



# Observational Astronomy

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# SPECTROSCOPY and spectrometers

Kitchin, pp. 310-370



# Spectroscopic methods

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- Different purposes require different instruments
- Main spectroscopic methods:
  - *Spectrophotometry*
  - *Low resolution*
  - *Long slit, high resolution*
  - *High resolution*
- Spectroscopic observations are characterized by: *dispersion/spectral resolution* and *spectral range*



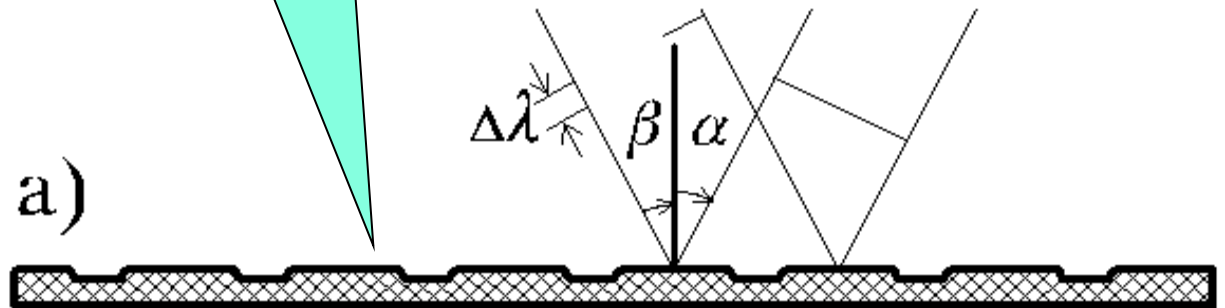
# Spectrophotometry

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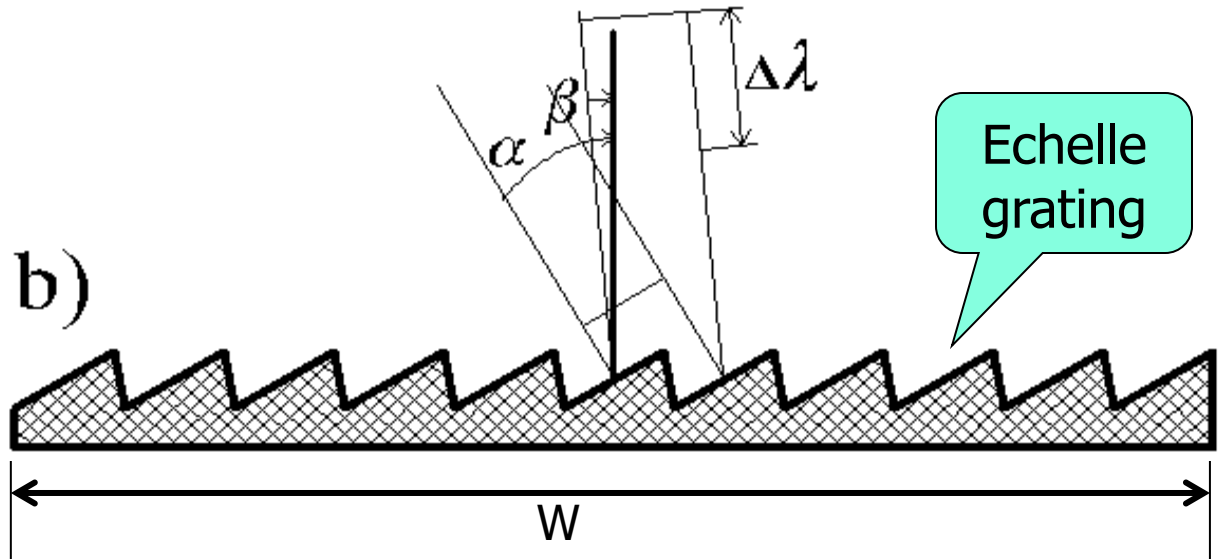
- Typical goal: search for objects with specific spectral features
- Method 1: objective prism, telescope "sees" the source through a prism, therefore each point source looks like a small spectrum
- Method 2: narrow band filters for given spectral features. Often such filters have the possibility to change central wavelength by changing temperature/pressure. There is no slit!

