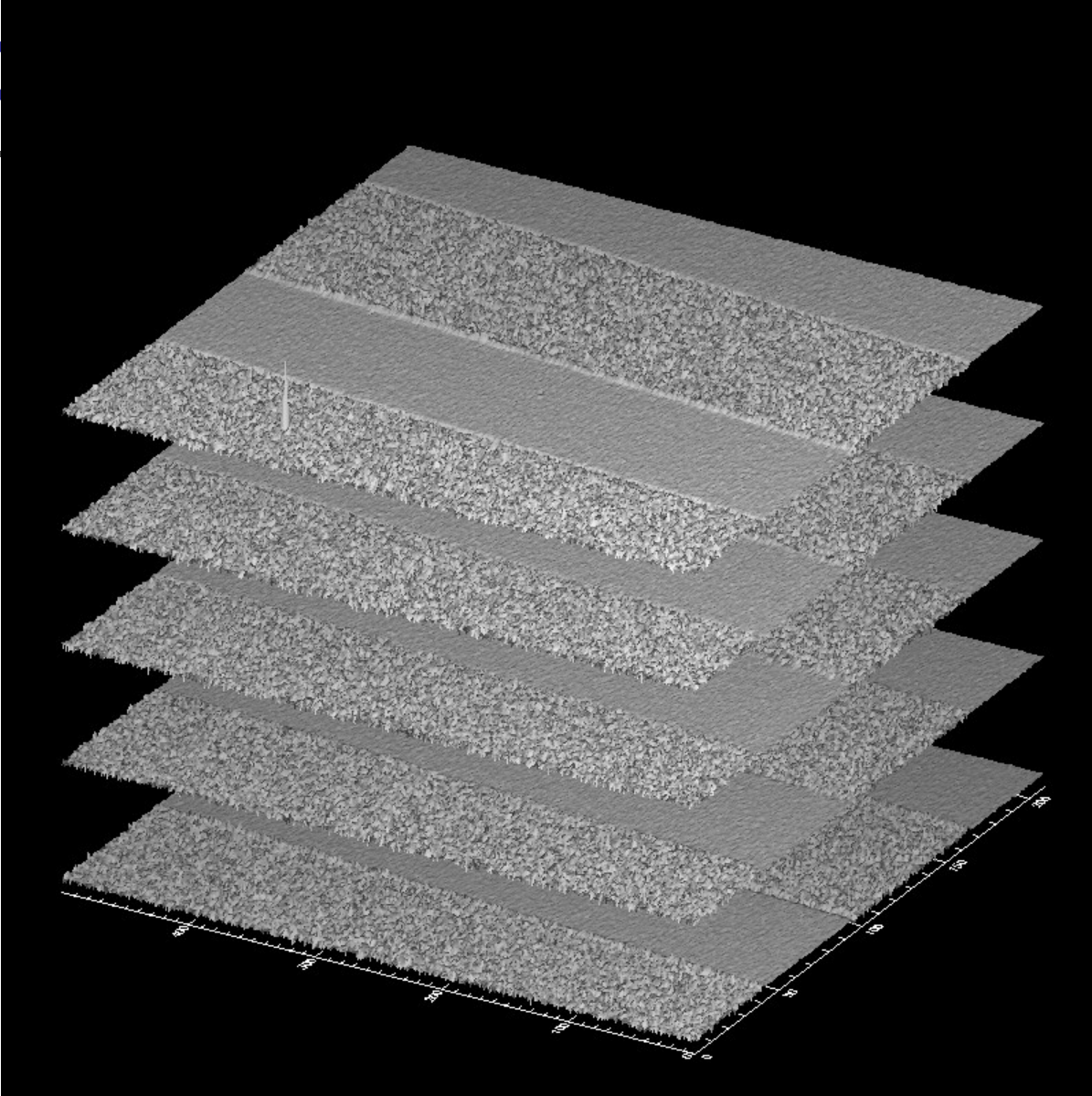
One step at a time: making master bias and master flat/dark

- 
- The goal is to replace the actual calibration data with a model which is free of random noise but carries all the necessary calibration signatures.
 - Master S/N must be much larger than the S/N in science frames!!! Add together signal in many frames
 - Main issue: getting rid of random errors, e.g. cosmic ray hits
 - Method: filtering within a frame or across a stack of frames
 - Cross-check between groups of calibration frames