# Gratin

Conventional  
grating



Interference:



Grating formula:  $OPD = \delta \sin \alpha + \delta \sin \beta = m\lambda$

Optical path difference



## A bit of math:

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- Expression for angular dispersion is found by differentiating the grating eq.:

$$md\lambda = \delta \cos \beta d\beta$$

$$\frac{d\lambda}{d\beta} = \delta \cos \beta / m \quad \text{Angular dispersion}$$

- Linear dispersion is readily obtained for a given focal length

$$\frac{d\lambda}{dx} = \delta \frac{\cos \beta}{m \cdot f_{\text{cam}}} \quad \text{Linear dispersion}$$



... and some more ...

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- Angular resolution. Think of a grating as a mirror, its diffraction angle is given by:

$$\Delta\beta = \lambda / (W \cdot \cos \beta)$$

Projected size of the grating

- ... and combining it with the angular dispersion equation:

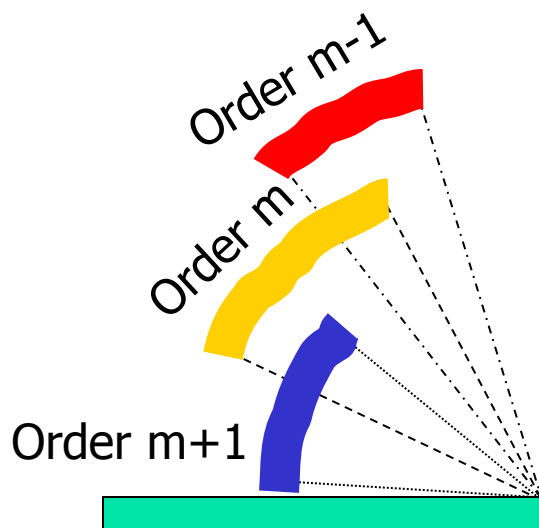
$$\frac{\lambda}{\Delta\lambda} \equiv R = m \cdot \frac{W}{\delta} = m \cdot N$$

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- *Resolving power* depends in the number of illuminated grooves!

# Free spectral range

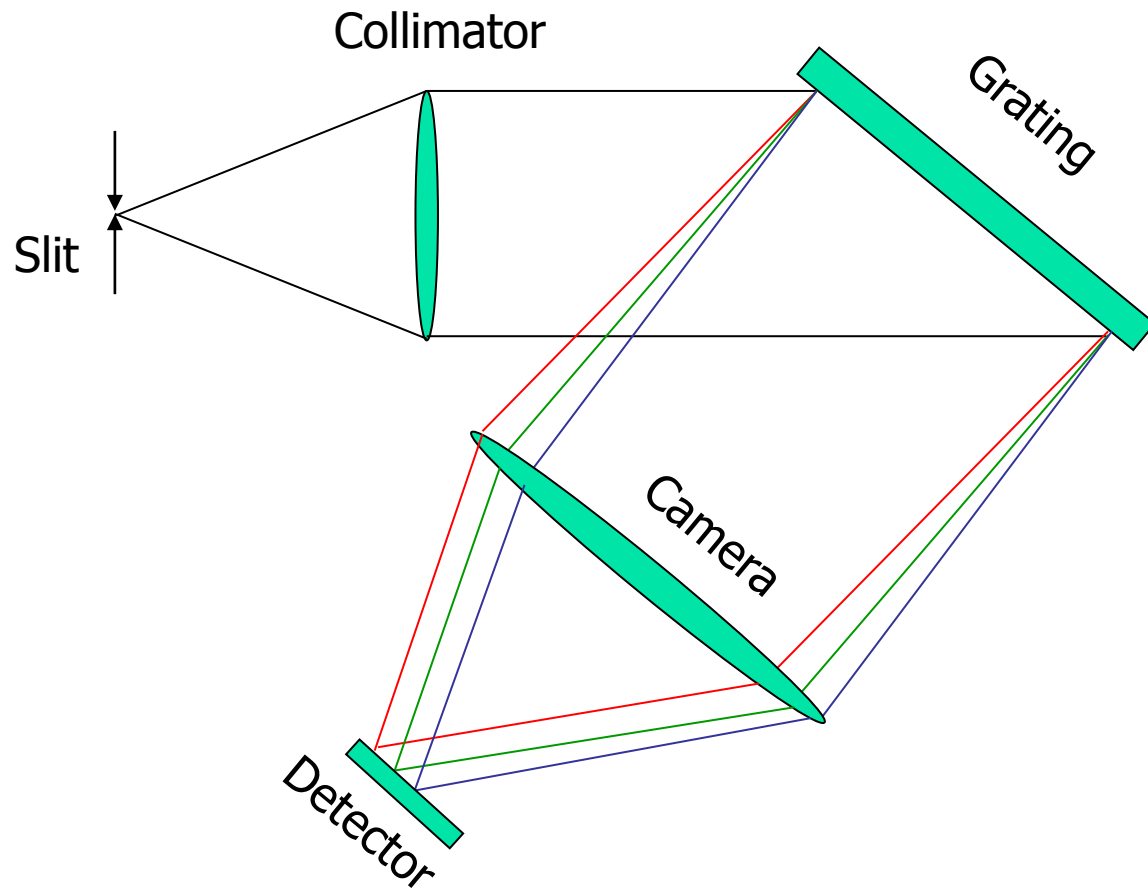
The free spectral range (FSR) of a diffraction grating is defined as the spectral interval in a given order which does not overlap with the wavelengths in adjacent orders.



$$\begin{aligned} \text{FSR} &= \lambda_m - \lambda_{m+1} = \frac{\delta \sin \beta}{m} - \frac{\delta \sin \beta}{m+1} = \\ &= \frac{\delta \sin \beta}{m \cdot (m+1)} \end{aligned}$$

For a prism FSR is the whole sp. range!

# Grating spectrometers





# Real world: the seeing and the pixel size

- The angular slit size as seen by the grating is:

$$\Delta\alpha = s / f_{\text{coll}}$$

where  $f_{\text{coll}}$  is the focal length of the collimator and  $s$  is the linear width of the slit. Grating equation connects this to the angular resolution element:

$$\Delta\alpha \cos \alpha = s / f_{\text{coll}} \cos \alpha = -\Delta\beta \cos \beta$$

$$|\Delta\beta| = \frac{s \cdot \cos \alpha}{f_{\text{coll}} \cdot \cos \beta}$$

- If we try to match this to the angular resolution of the grating we end up with too narrow slit.
- In practice, we select the slit, translate this to angular resolution and select the camera focal length to match the pixel scale.



# Putting some numbers

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## Home work

The spectrograph for the BWT is based on a 20 cm grating with a blaze angle of  $66.5^\circ$  and 72 grooves per mm

- Find angular resolution of the grating at  $4000 \text{ \AA}$ ,  $6000 \text{ \AA}$  and  $8000 \text{ \AA}$
- Find optimal slit size with collimator length of 80cm
- Take a realistic seeing ( $2''$ ) and the corresponding entrance slit size. Compute the resolution  $R$  and the camera focal length to achieve 3 pixel sampling of a resolution element (15 micron pixel size)
- Why is it hard to make high-resolution spectrometers for large telescopes? How the size of the primary mirror affects parameters and dimensions of a spectrometer?