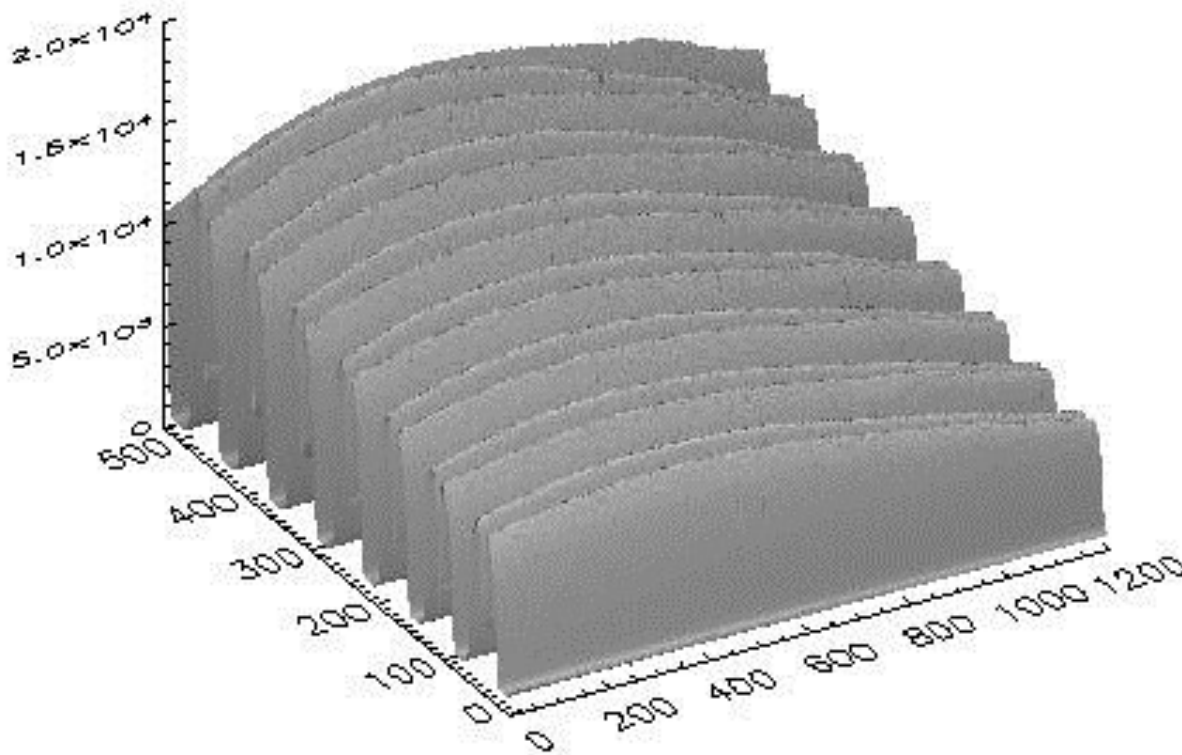
E



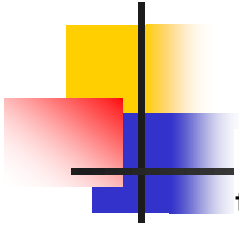
6 times larger vertical scale

Flat field

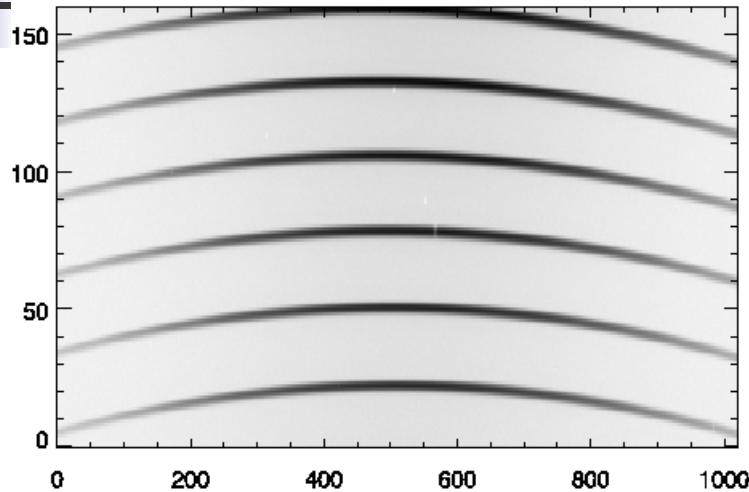
Fragment of a master flat field



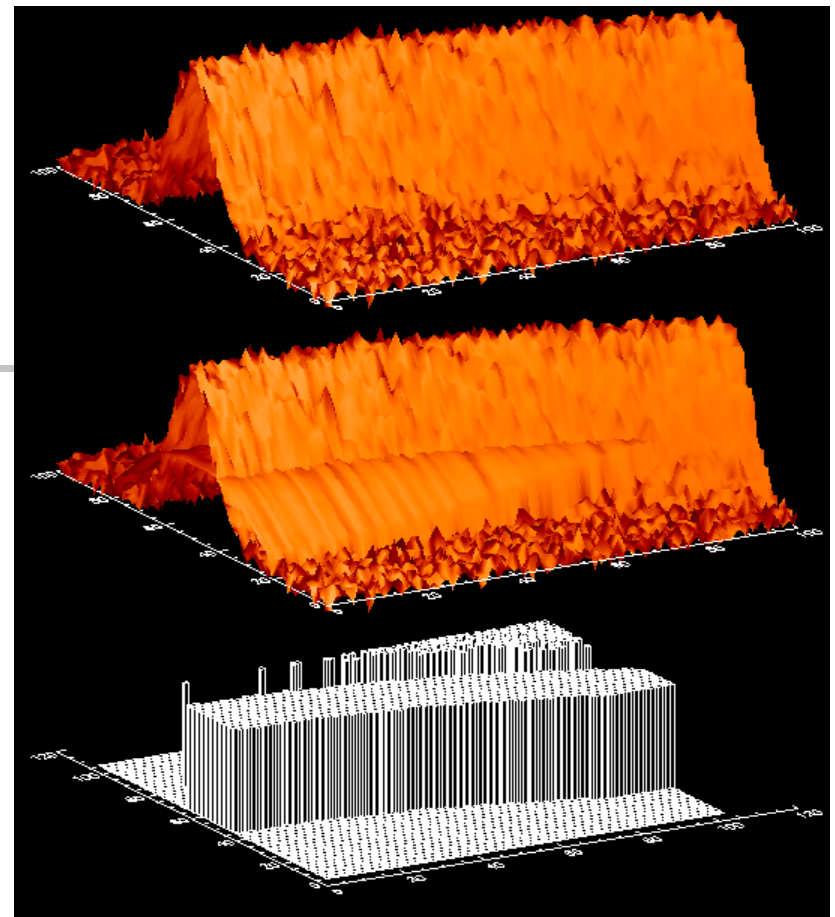
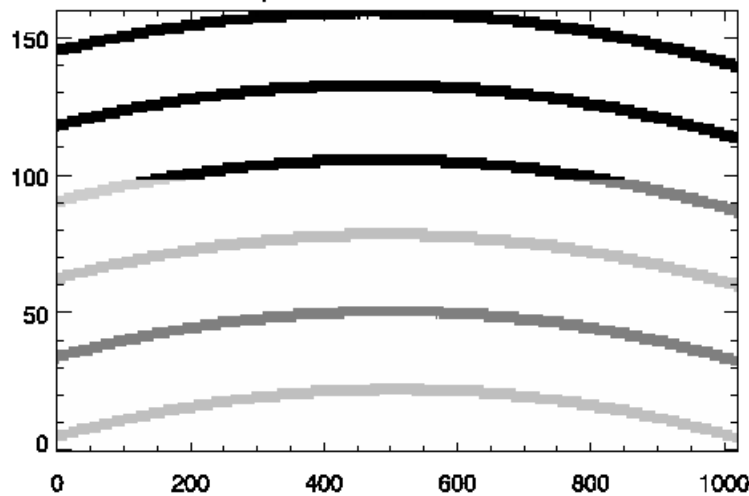
Order tracing