# Modern concept

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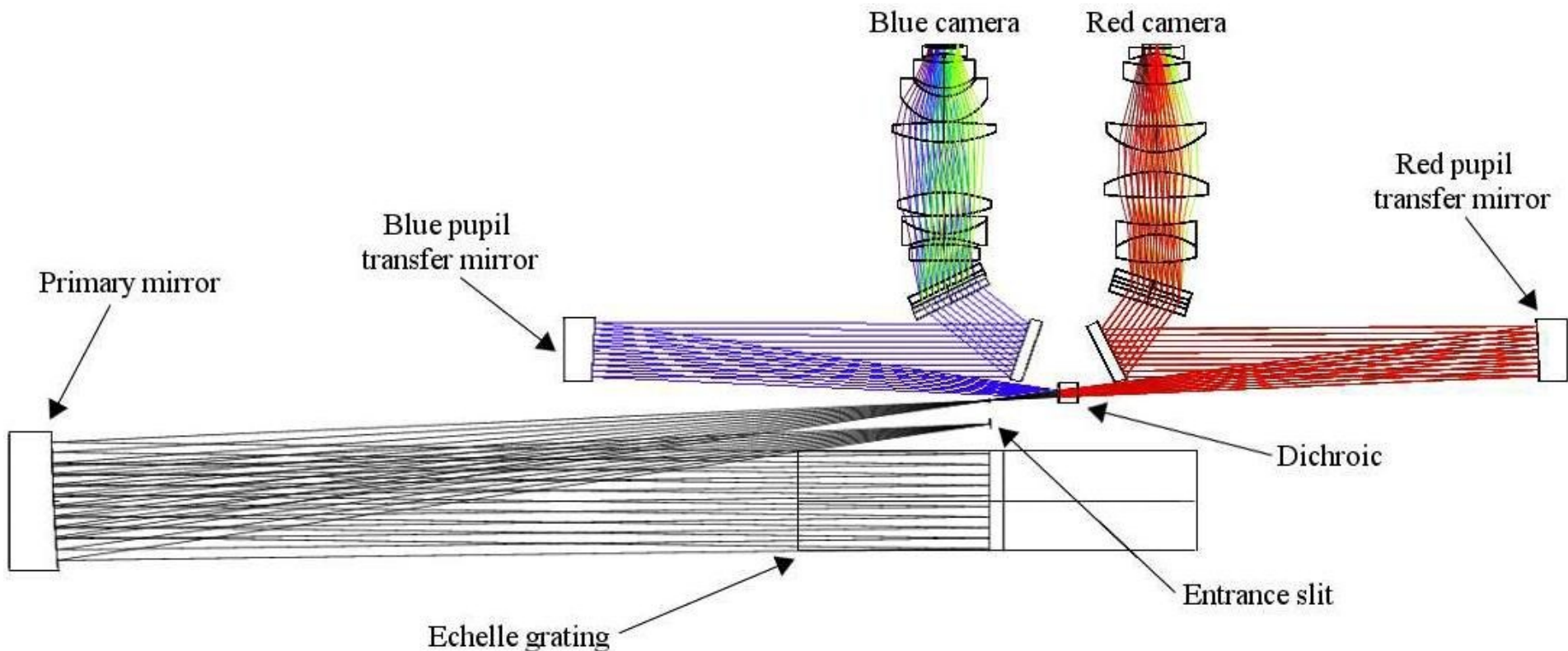
- Echelle gives high resolving power (high orders) and high efficiency (no dark stripes)
- Spectral orders overlap (maximum reflection at blaze angle)  $\Rightarrow$  order selection or cross-disperser is needed (e.g. grating or prism)
- Central wavelength of order  $m$  is given by:

$$\lambda_m = 2\delta \sin \theta_{\text{blaze}} / m$$

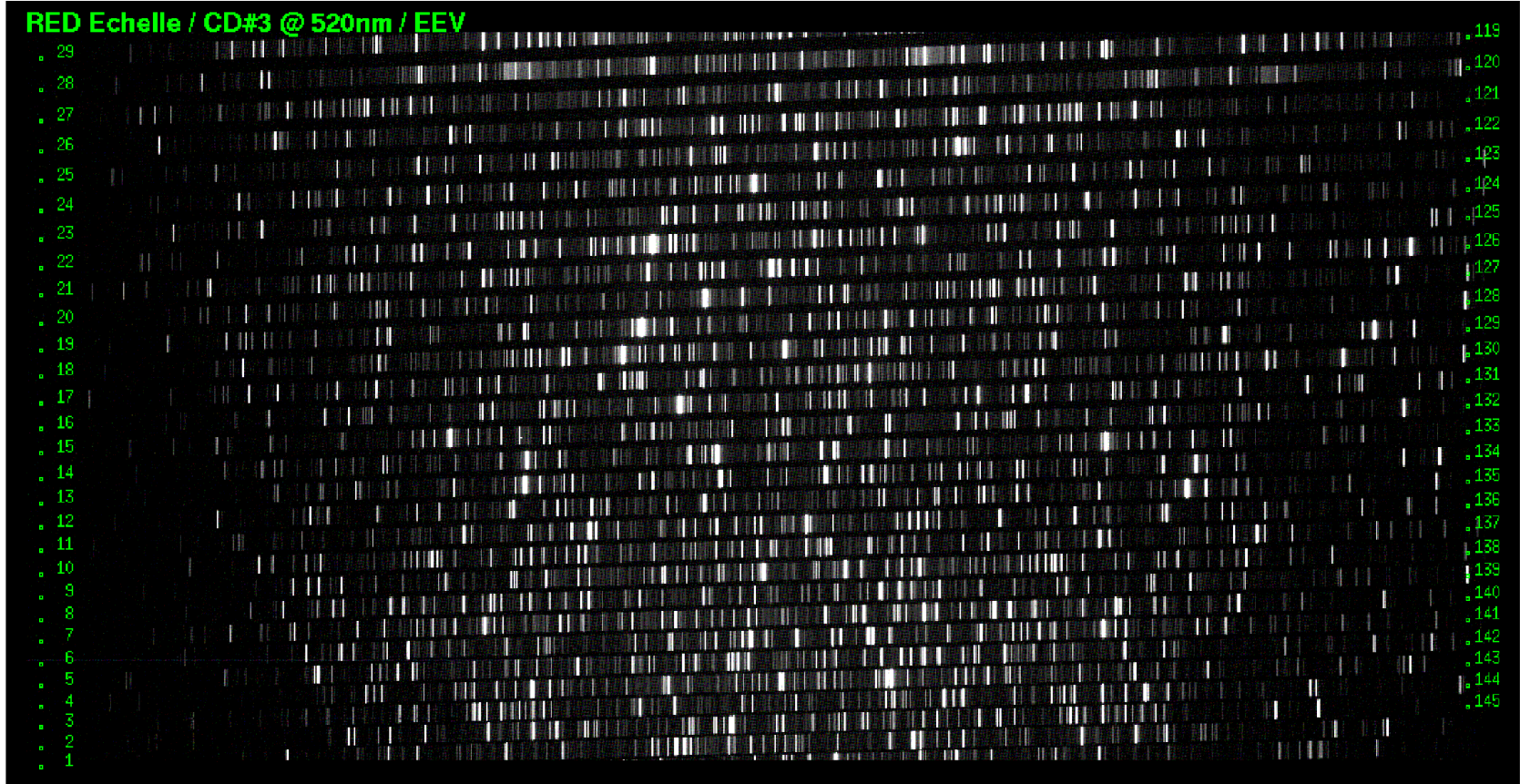
- With a cross-disperser the whole spectrum is packed in a rectangular 2D format, perfect for an electronic detector