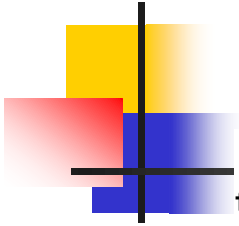
Fragment of an order definition frame



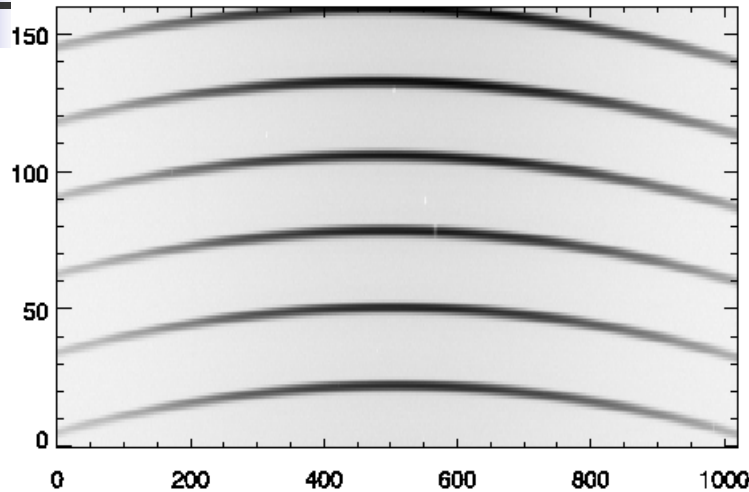
Selected pixels and cluster identification



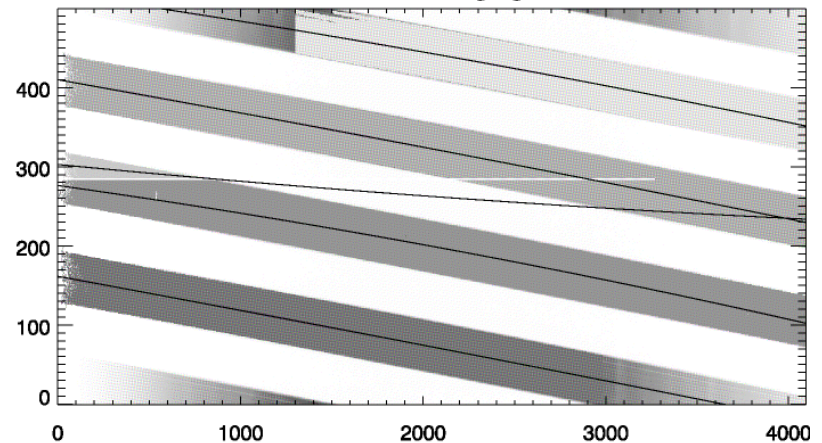
Order tracing (2)



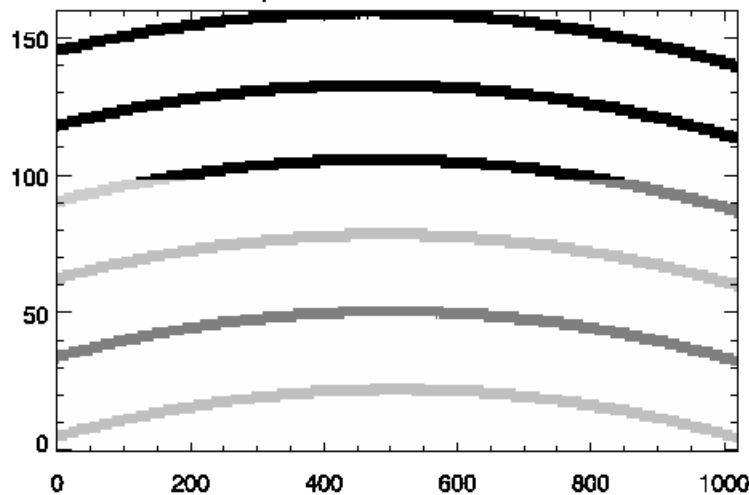
Fragment of an order definition frame



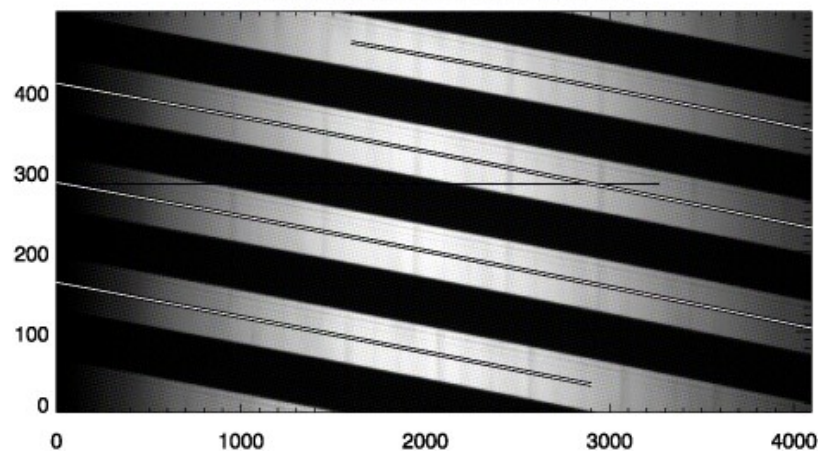
Cluster merging



Selected pixels and cluster identification

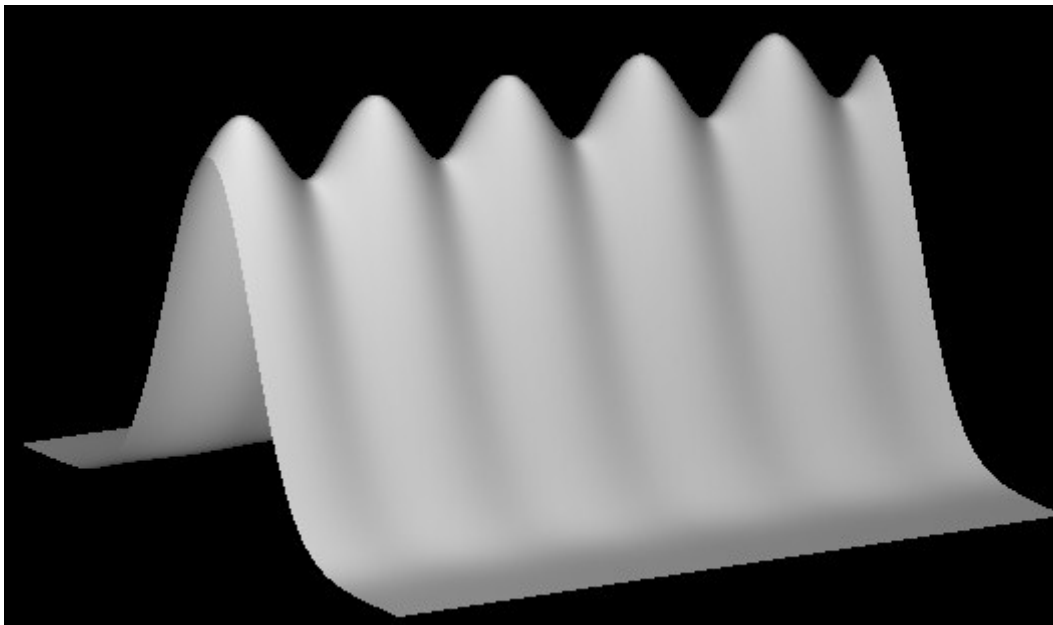


Final definition of order locations



Conceptual Algorithm

Any point in the focal plane can (in principle) be represented by a product of the *spectrum* and the *slit illumination function* $f(x, y) = P(x) \cdot L(y - y_c)$



$$\underbrace{P(x)}_{(\sin x + a)} \cdot \underbrace{L(y)}_{e^{-\left(\frac{y}{b}\right)^2}}$$

looks like a real spectral
order





Now the Real Thing...

- CCD pixel with coordinates x and y is given by:

$$f(x, y) = P(x) \cdot \int_y \Pi(y' - y_c) \cdot L(y') dy'$$

- In practice we reconstruct the slit function L on some discrete grid with resolution \geq than CCD pixels. Thus we can write:

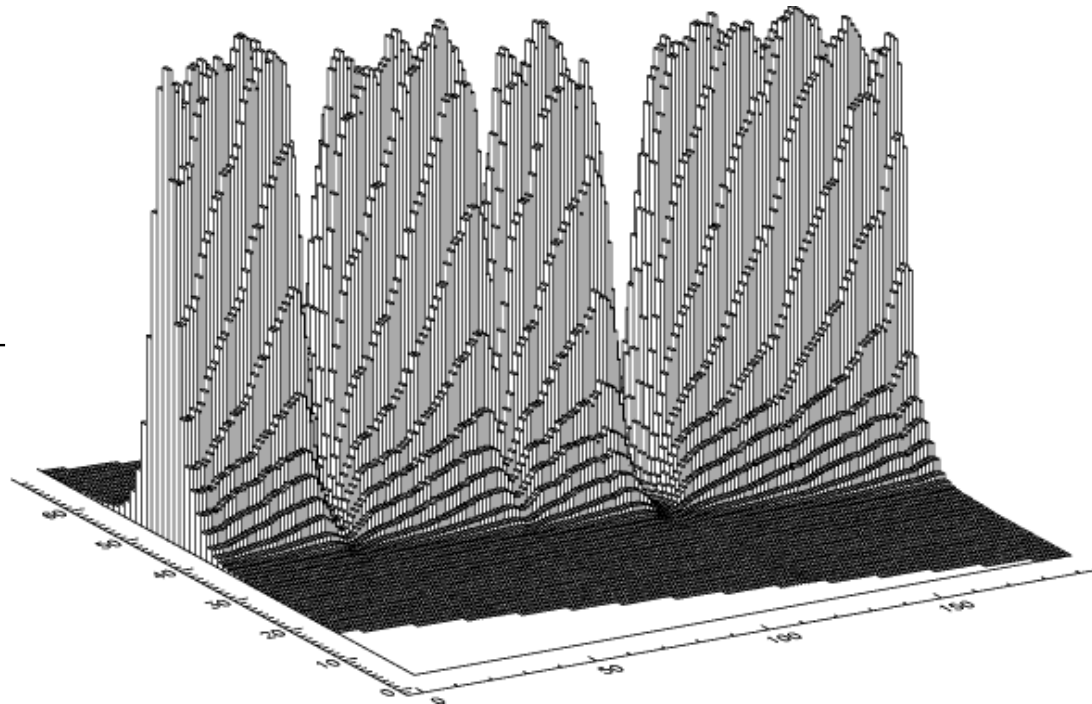
$$f(x, y) \approx P(x) \cdot \sum_j \omega_{x,y}^j L_j$$

Slit function decomposition

Ideal model: Image on CCD is a sequence of monochromatic images of the entrance slit sampled with CCD pixels