# Spectrograph designs

## Echelle, white pupil (e.g. SALT-HRS)



# Echelle focal plane layout







# Side effects

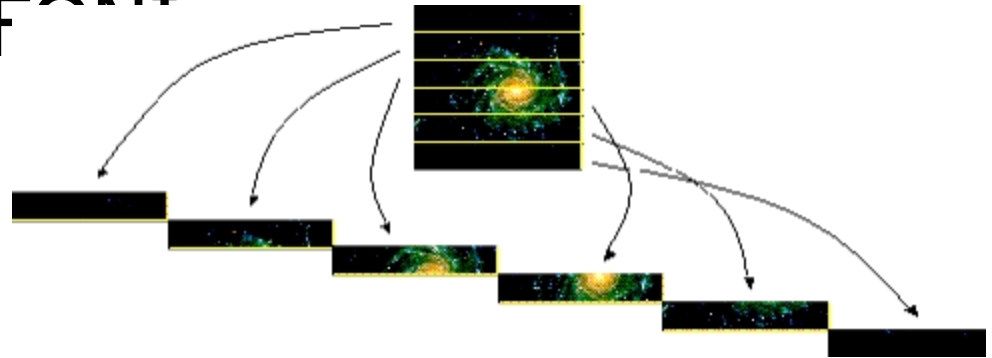
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- Orders are curved
- Order spacing changes
- Short FSR
- Camera aberrations directly affect resolution
- Hard to calibrate fringing

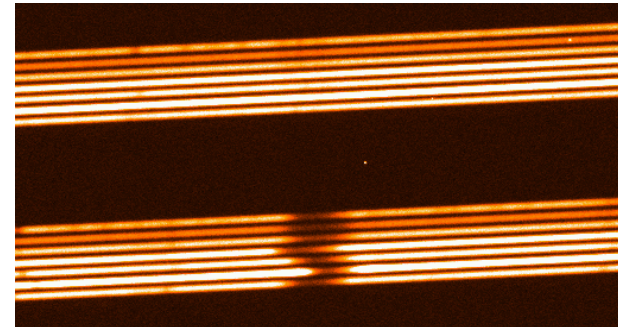


# Other spectroscopic instruments

- IFU instruments  
2D image slices are re-arranged in 1D slit. E.g. SINFONI



- Multi-object instruments.  
E.g. FORS, FLAMES



# Fabry-Perot interferometer

- The resolution is determined in the same way as for a grating
- Transmission/Reflection ratio depends on the wavelength
- The ratio between the reflection and the transmission peaks is called *finesse*
- F-P is often used as tunable filter