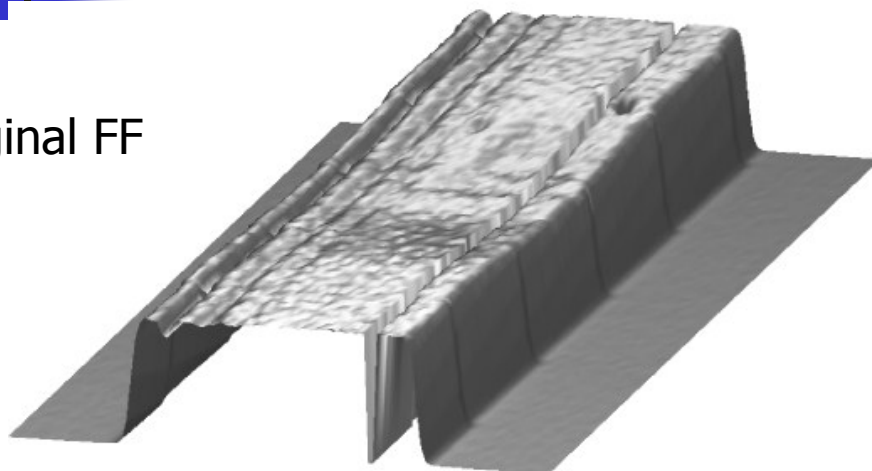
$$S_{xy} = Sp_x \times Sf_y$$

$$S_{xy} = \sum_{i \in y} \omega_{i,x,y} Sp_x Sf_{i+}$$

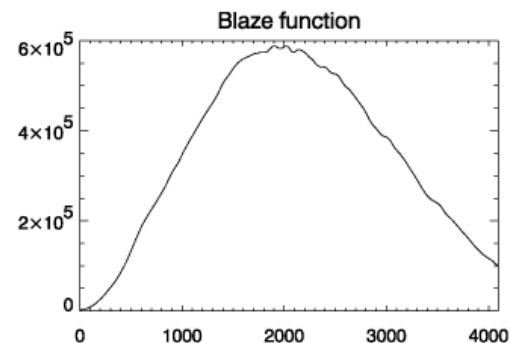
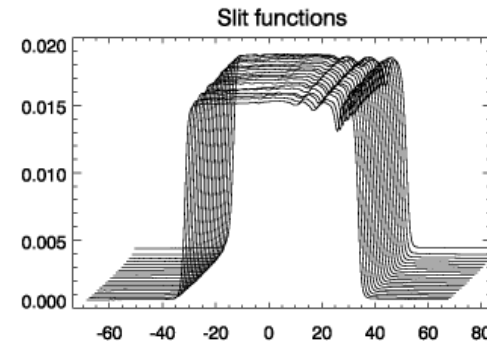


Normalizing flat field

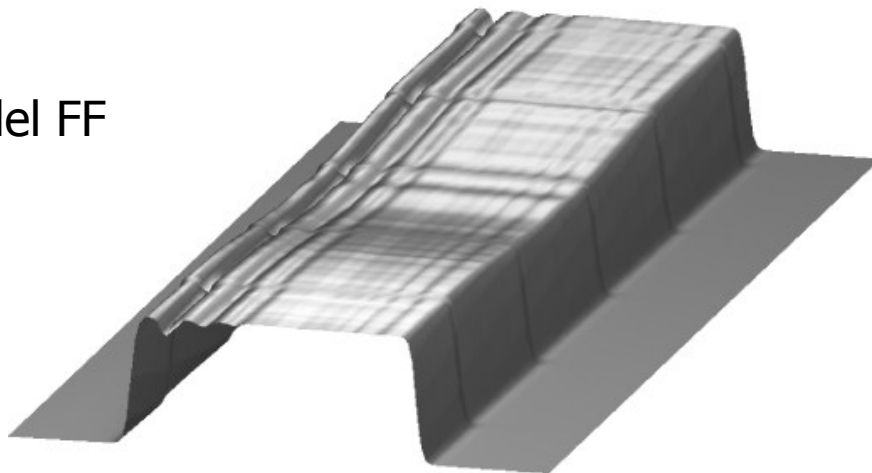
Original FF



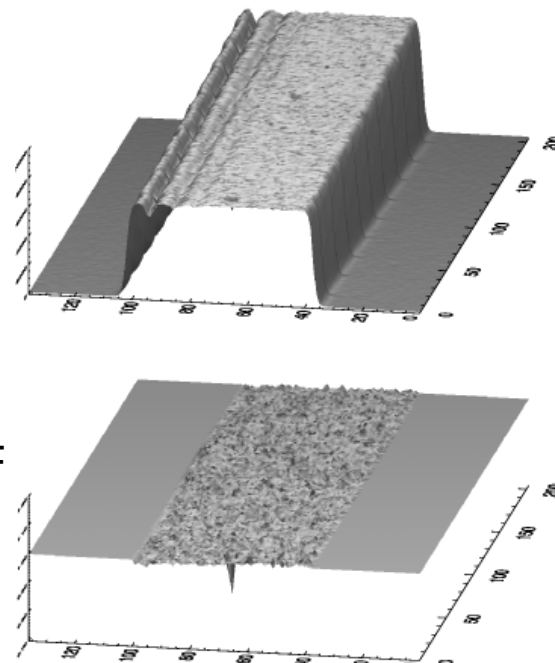
"Spectrum"



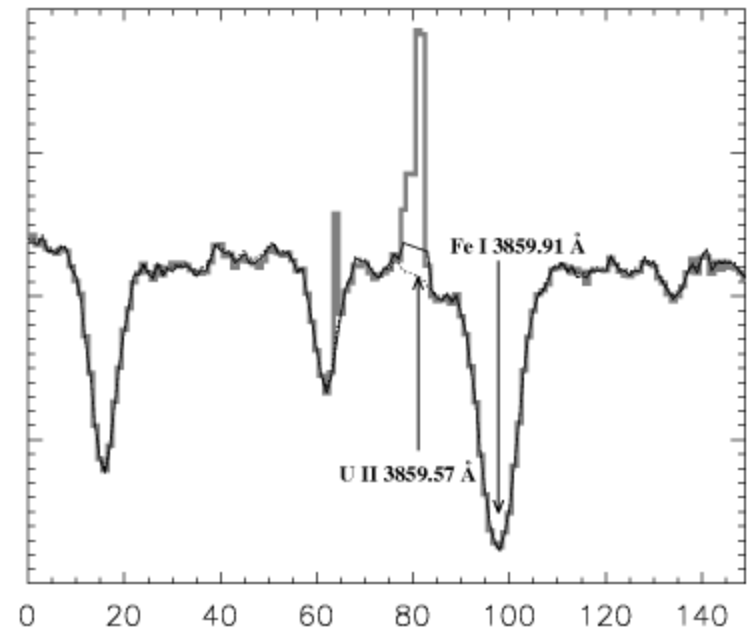
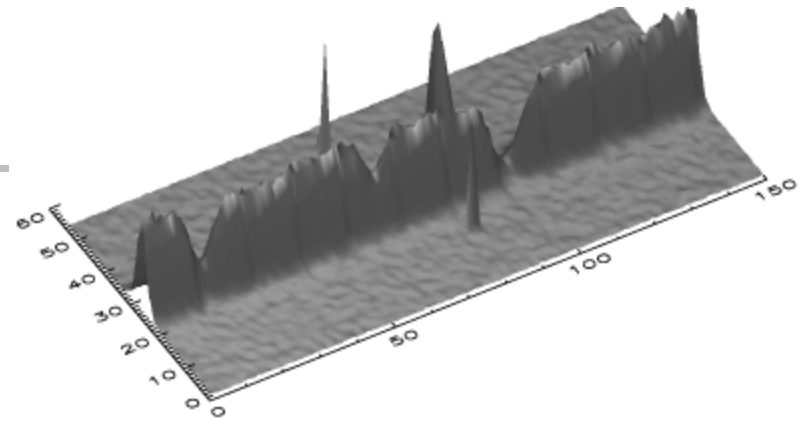
Model FF



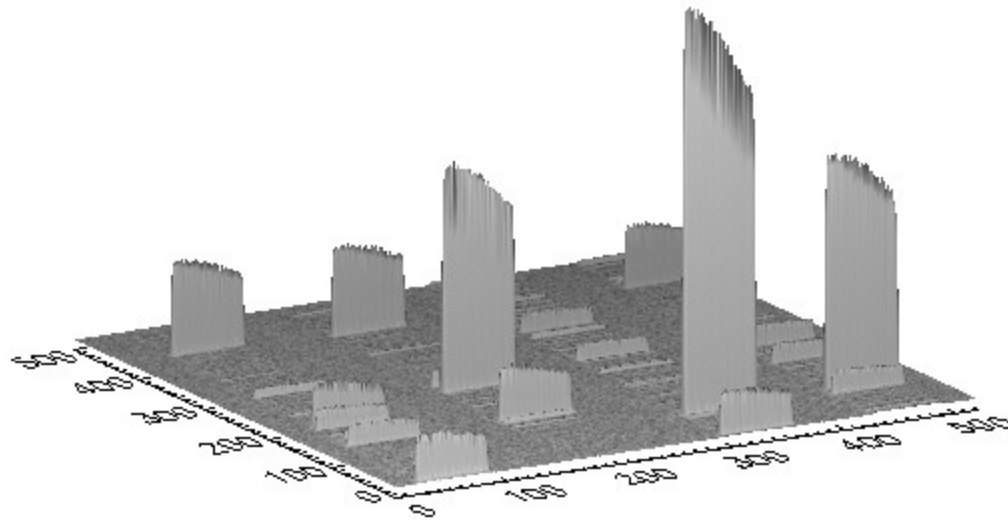
Normalized FF



Extracting science spectrum



Wavelength calibration



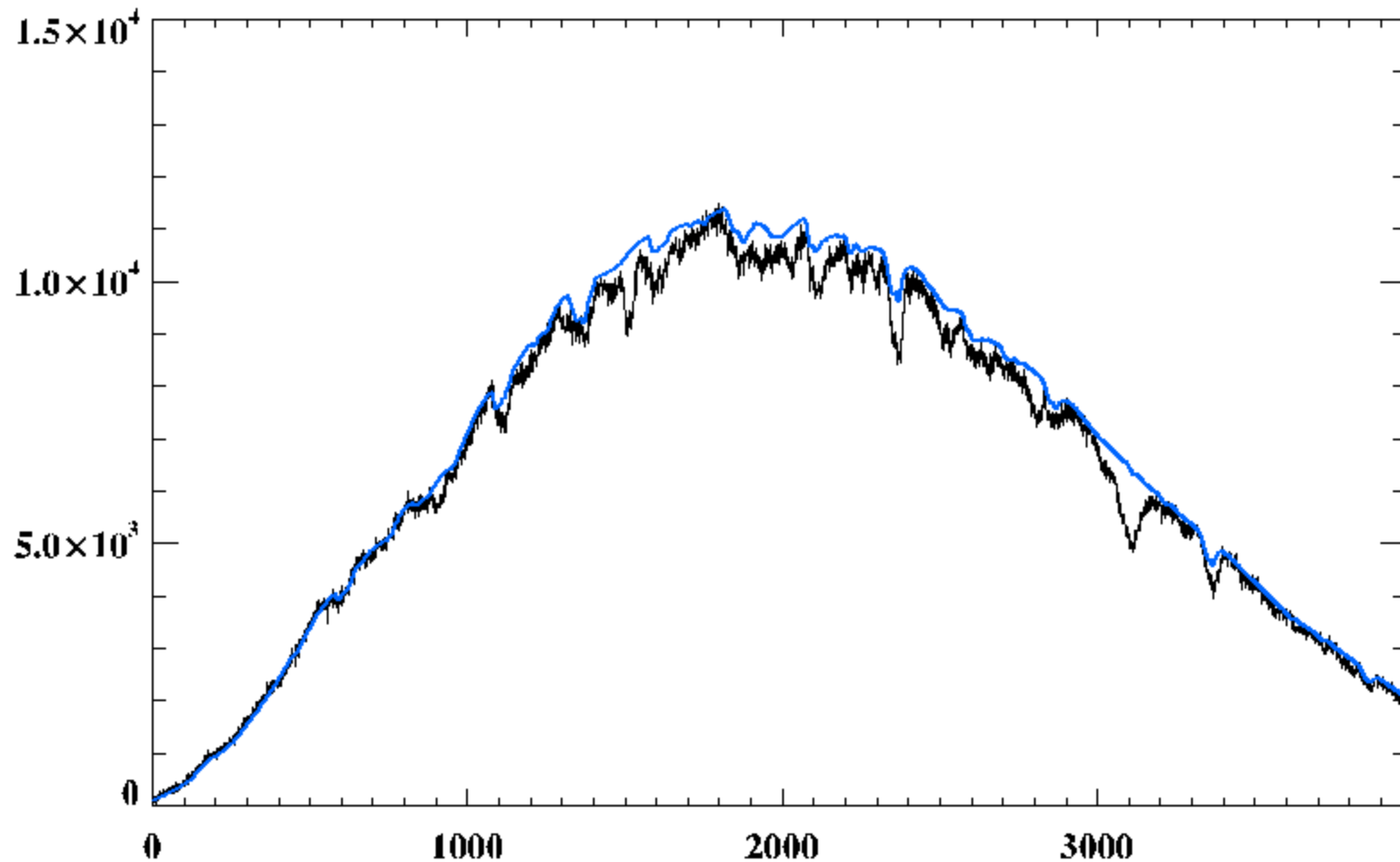
$$\lambda_{x,m} = \sum_{i,j} a_{i,j} m^i x^j$$

Order number

Pixel number

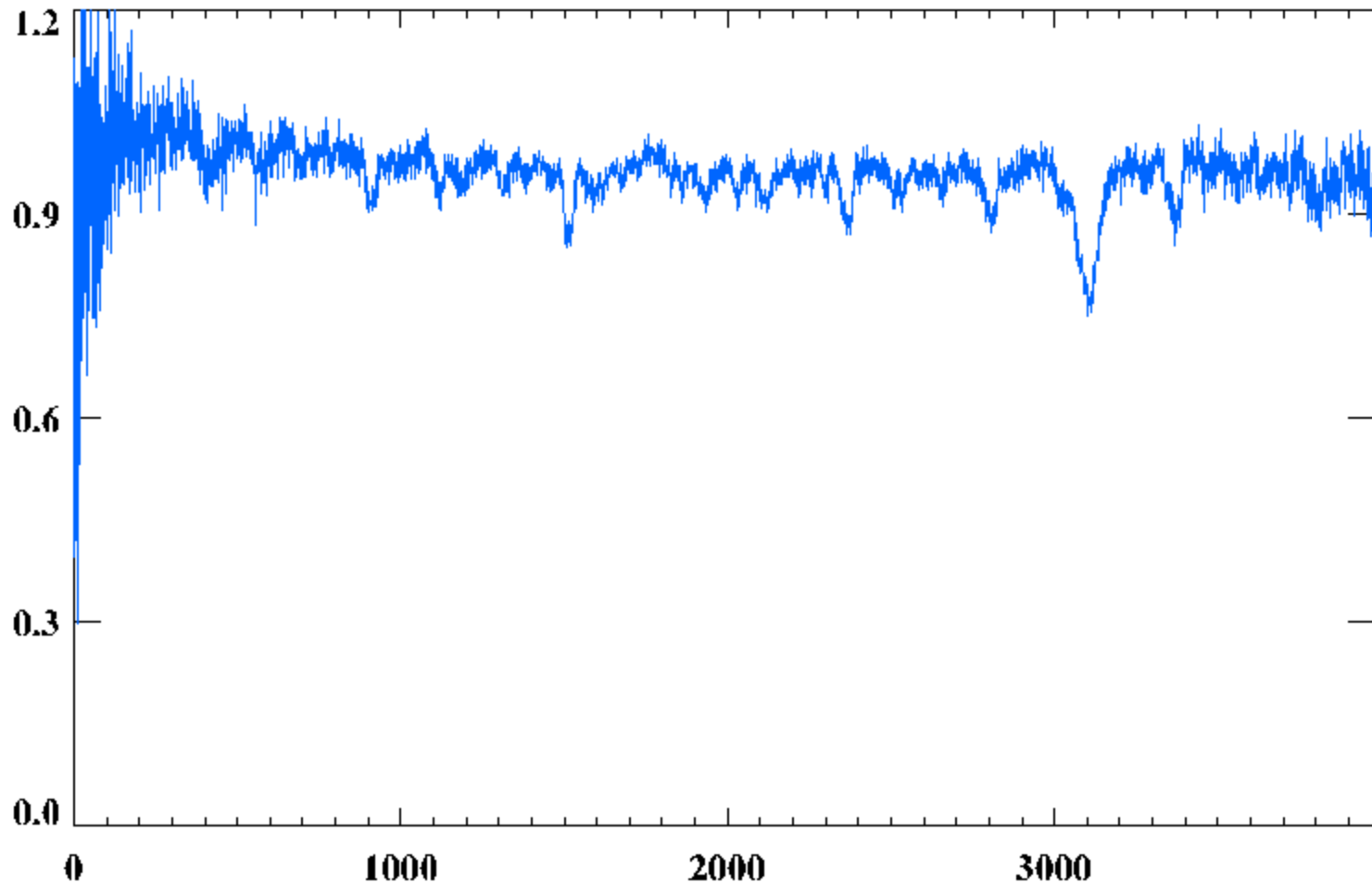


Continuum fit



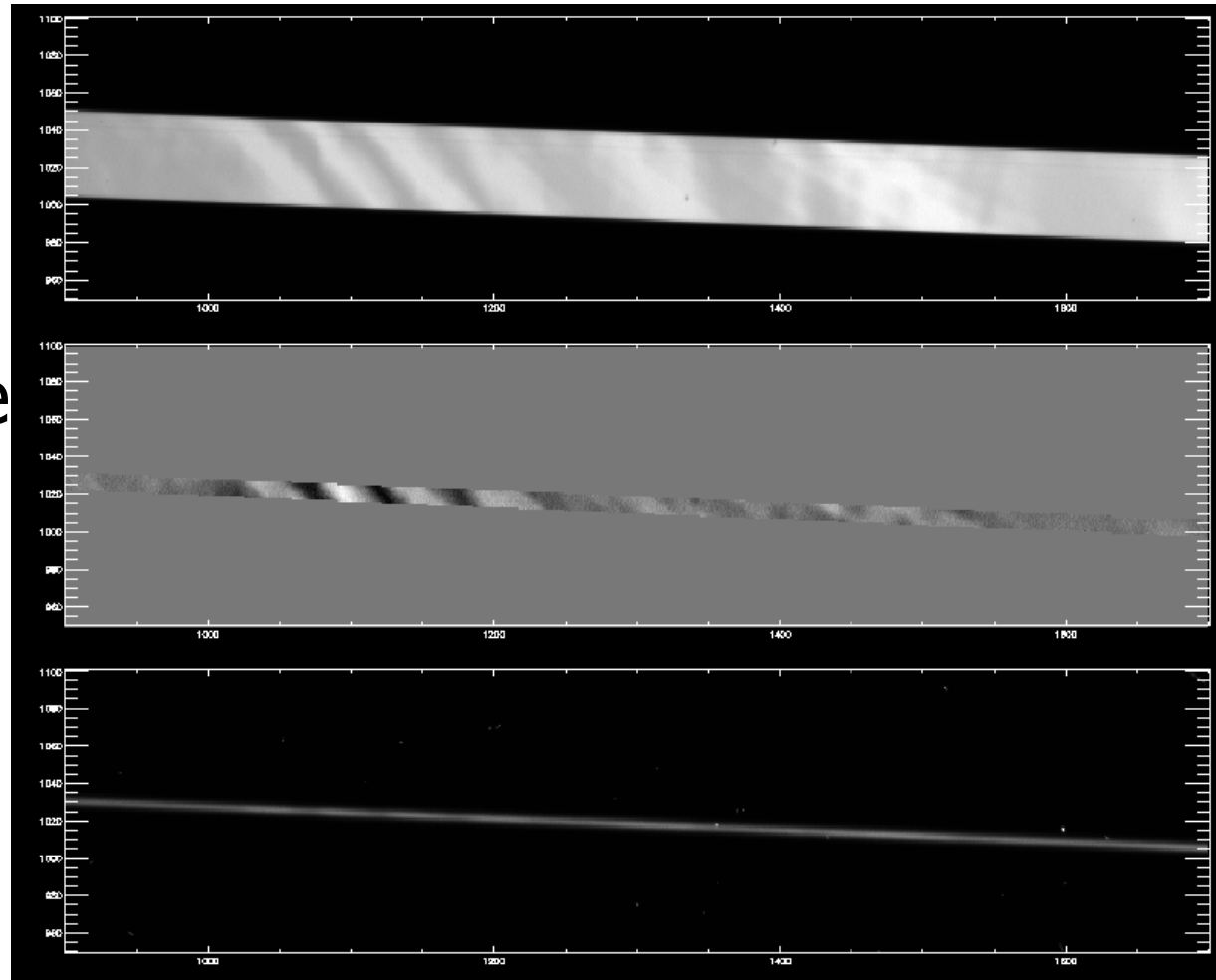


... but it is not perfect

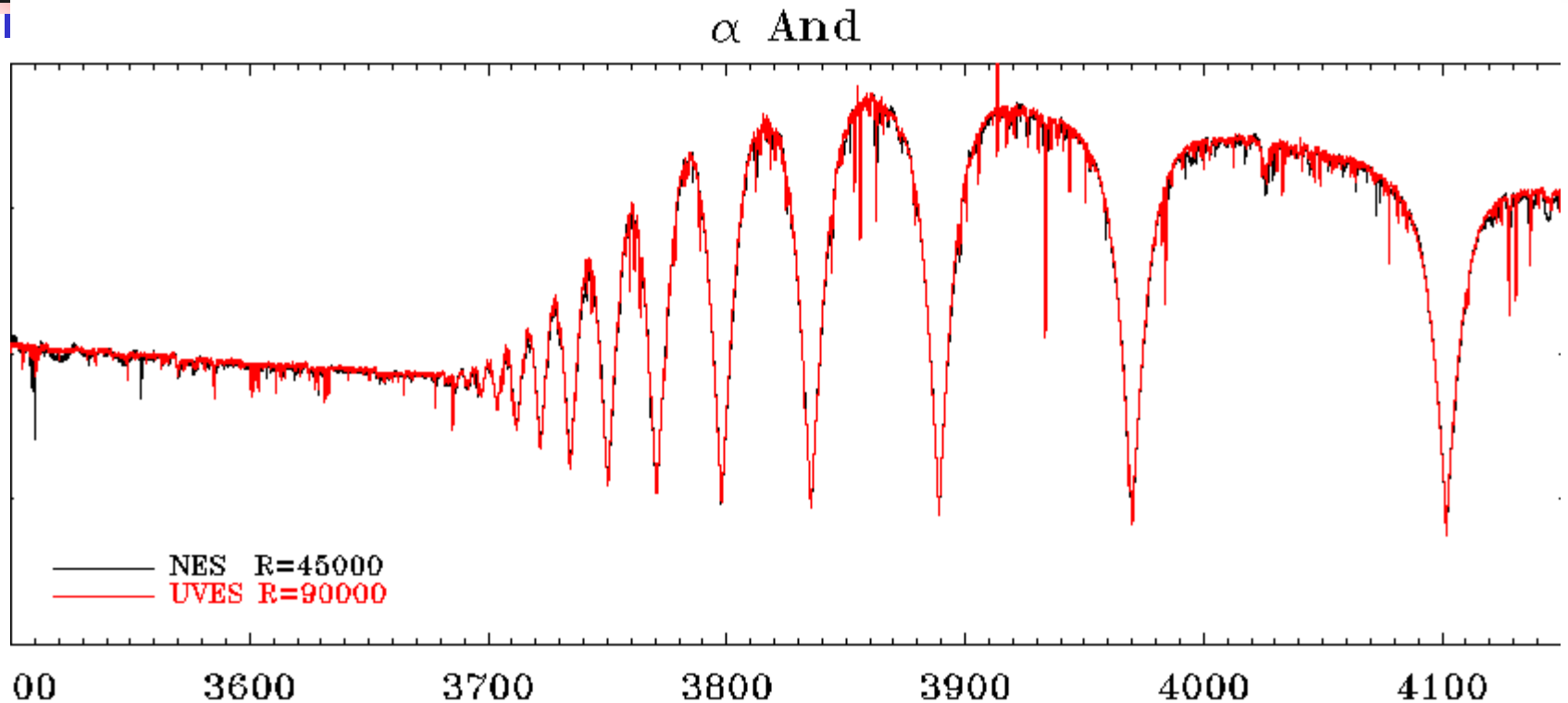


Fringing

Accurate fringing removal requires identical slit illumination by the FF as it is illuminated by the science target



Comparison with other algorithms



UVES POP Library, Bagnulo et al. 2003, Messenger 114, 10



FIES data reduction

- Attend a tutorial on using REDUCE
- Setup your own reduction script to create:
 - Master bias
 - Master flat
 - Normalized flatand to extract:
 - ThAr
 - your science spectra + pulsating star spectra
- Create a wavelength solution using *wavecal* and ThAr spectrum
- Fit the continuum using *make_cont*
- Compare spectra in selected wavelength regions